



Post QM17 : Flow

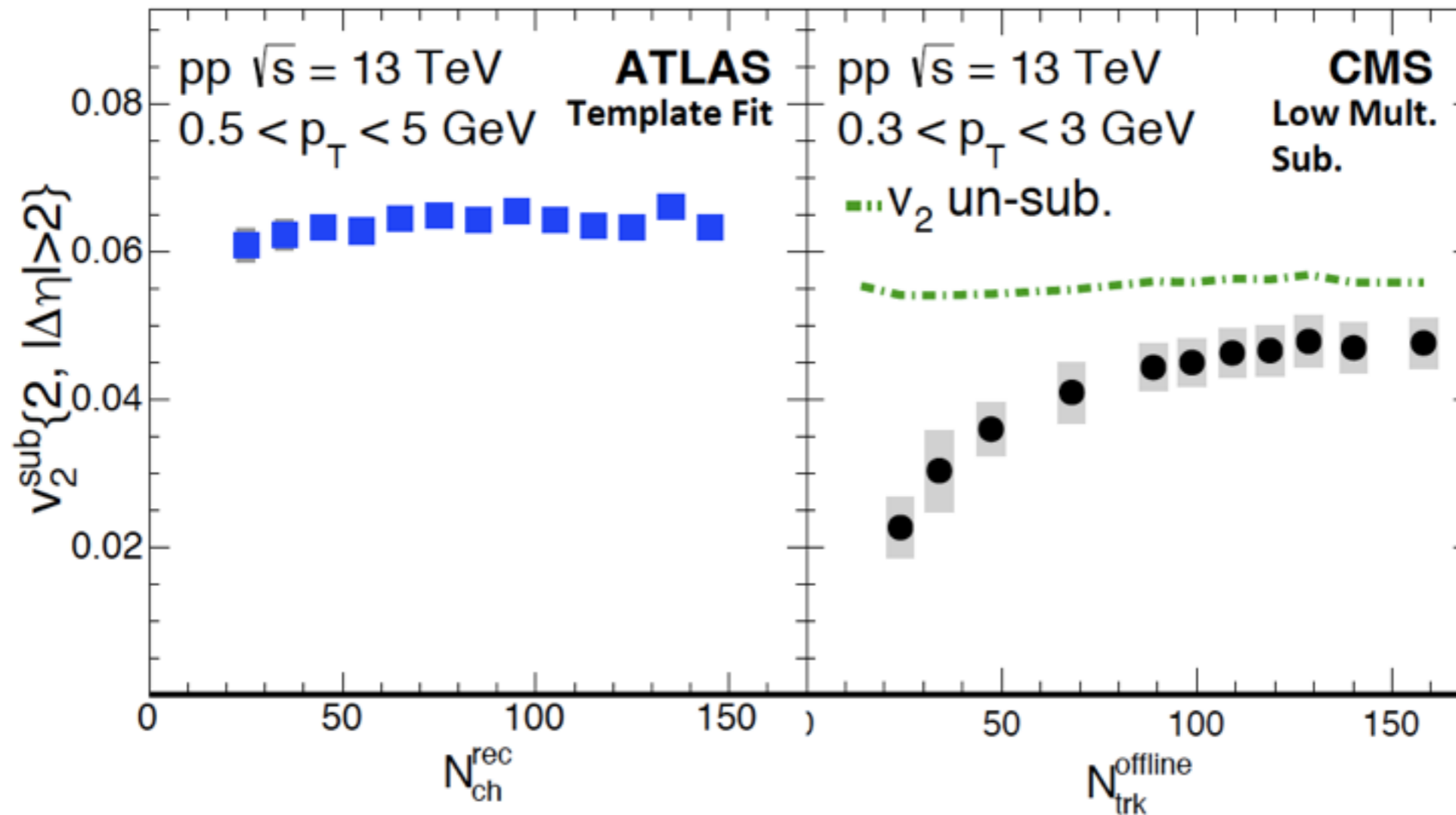
Hiroshi Nakagomi
Univ. of Tsukuba

Contents

- pp 13TeV at LHC
- p/d/³He+Au at RHIC
- Longitudinal direction
 - Event plane de-correlation
 - Forward/backward asymmetry of v_n
 - HBT
- Event shape engineering
 - HBT
- Low energy(Fixed target HADES)
 - v_3 w.r.t Ψ_1

v_2 in p+p 13 TeV

CMS Zhenyu Chen

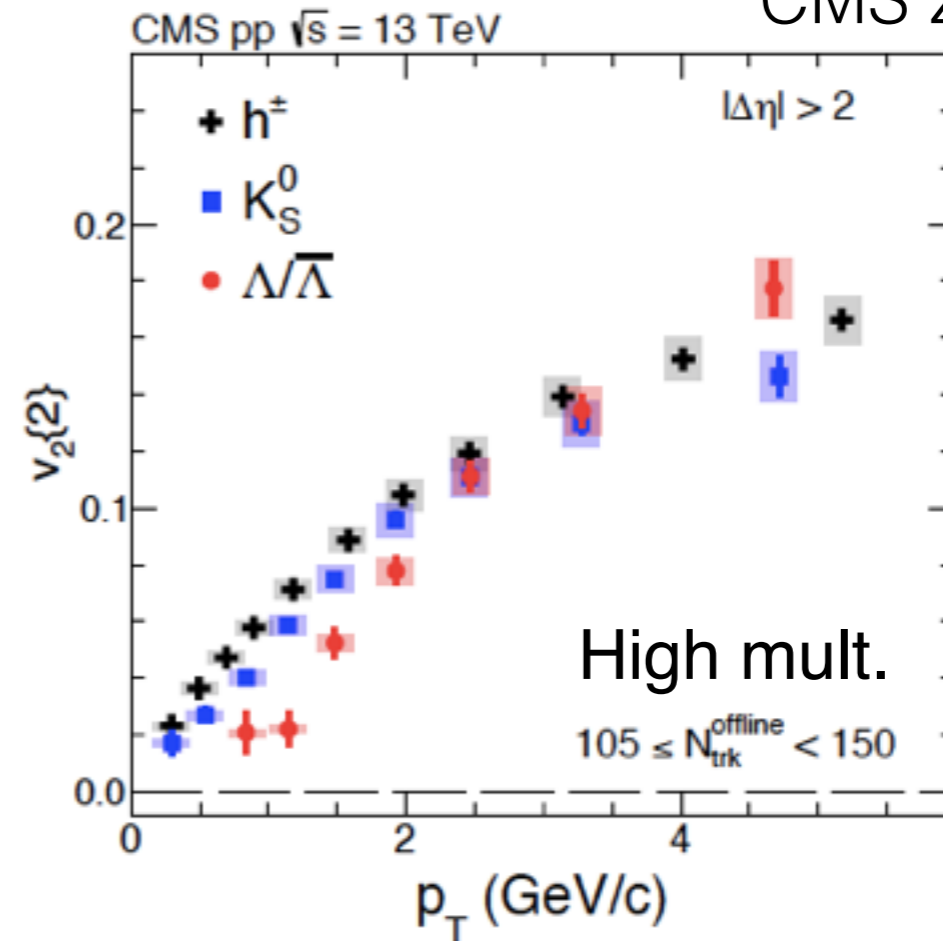
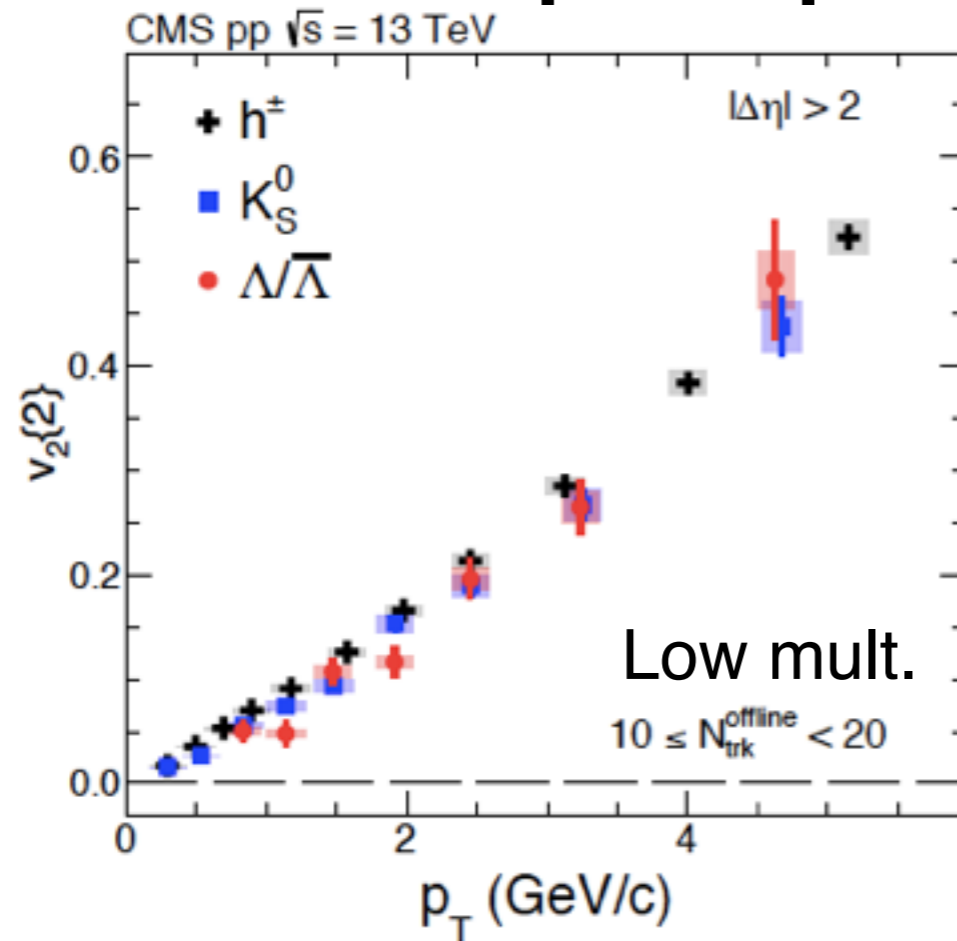


- ATLAS Template fit
 - Template function using low mult.
 - Assume $v_2 \neq 0$ in low mult.
 - No multiplicity dependence

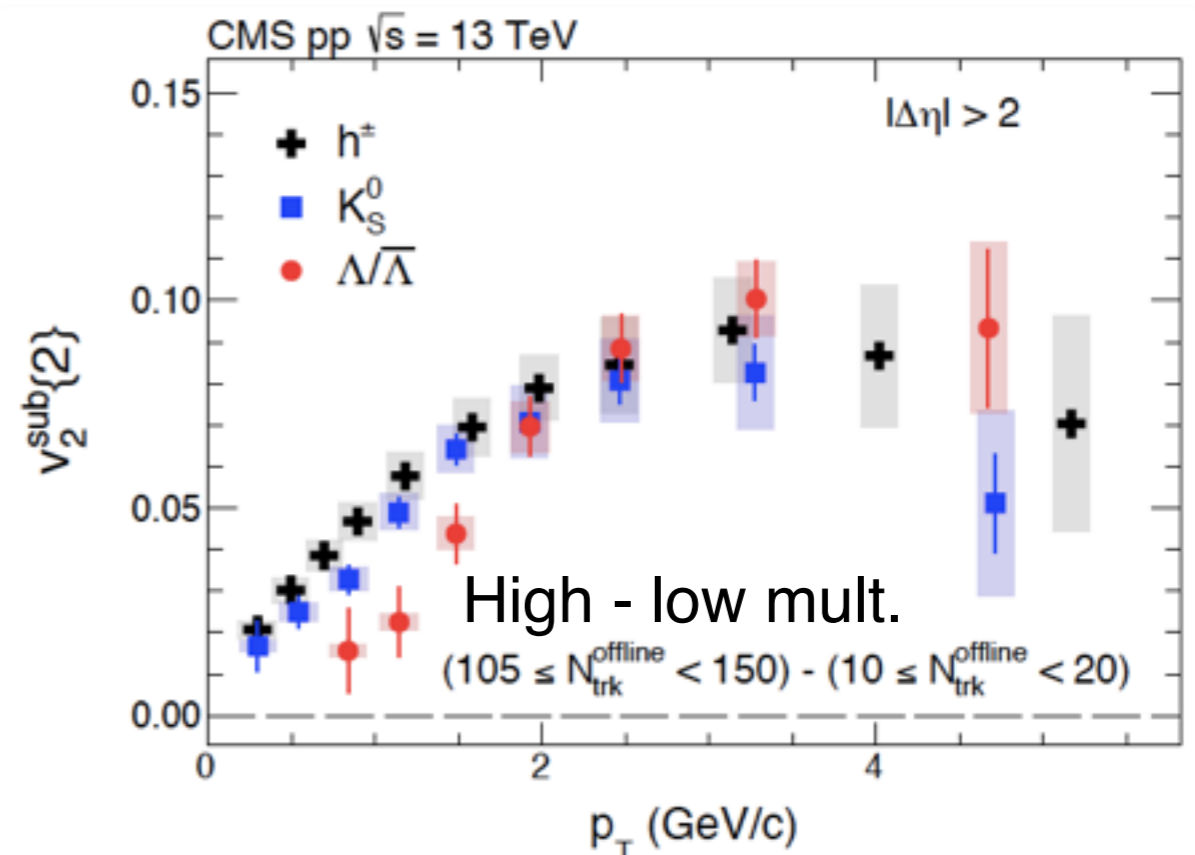
- CMS Low mult. subtraction method
 - Subtract low mult. from high mult.
 - Assume $v_2 = 0$ in low mult.
 - Strong multiplicity dependence

PID v_2 in p+p 13 TeV

CMS Zhenyu Chen



- $v_2\{2\}$ without subtraction
 - Non-flow is included
 - Low mult. does not show mass ordering
 - Mass ordering at high mult.
- $v_2\{2\}$ with subtraction
 - Suppress non-flow
 - Mass ordering is still seen



$c_2\{4\}$ in p+p 13 TeV (CMS)

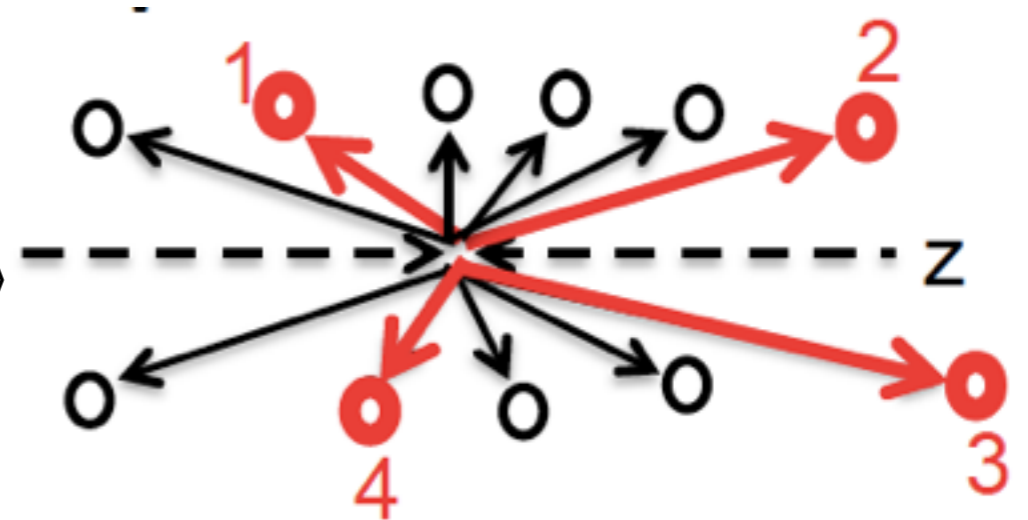
- Four particle correlation

$$c_n\{4\} = \frac{\langle\langle \cos[n(\phi_1 + \phi_2 - \phi_3 - \phi_4)] \rangle\rangle}{-2\langle\langle \cos[n(\phi_1 + \phi_2)] \rangle\rangle^2}$$

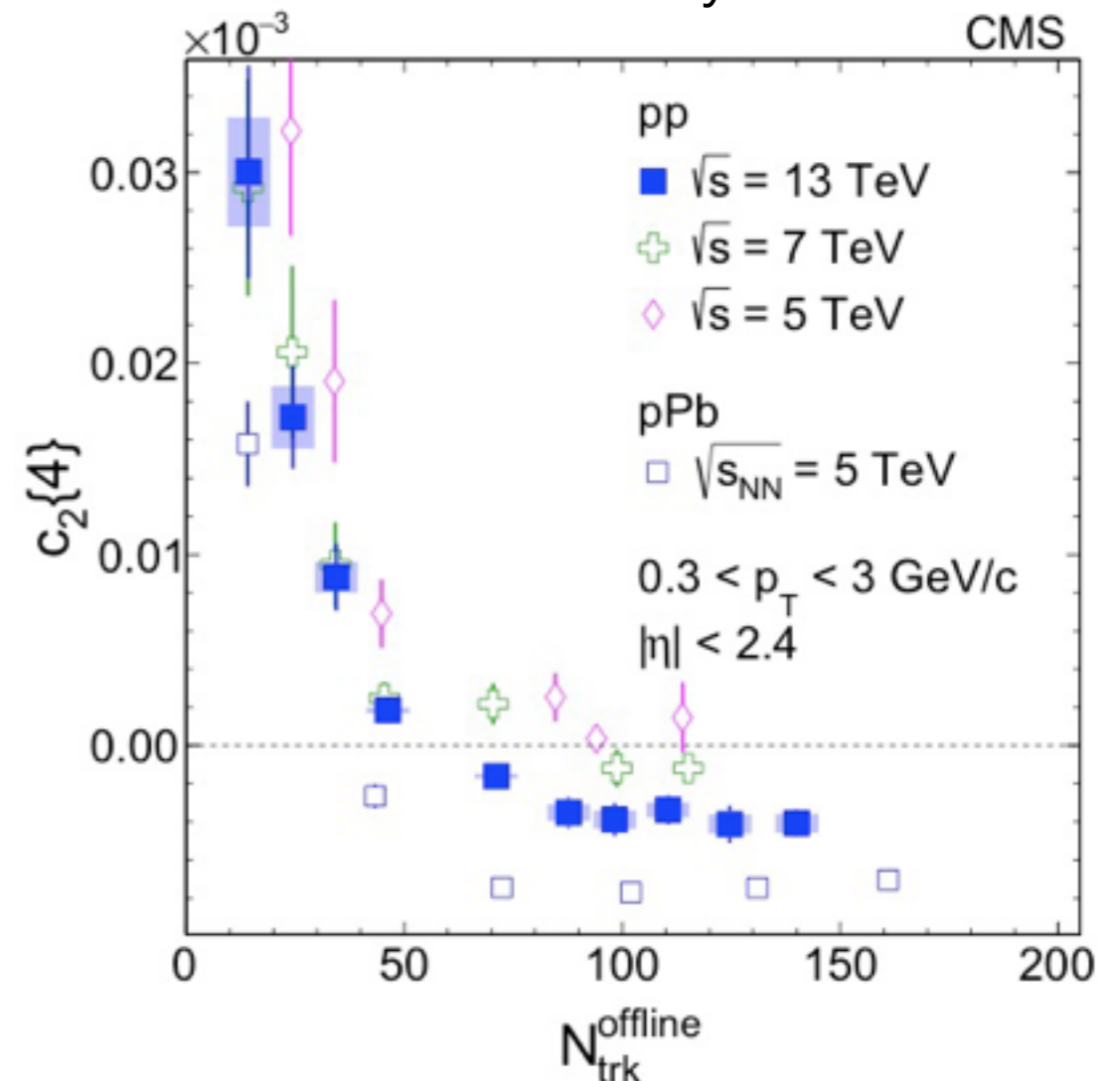
$$v_2\{4\} = \sqrt[4]{-c_n\{4\}}$$

- Negative $c_n\{4\} \rightarrow$ positive $v_n\{4\}$
- Suppress non-flow, fluctuation

- pp 13 TeV shows negative $c_2\{4\}$
 - Indicate positive v_2
 - Energy dependence
 - Collectivity ?

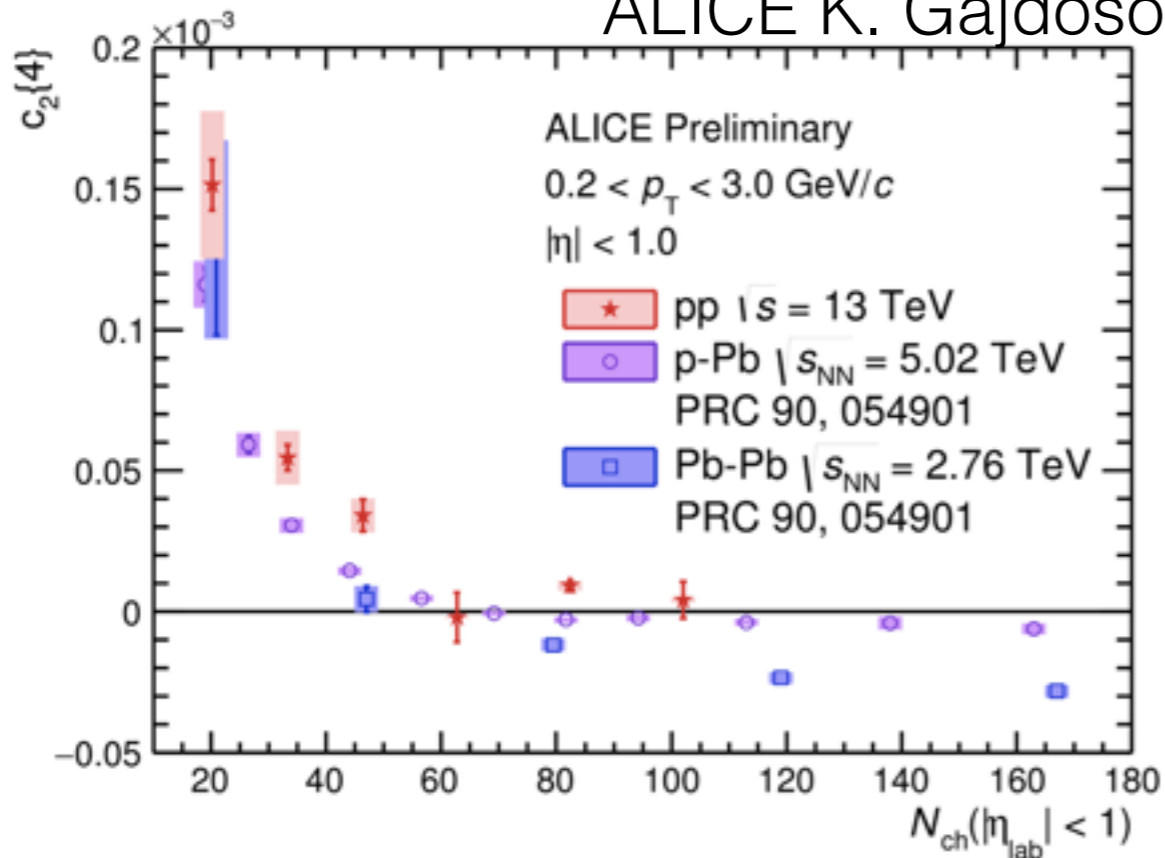


CMS Zhenyu Chen



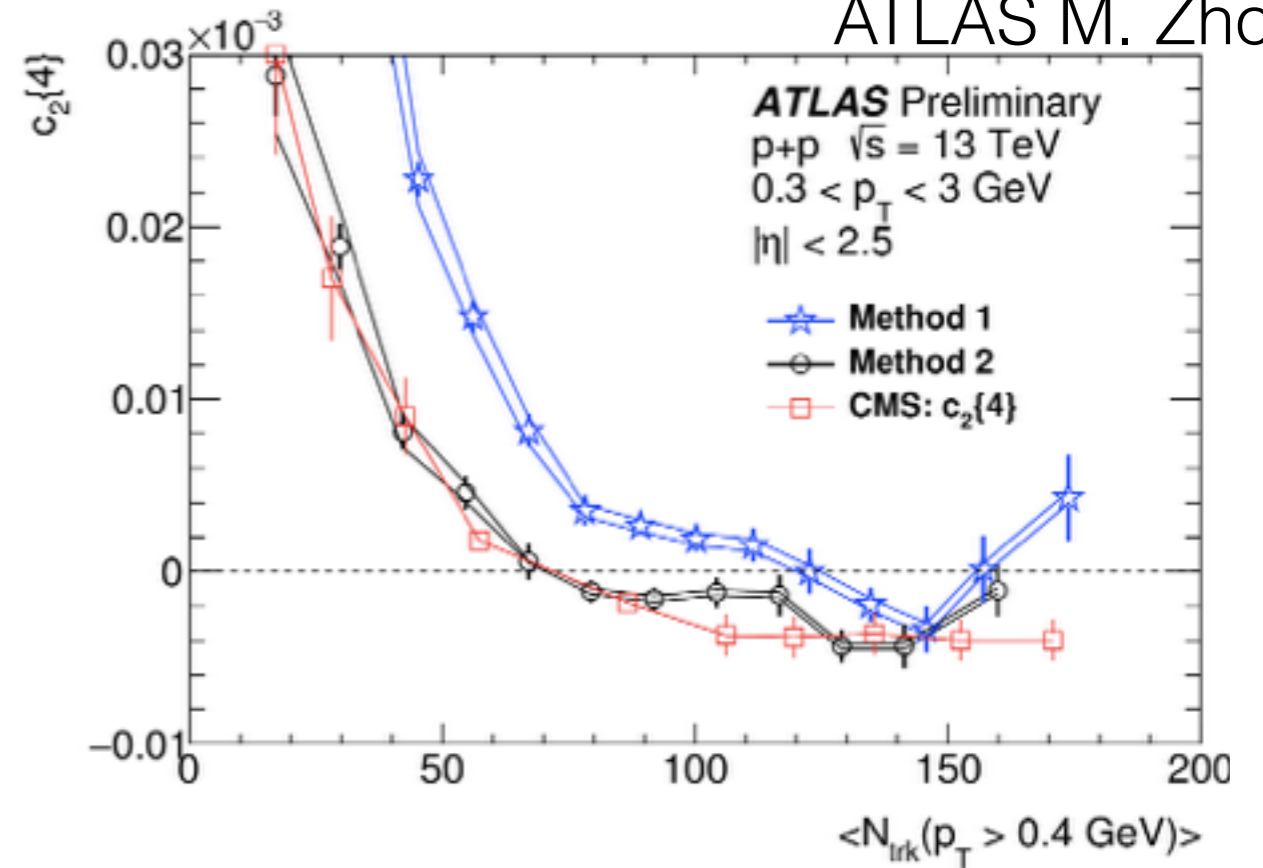
$c_2\{4\}$ in p+p 13 TeV (ALICE, ATLAS)

ALICE K. Gajdosova



Event classification with $0.2 < p_T < 3.0$ GeV

ATLAS M. Zhou



Method1: Event classification with $0.3 < p_T < 3.0$ GeV

Method2: Event classification with $p_T > 0.4$ GeV (=CMS)

- ALICE/ATLAS (Method1)

- $c_2\{4\}$ and event classification with same p_T range

- $c_2\{4\}$ shows no negative sign

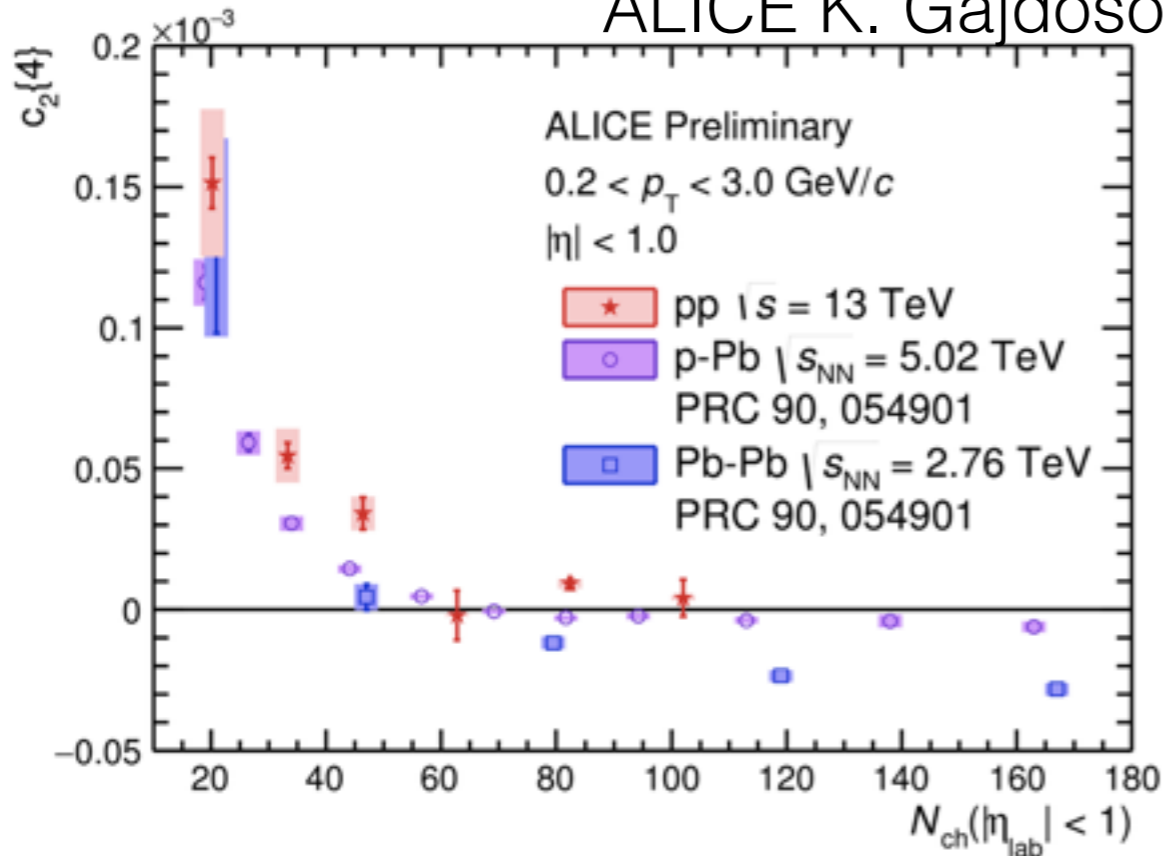
- ATLAS (Method2)

- $c_2\{4\}$ shows negative sign, consistent with CMS result

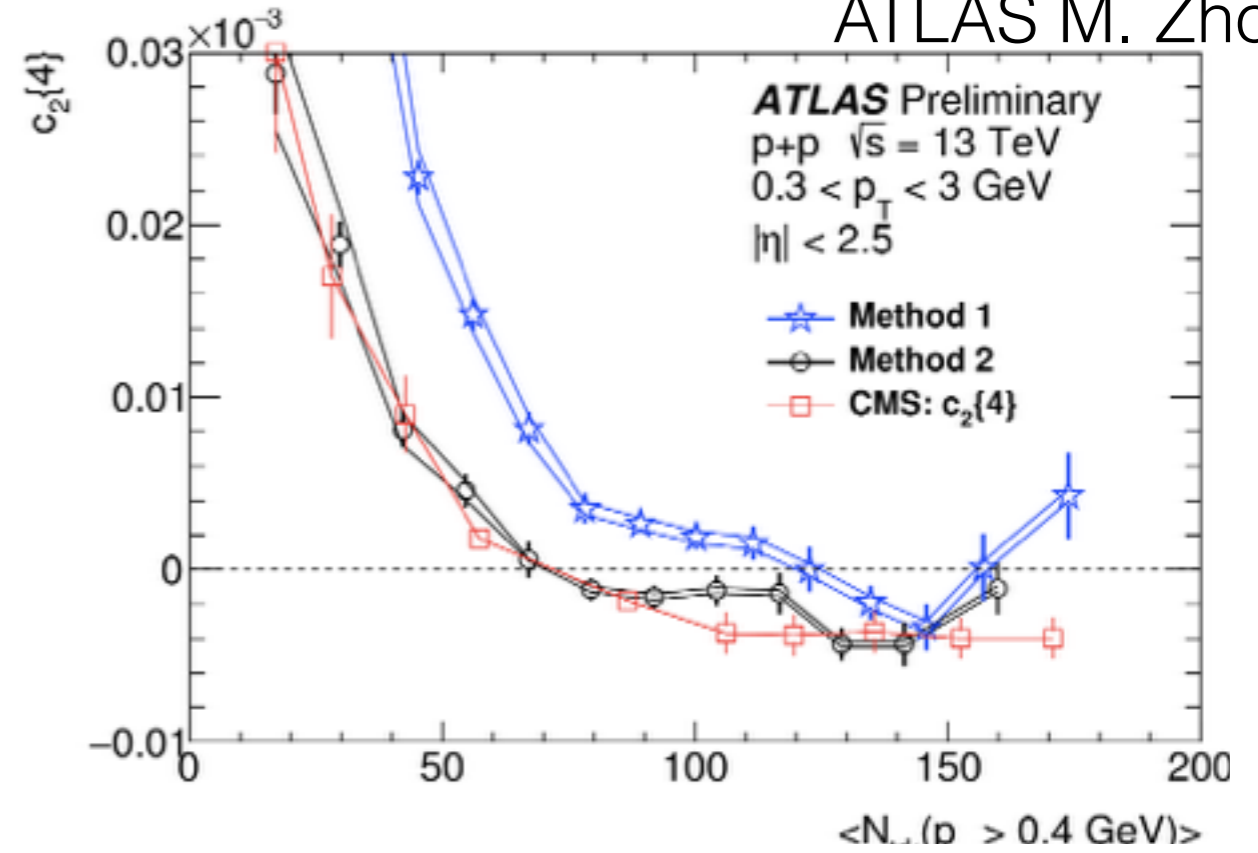
- $c_2\{4\}$ depends on event classification (multiplicity fluctuation)

$c_2\{4\}$ in p+p 13 TeV (ALICE, ATLAS)

ALICE K. Gajdosova



ATLAS M. Zhou



Event classification with $0.2 < p_T < 3.0$ GeV

Method1: Eve
 Method2: Eve

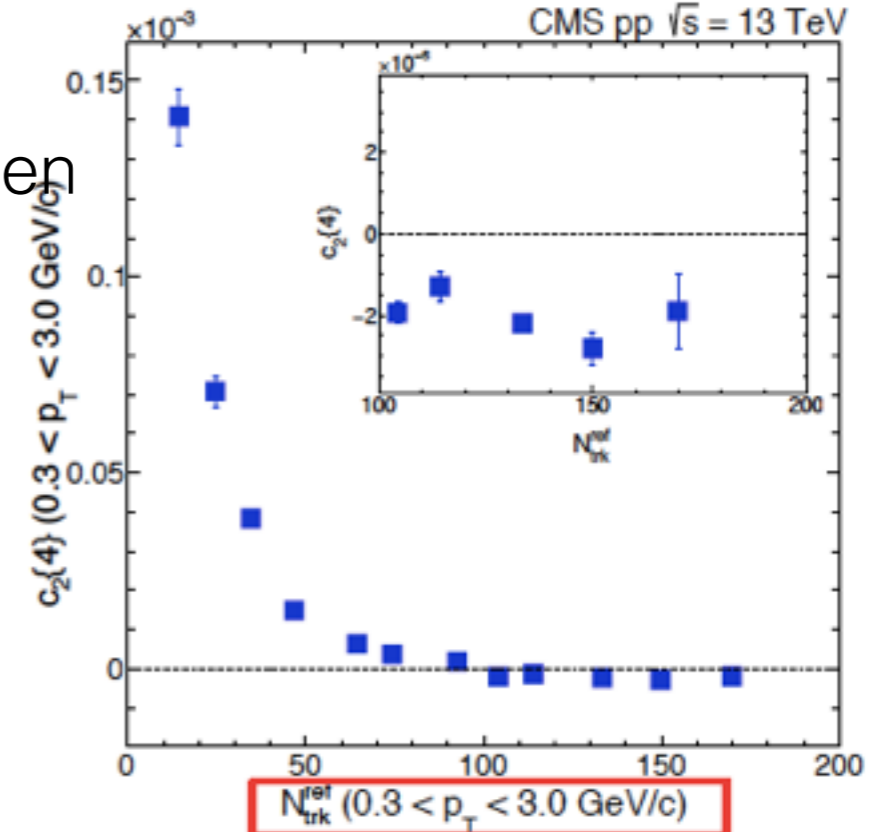
CMS Zhenyu Chen

- CMS

- $c_2\{4\}$ and event classification with same p_T range

- $c_2\{4\}$ shows negative sign

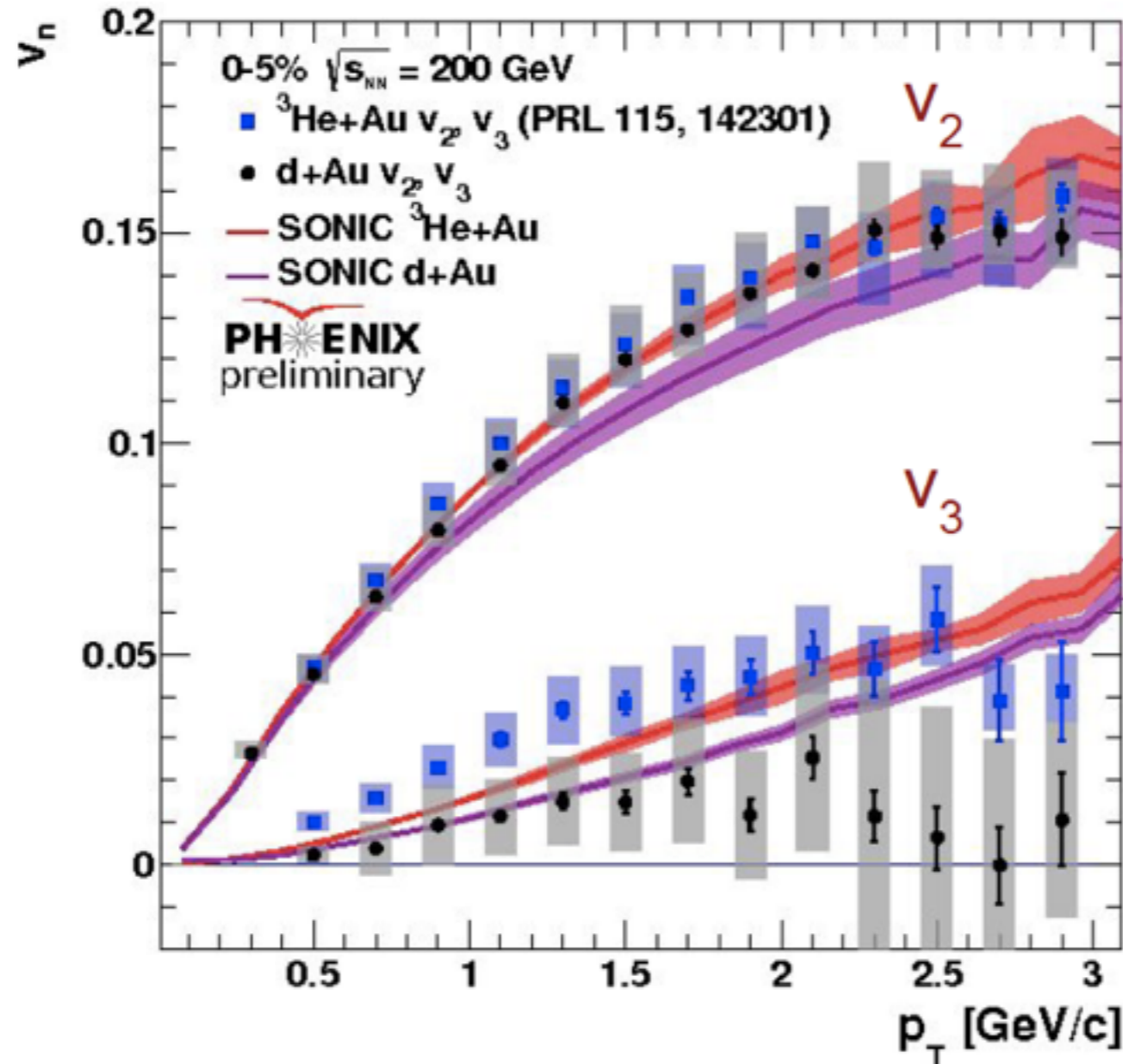
- CMS does not agree with ATLAS (Method1)/ALICE



3)

d+Au v_3

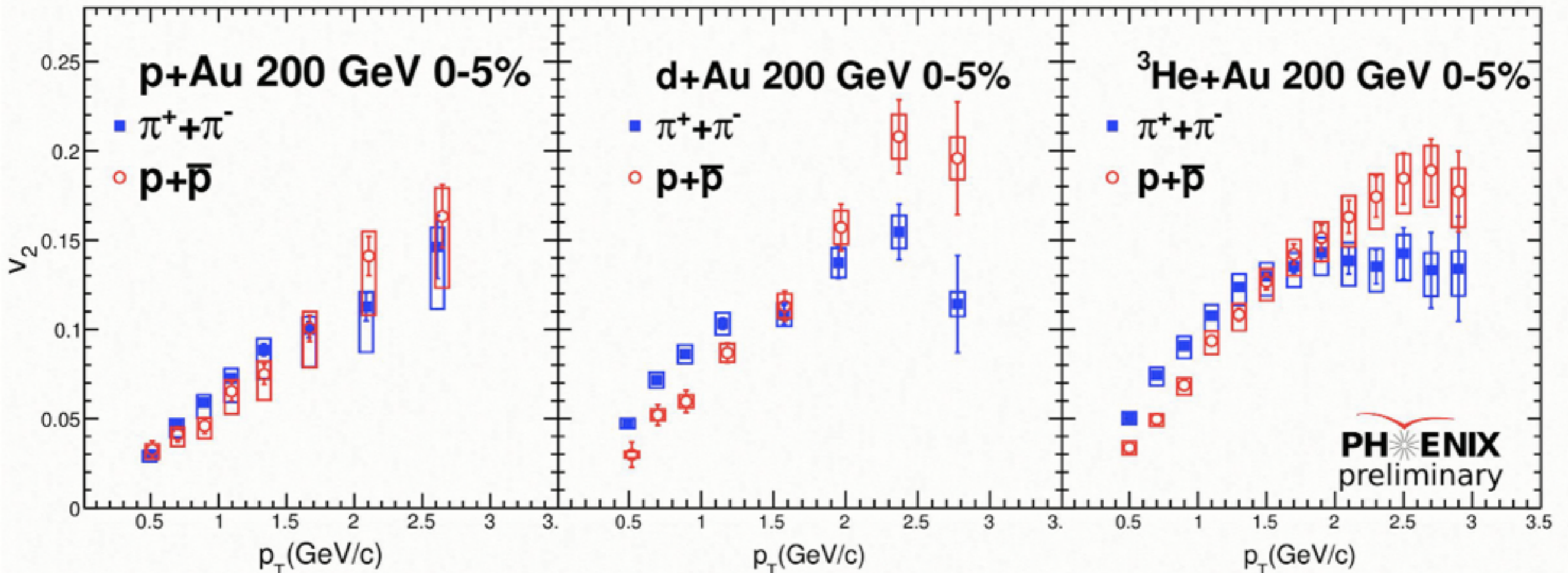
PHENIX Q. Xu



- v_3 in d+Au is observed
 - Event plane method
- Hydrodynamics reproduces ordering of v_3
 - v_3 ($^3\text{He+Au}$) $>$ v_3 (d+Au)

PID v_2 in p/d/ ^3He +Au

PHENIX Q. Xu



- Charged π and p v_2 in p/d/ ^3He +Au is observed
 - Event plane method
- Mass-ordering feature is seen
 - Less pronounced in p+Au

d+Au BES: v_2 vs p_T

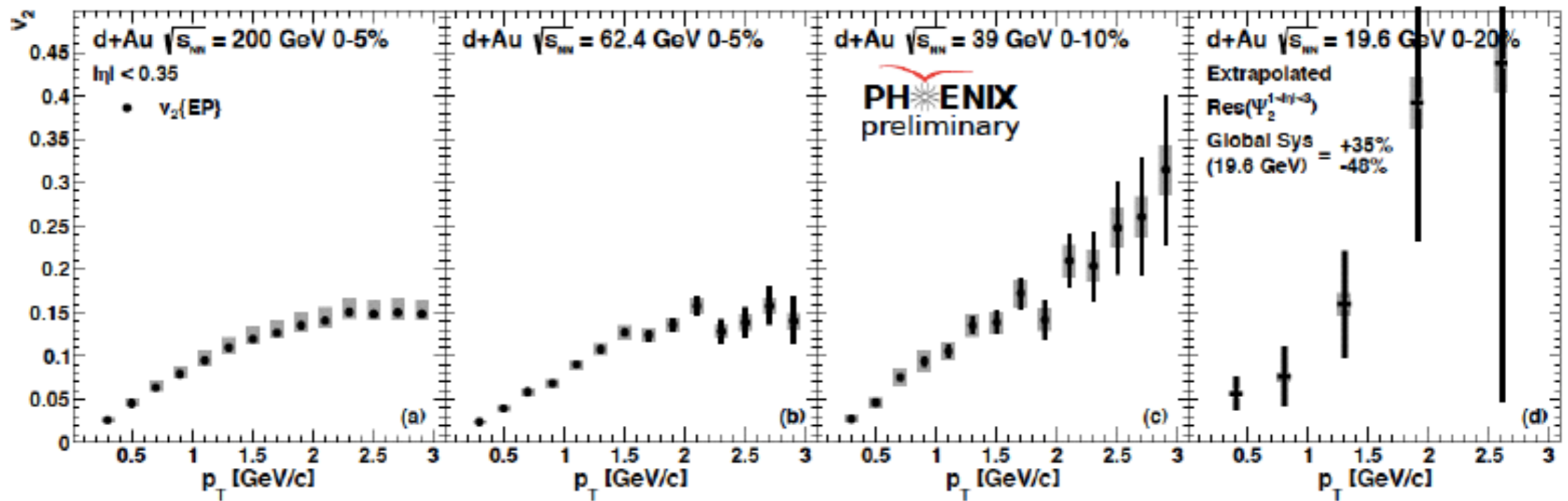
PHENIX J. Velkovska

200 GeV

62 GeV

39 GeV

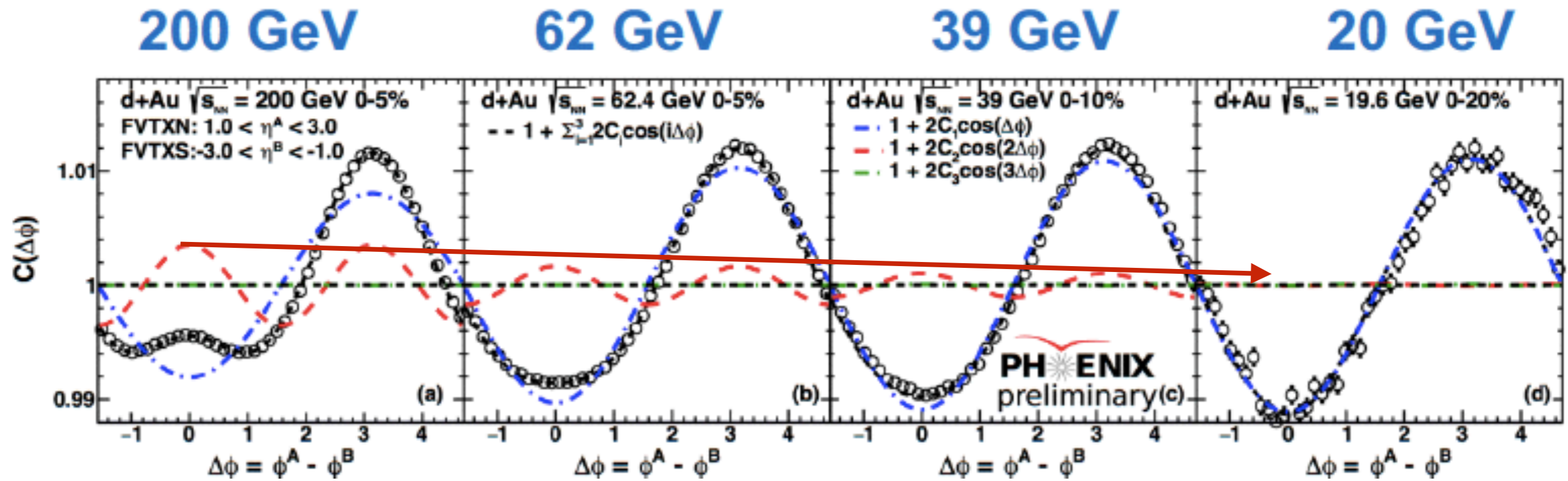
20 GeV



- v_2 at 200 and 62 GeV shows a similar p_T dependence
- v_2 at 39 and 20 GeV increase at high p_T
 - Non flow ?

d+Au BES: Ridge

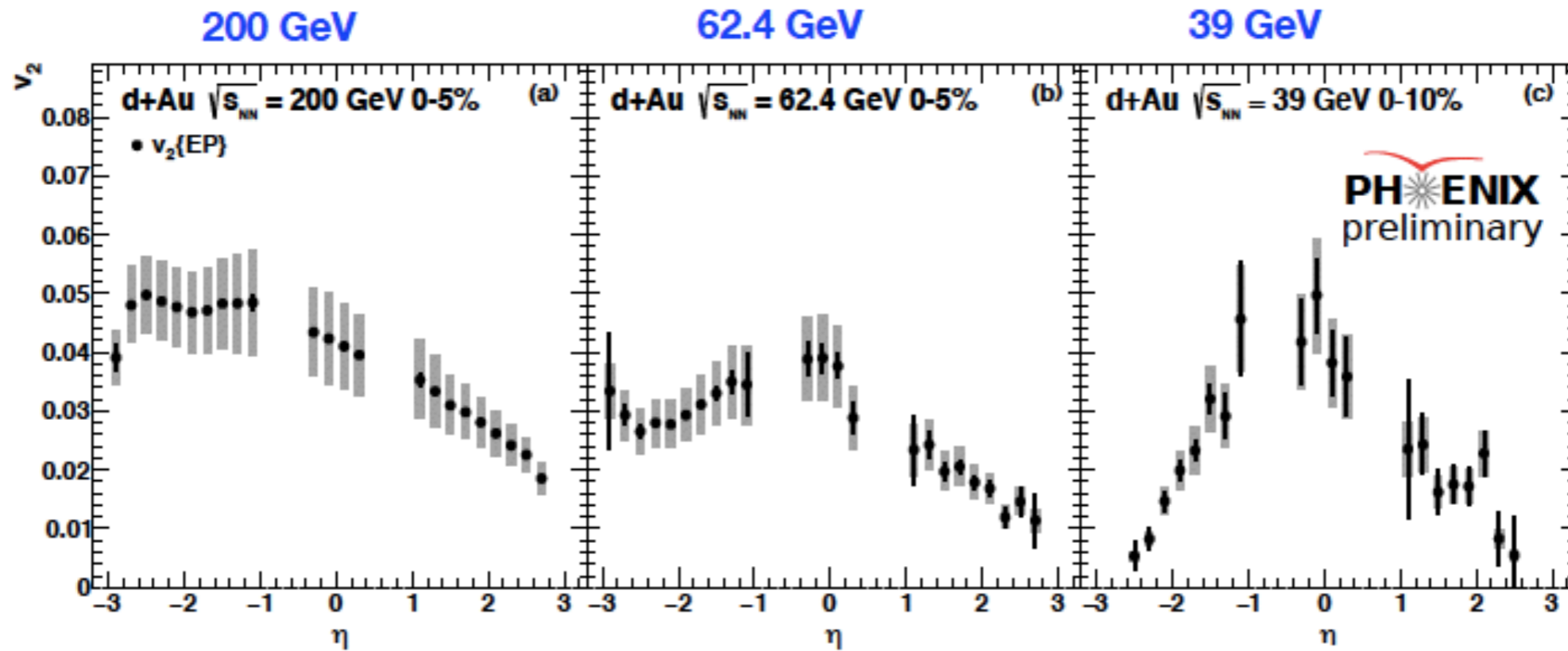
PHENIX J. Velkovska



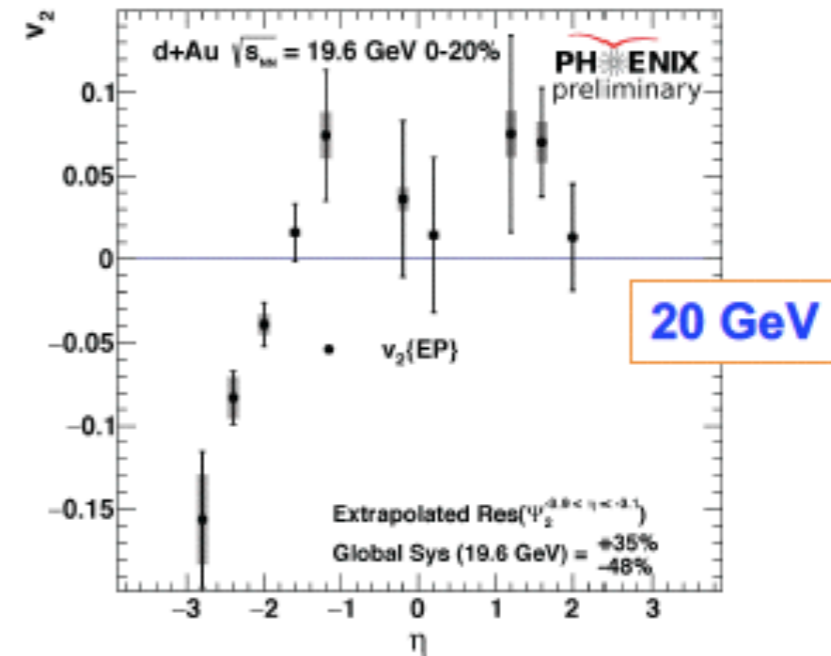
- Long range correlation is observed in d+Au BES
 - $p_T > 0$, $|\Delta\eta| > 2$, charged hadrons (Forward vertex detector)
- Elliptic component decreases with decreasing energy

d+Au BES: v_2 vs η

Velkovska



- Forward: similar values at all $\sqrt{s_{NN}}$
- Backward: decrease with $\sqrt{s_{NN}}$
 -Au-going side v_2 drastically changed below 39 GeV



Julia Velkovska, QM 2017

Event plane de-correlation

ATLAS M.Soumya
P. Huo



$$R_{n,n|n,n} = \frac{\langle q_n(-\eta_{ref})q_n(-\eta)q_n^*(+\eta)q_n^*(+\eta_{ref}) \rangle}{\langle q_n(-\eta_{ref})q_n^*(-\eta)q_n(+\eta)q_n^*(+\eta_{ref}) \rangle}$$

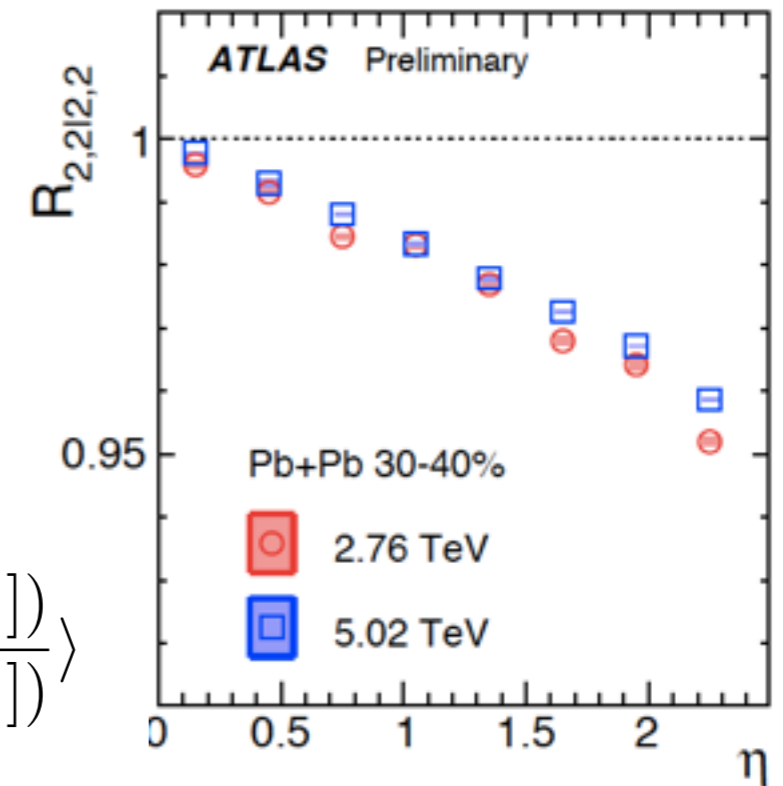
$$\sim \left\langle \frac{\cos(n[\Psi_n(-\eta_{ref}) - \Psi_n(\eta_{ref}) + (\Psi_n(-\eta) - \Psi_n(\eta))])}{\cos(n[\Psi_n(-\eta_{ref}) - \Psi_n(\eta_{ref}) - (\Psi_n(-\eta) - \Psi_n(\eta))])} \right\rangle$$

$$R_{n,n|n,n} = 1 : \eta \text{ independent } \Psi_n$$

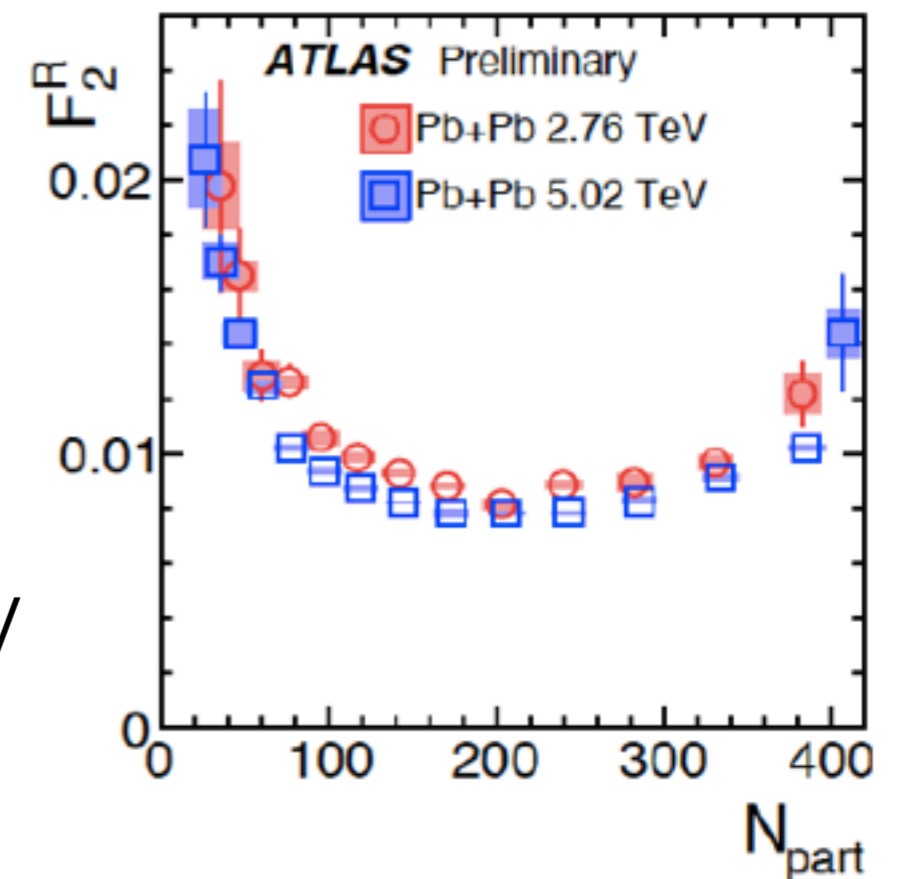
$$\Psi_n(-\eta_{ref}) = \Psi_n(\eta) = \Psi_n(-\eta) = \Psi_n(\eta_{ref})$$

$$R_{n,n|n,n} < 1 : \eta \text{ dependent } \Psi_n$$

- De-correlation increasing linearly with increasing η gap
- De-correlation is smaller at lower energy
- De-correlation is smallest at mid-central



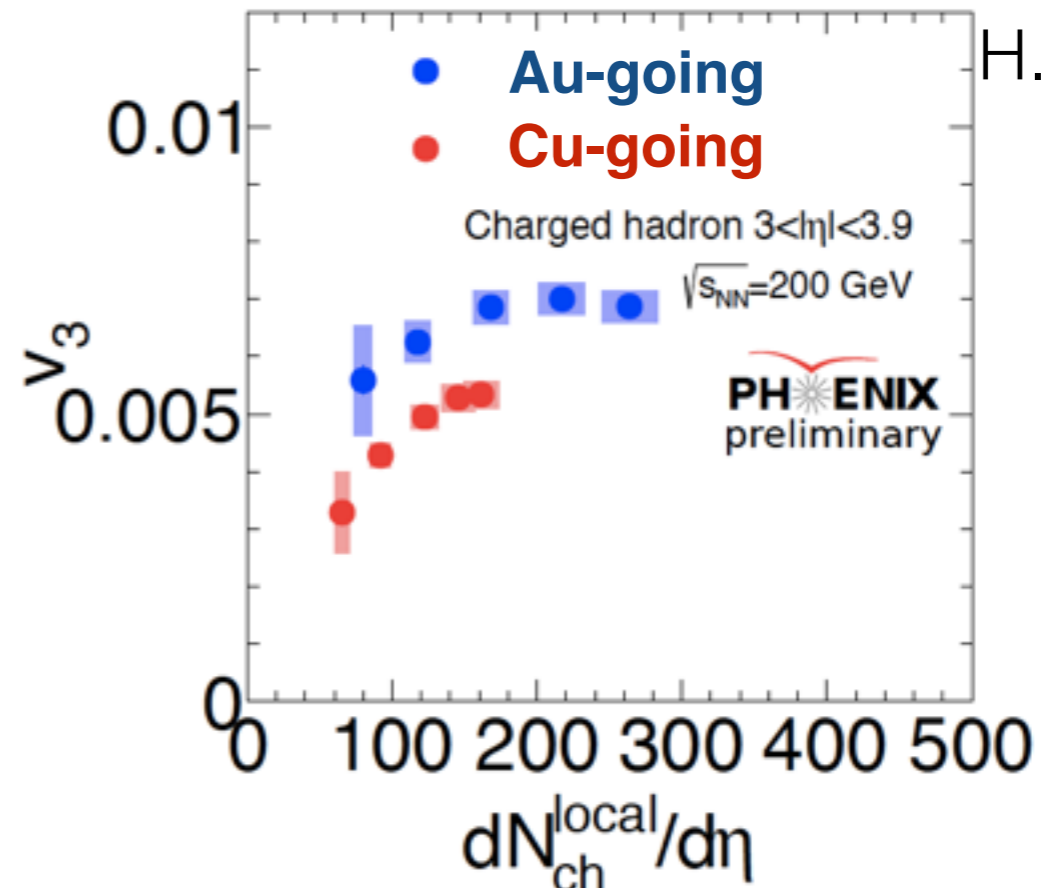
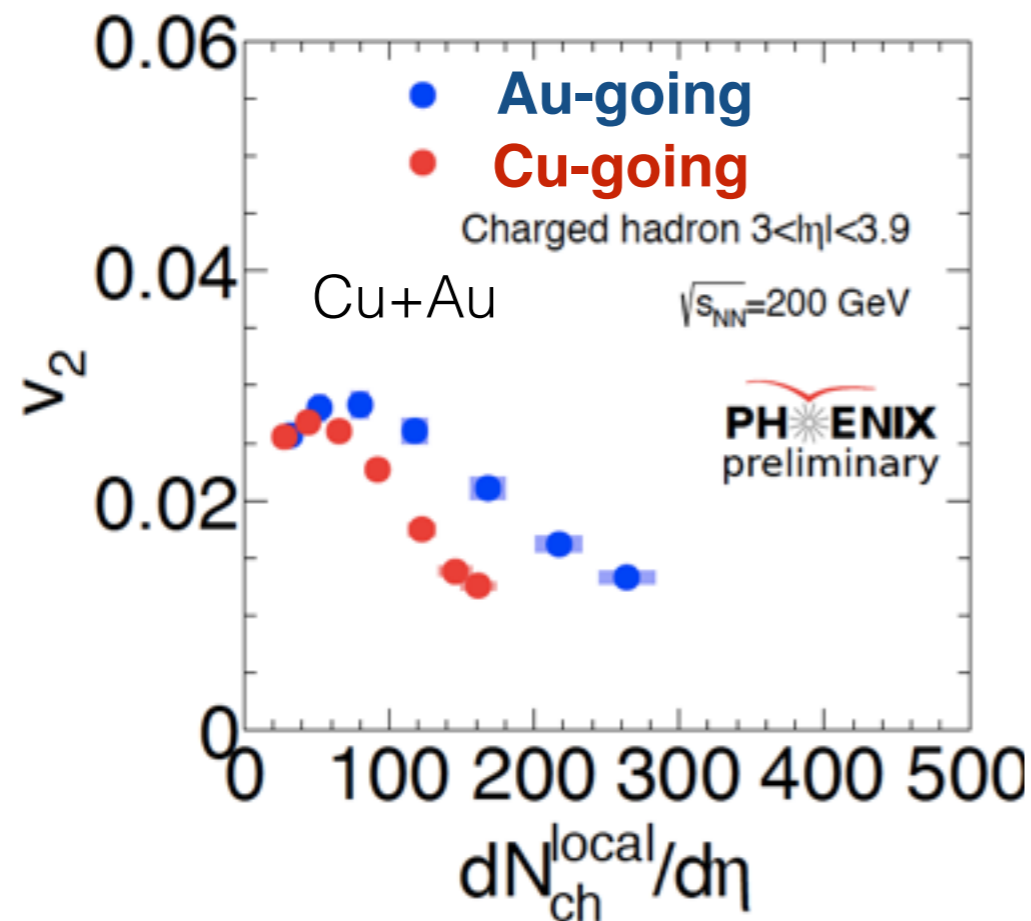
$$R_{n,n|n,n} \approx 1 - 4F_{n;2}^{TWL} \eta$$



Forward/Backward asymmetry of v_n

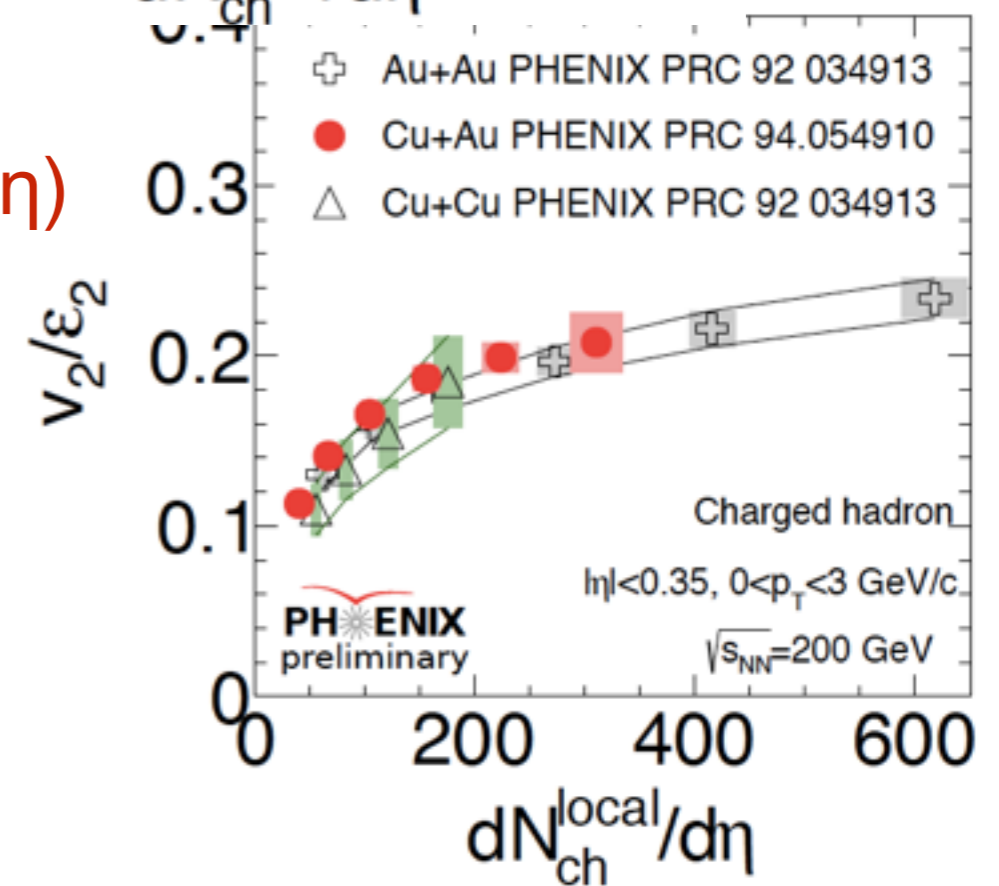
PHENIX M. Shimomura

H. Nakagomi



- F/B v_n plotted as a function of F/B $dN_{ch}/d\eta$
 - **Au-going $v_n(dN_{ch}/d\eta) > \text{Cu-going } v_n(dN_{ch}/d\eta)$**
 - $\epsilon_{n,Au\text{-going}} \neq \epsilon_{n,Cu\text{-going}} ?$

- Empirical relation among v_2 , ϵ_2 and $dN/d\eta$ at mid- η
 - $v_2/\epsilon_2 \propto f(dN/d\eta)$
 - Study of eccentricity



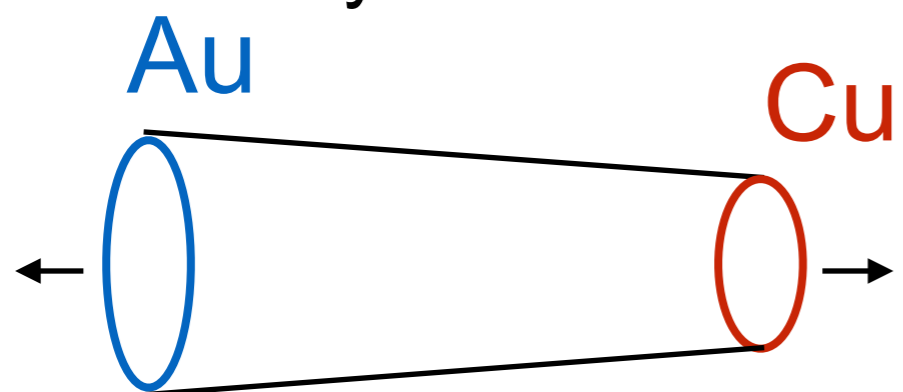
V_n/ϵ_n : Asymmetric initial eccentricity

PHENIX M. Shimomura

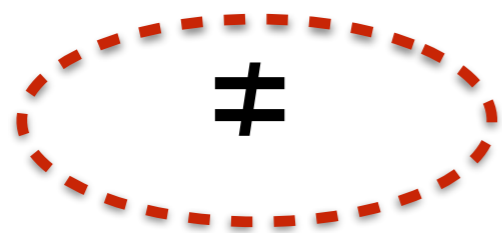
H. Nakagomi

Initial eccentricity

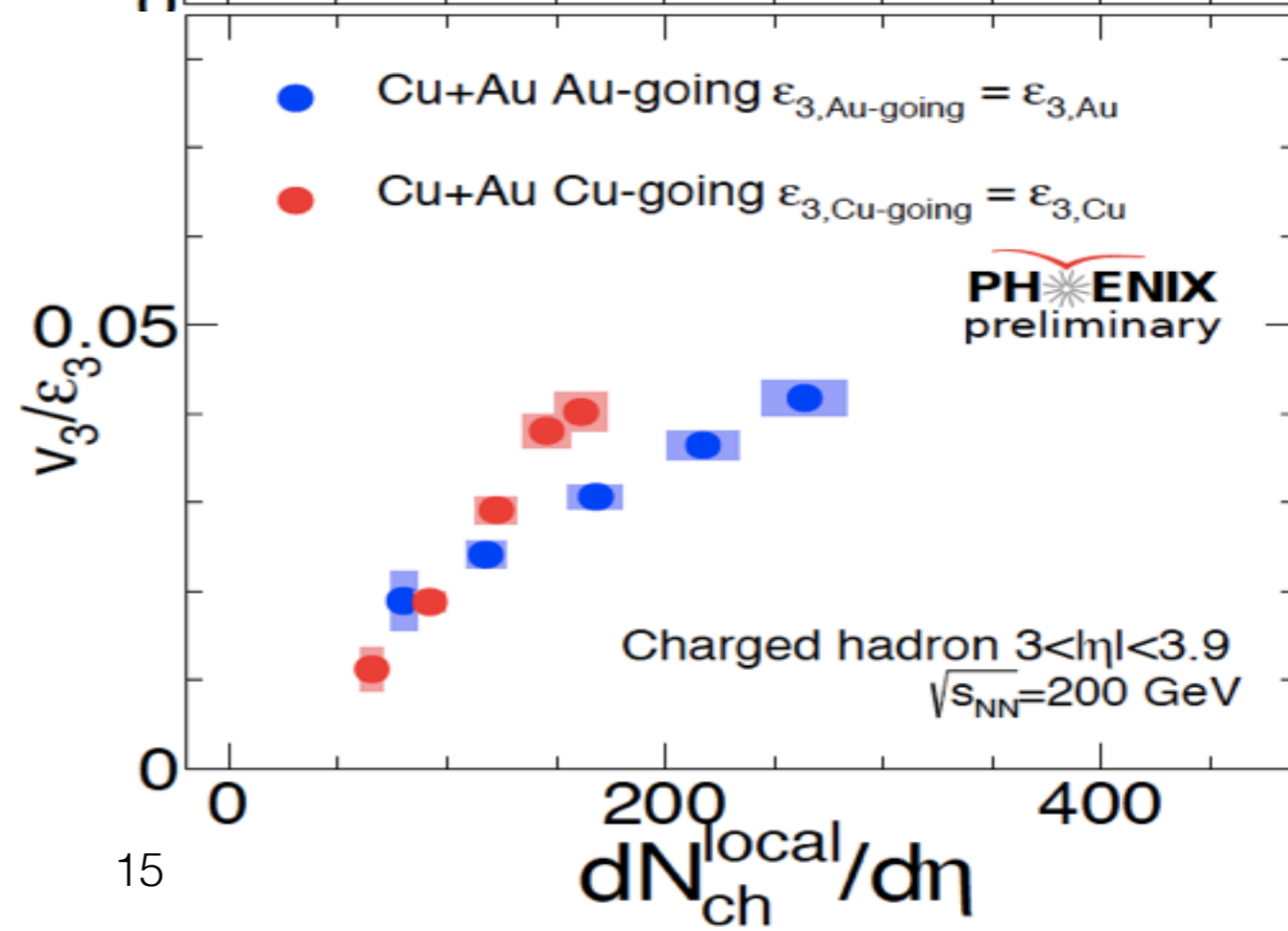
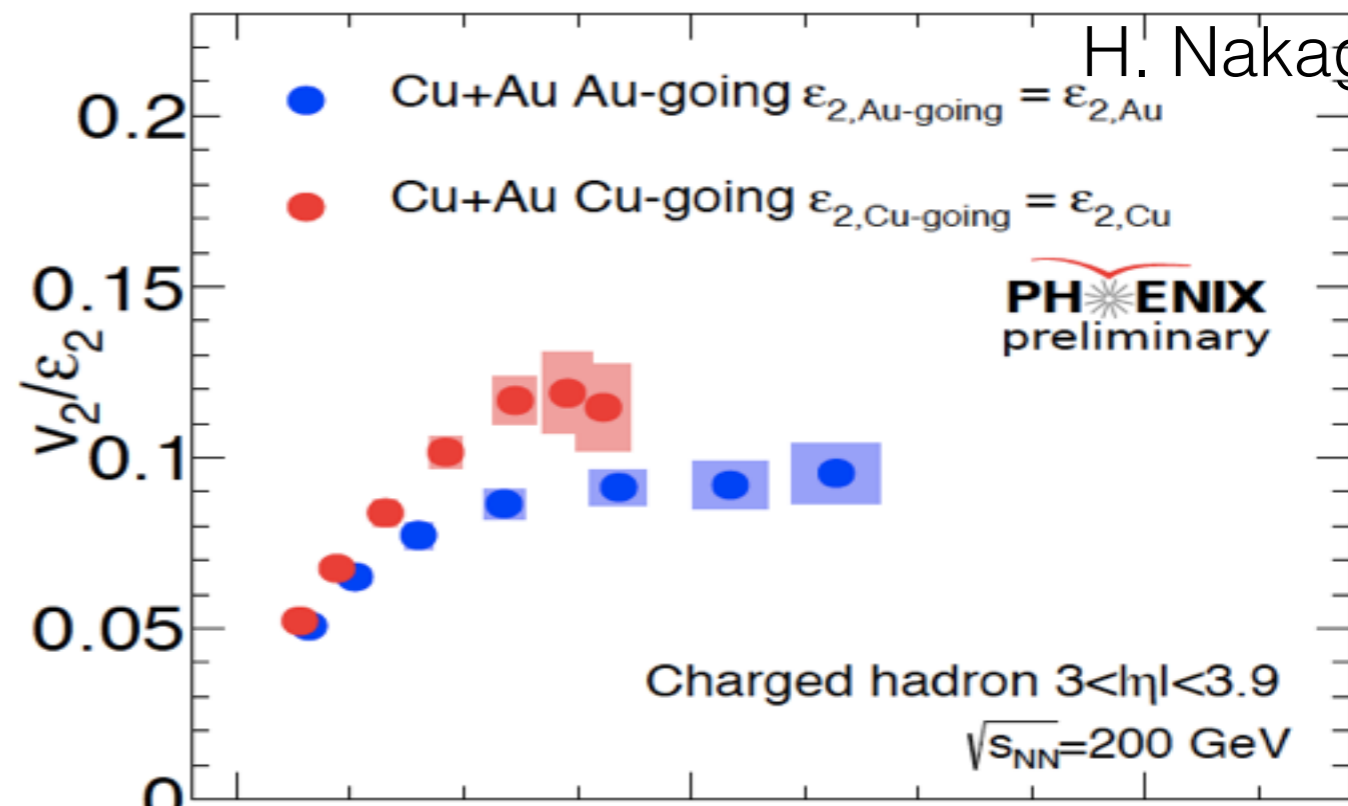
Asymmetric



$$V_n, \text{ Au-going} / \epsilon_{n, \text{ Au}}$$



$$V_n, \text{ Cu-going} / \epsilon_{n, \text{ Cu}}$$

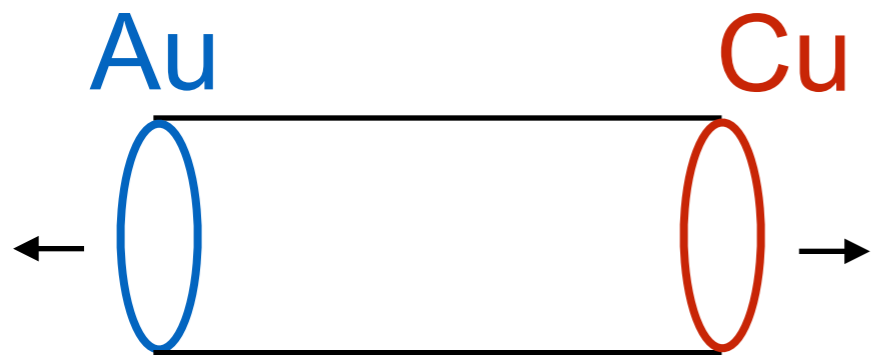


V_n/ϵ_n : Symmetric initial eccentricity

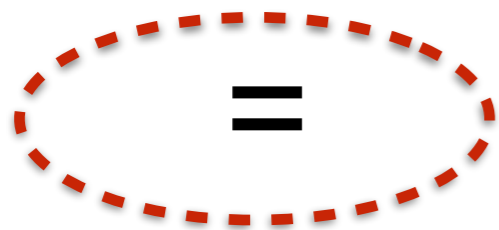
PHENIX M. Shimomura

H. Nakagomi

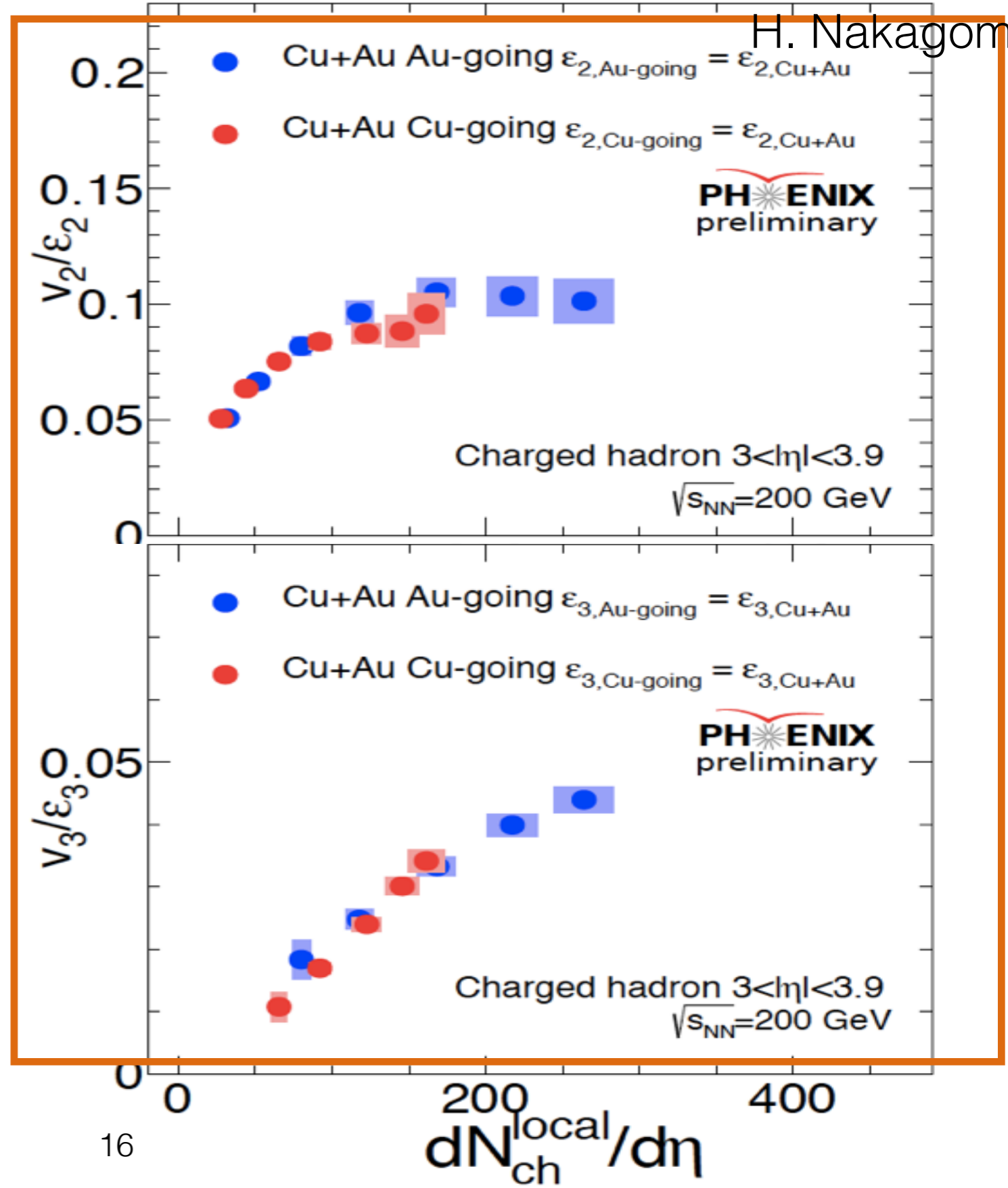
Initial eccentricity
Symmetric



$$V_n, \text{ Au-going} / \epsilon_n, \text{ Cu+Au}$$

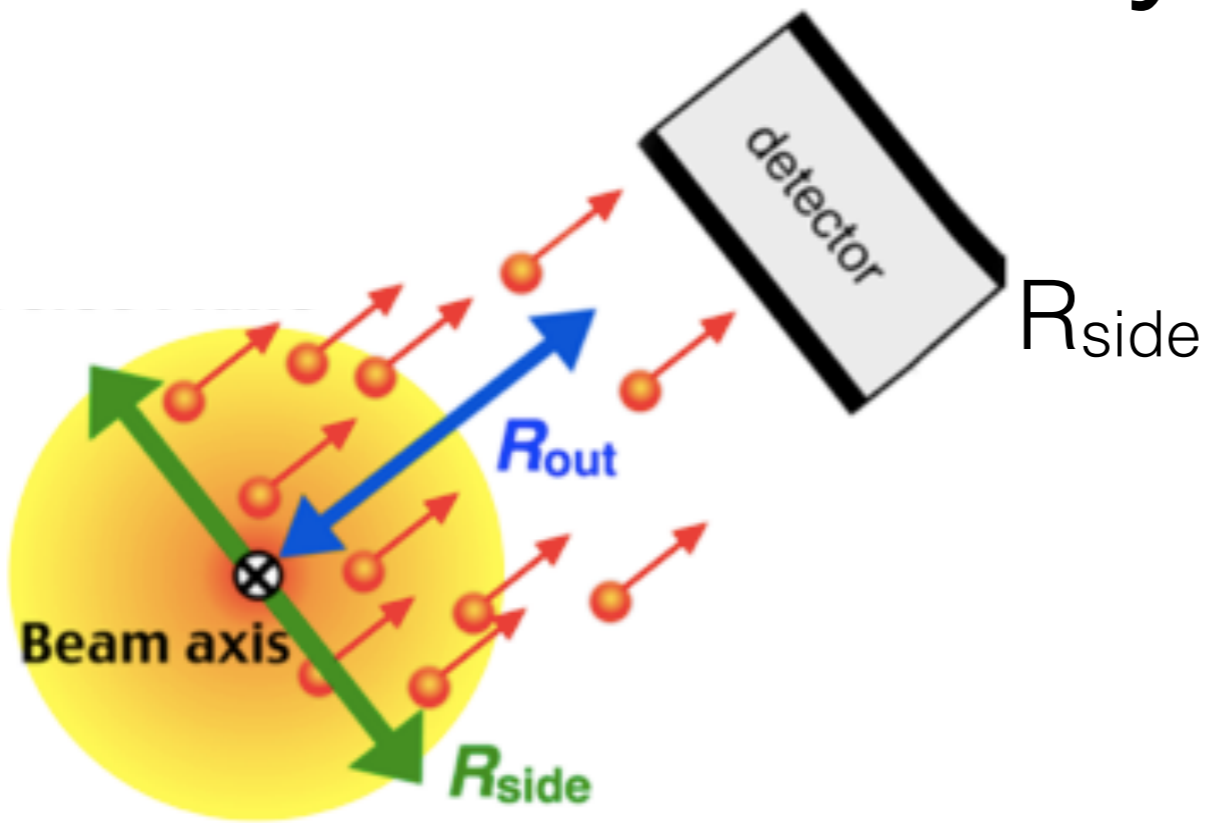


$$V_n, \text{ Cu-going} / \epsilon_n, \text{ Cu+Au}$$

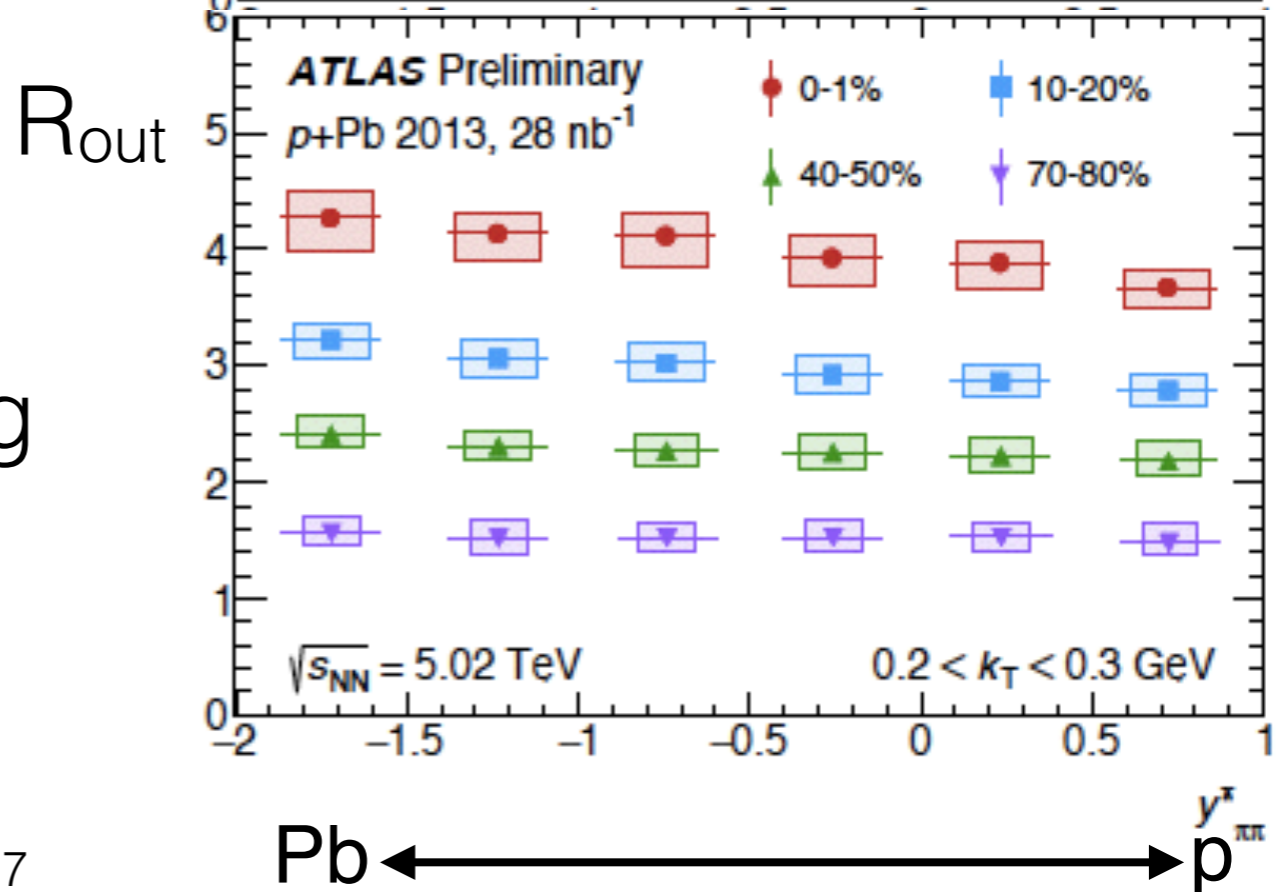
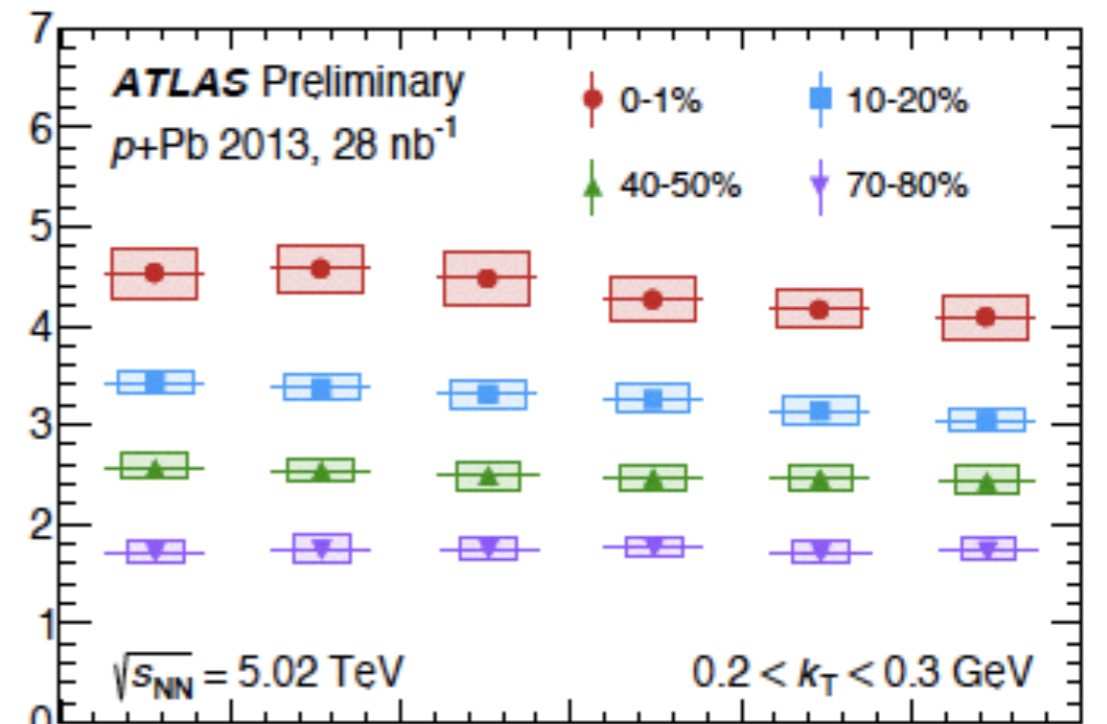
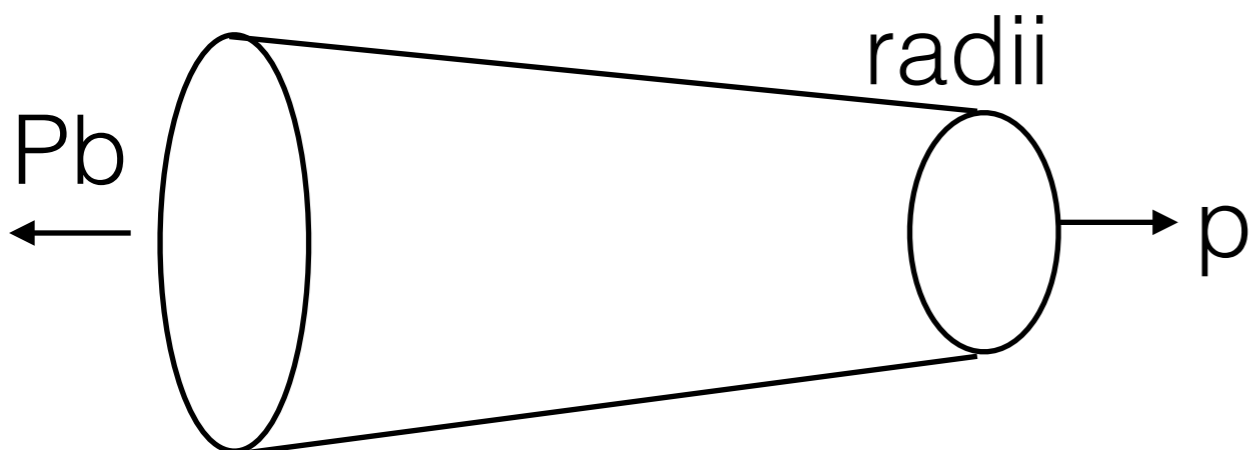


p+Pb HBT radii vs y (rapidity of pion pair)

ATLAS M. Clark



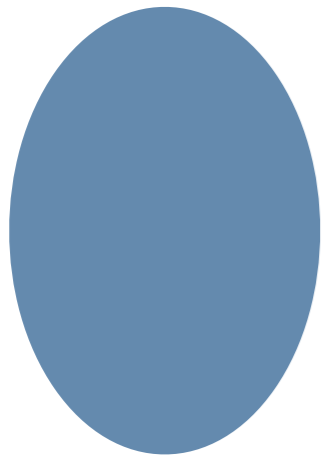
- $y' = y - 0.465$
-Center of momentum frame
- Central: Pb-going > p-going
- Peripheral : Pb-going ~ p-going



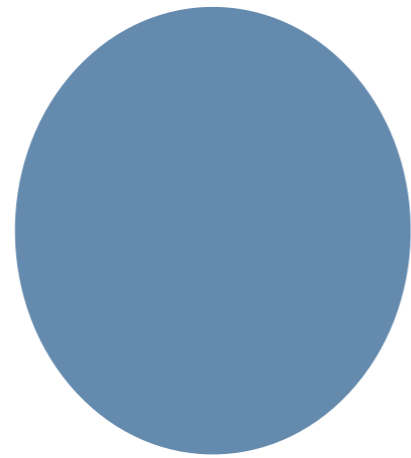
HBT w.r.t Ψ_n in Pb+Pb with event shape engineering

✓ Event shape engineering

- Select larger flow vector $Q_n \propto v_n$



Large Q_2 :20%



Average Q_2

- Large q_2 selection

- 20% larger v_2

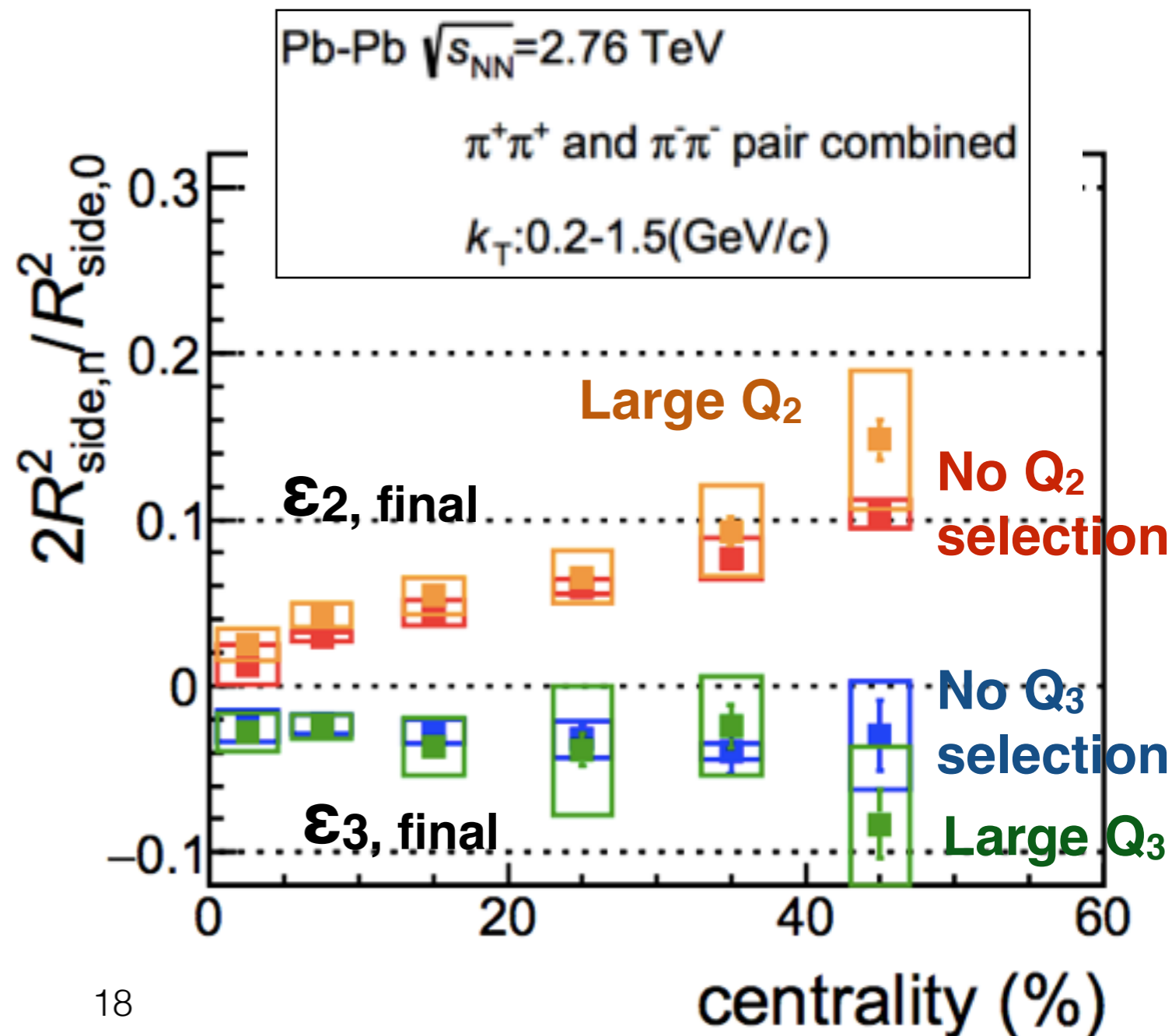
- slightly enhance final eccentricity

- Large q_3 selection

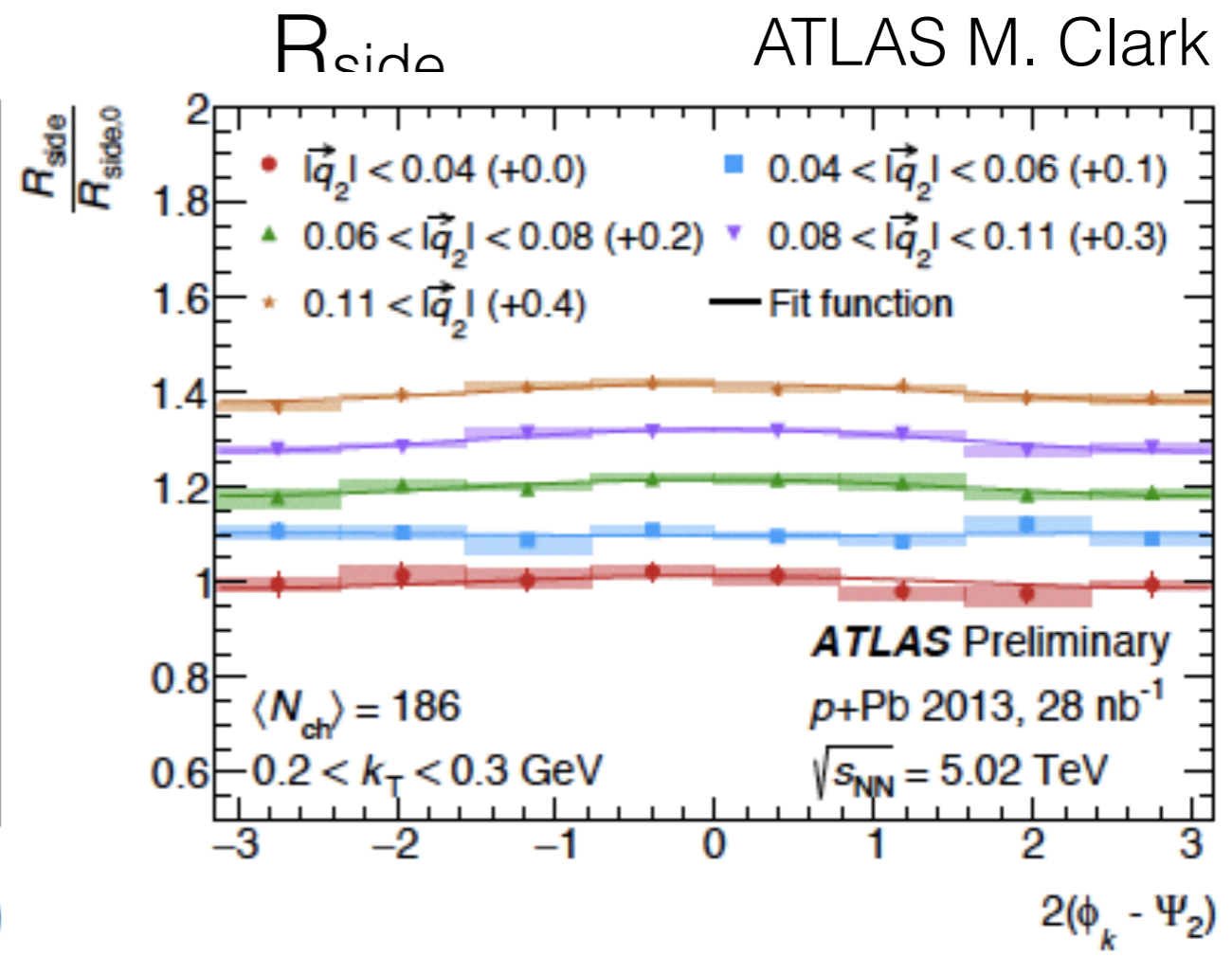
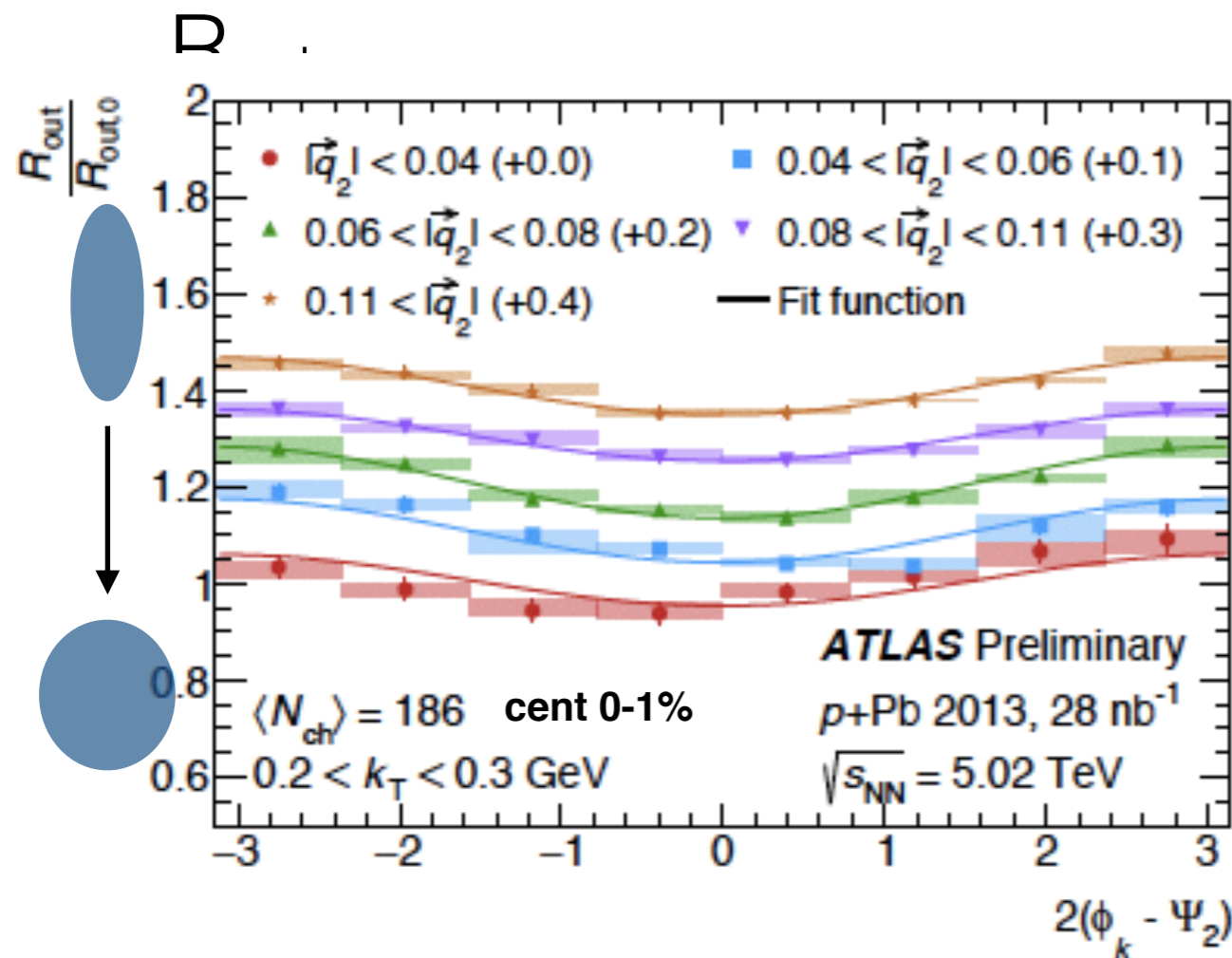
- 15% larger v_3

- Final eccentricity does not change

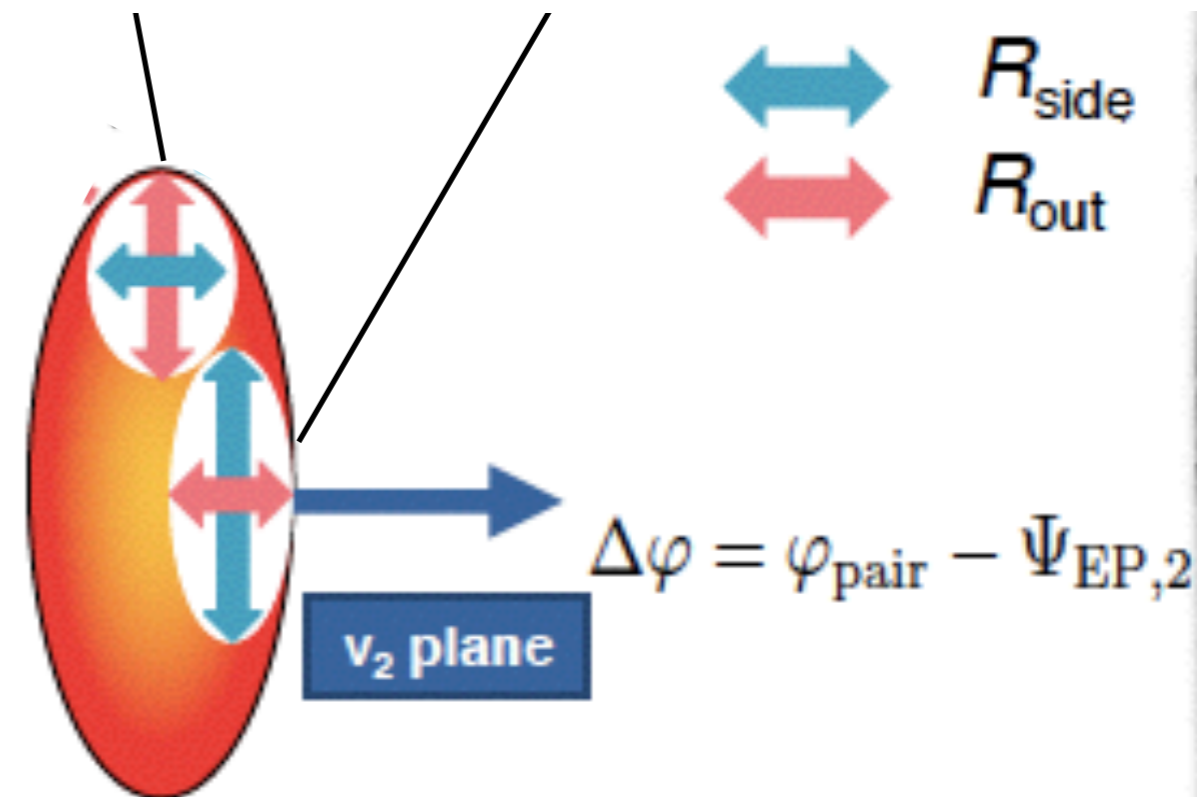
ALICE M. Saleh & N. Tanaka



HBT w.r.t Ψ_2 in p+Pb with event shape engineering



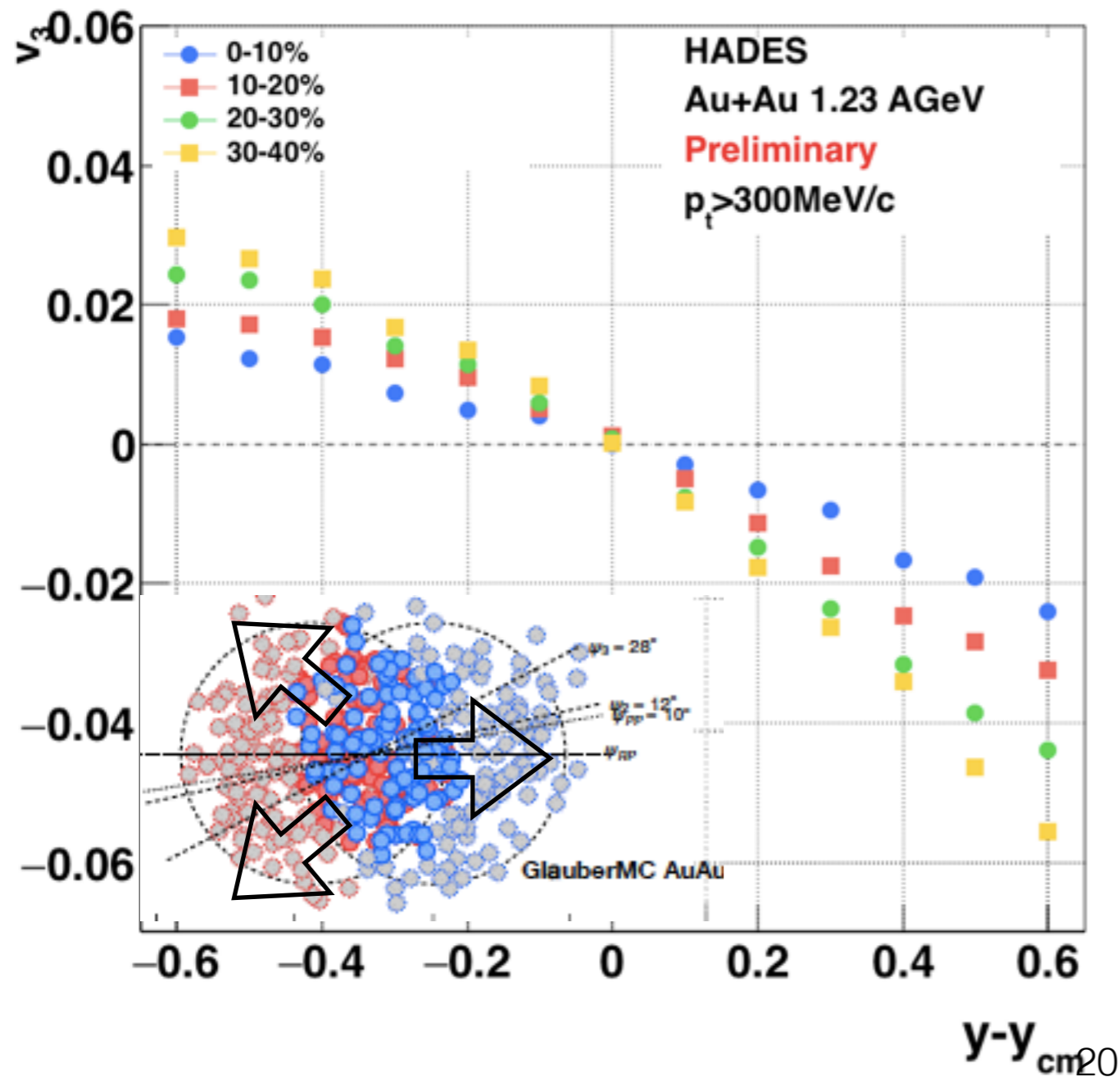
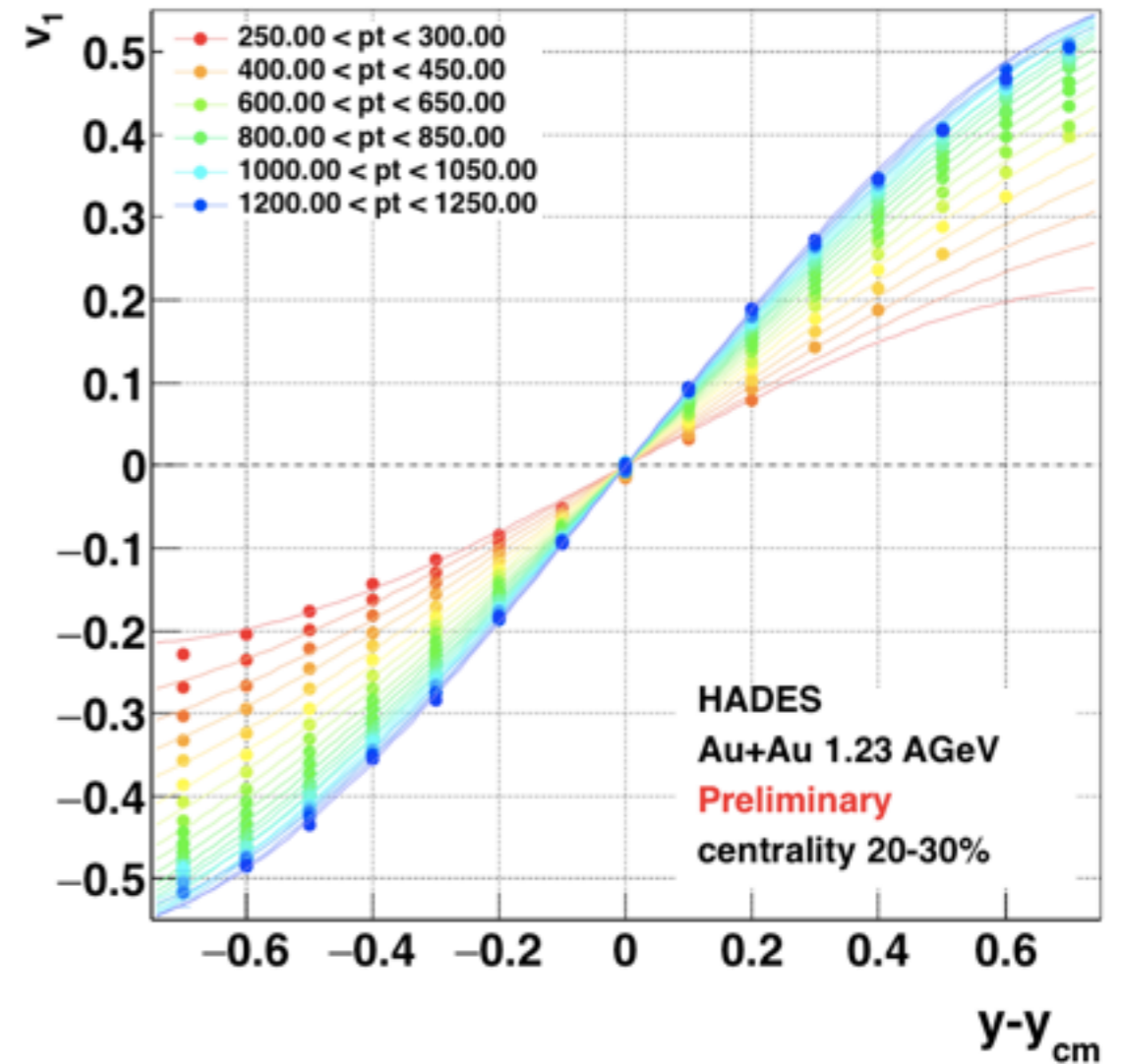
- R_{out} : Smaller in-plane size
- R_{side} : Larger in-plane size
- Same sign of modulation as seen in A+A
- Does not show strong dependence of Q selection



Proton v_3 w.r.t $\Psi_{1,\text{spec}}$ in Au+Au at 1.23 AGeV

HADES Behruz Kardan

- Proton v_1 w.r.t spectator Ψ_1
 - Forward : same direction as Ψ_1
 - Backward: opposite direction as Ψ_1



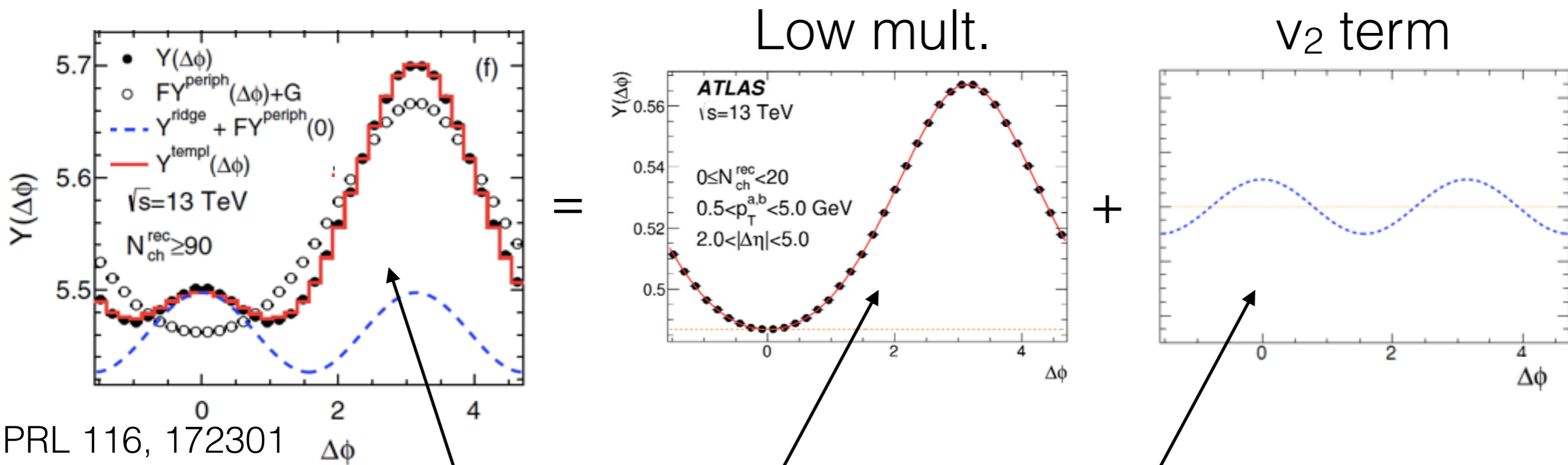
- Proton v_3 w.r.t spectator Ψ_1
 - Never observed at collider energy
 - Forward: opposite direction as Ψ_1
 - Backward: same direction as Ψ_1

Summary

- pp 13TeV at LHC
 - v_2 : ATLAS/CMS show different multiplicity dependence
 - v_2 : mass ordering is observed as seen in A+A
 - $c_2\{4\}$: Inconsistency between ATLAS/ALICE and CMS
- p/d/ ^3He +Au at RHIC
 - mass ordering is less pronounced in p+Au
 - d+Au BES p_T and η dependence is changed between 39 and 62.4
- Longitudinal direction
 - η dependent EP
 - Initial geometry is almost η independent
 - HBT radii is η dependent
- Event shape engineering
 - PbPb: Unlike $\epsilon_{2,Final}$, $\epsilon_{3,Final}$ is less sensitive
 - pPb: HBT radii w.r.t Ψ_2 , same oscillation as seen PbPb
- Low energy (Fixed target HADES)
 - v_3 w.r.t Ψ_1 is new observable at BES?

Template fit method (ATLAS)

- Extract flow component (v_2) via template function



$$Y^{\text{templ}}(\Delta\phi) = F \left[Y^{\text{periph}}(\Delta\phi) \right] + \left[Y^{\text{ridge}}(\Delta\phi) \right]$$

$$Y^{\text{periph}}(\Delta\phi) = Y^{\text{hard}}(\Delta\phi) + G_0 \left[1 + 2 v_{2,2}^0 \cos(2\Delta\phi) \right]$$

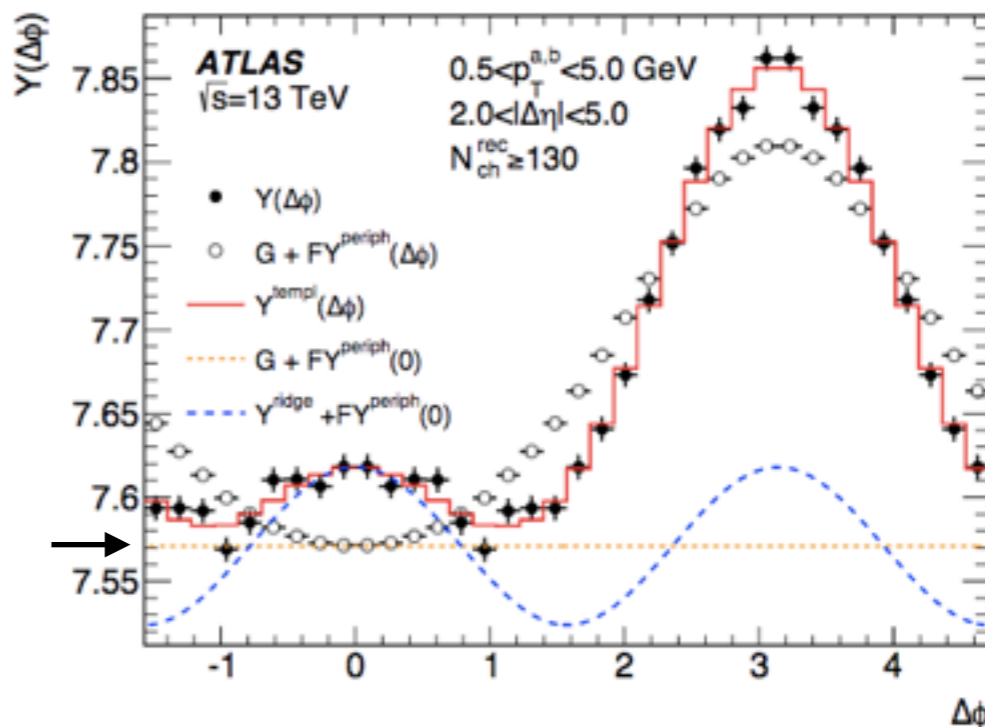
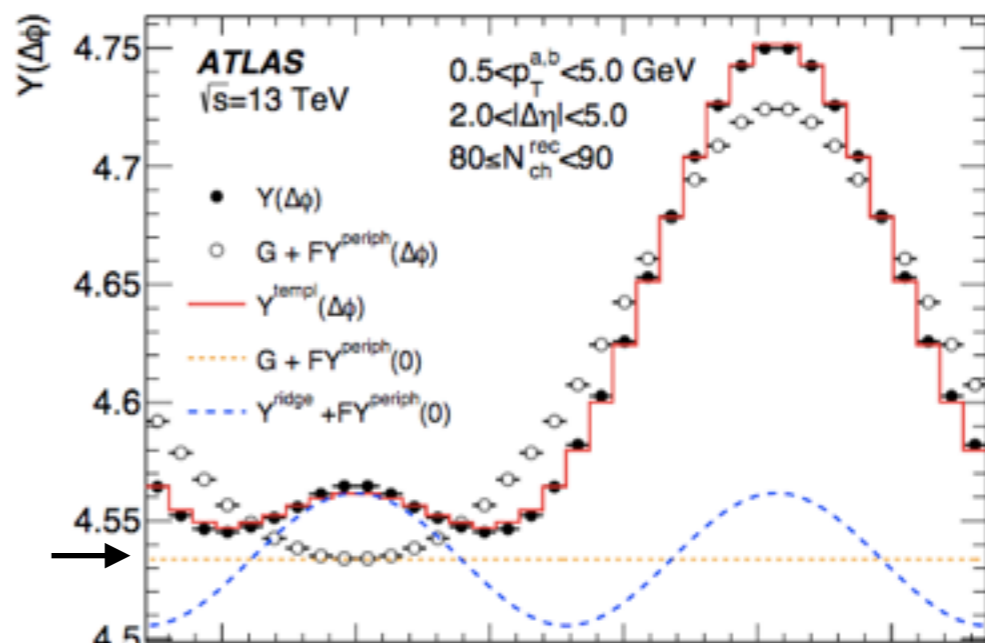
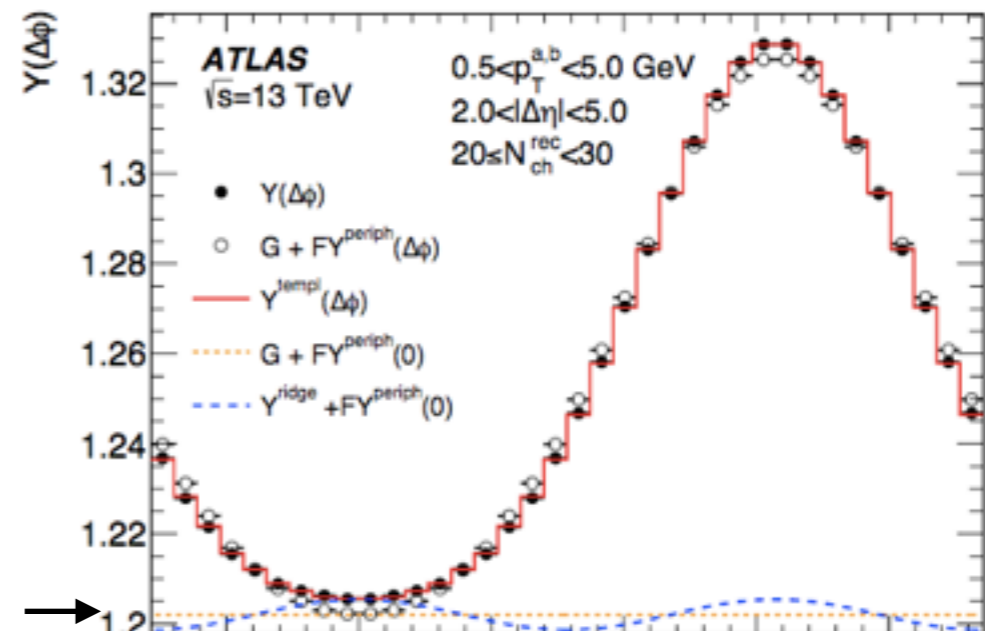
$$Y^{\text{ridge}}(\Delta\phi) = G \left[1 + 2 v_{2,2} \cos(2\Delta\phi) \right]$$

Ridge yield

- $v_{2,2}$ depends on baseline G

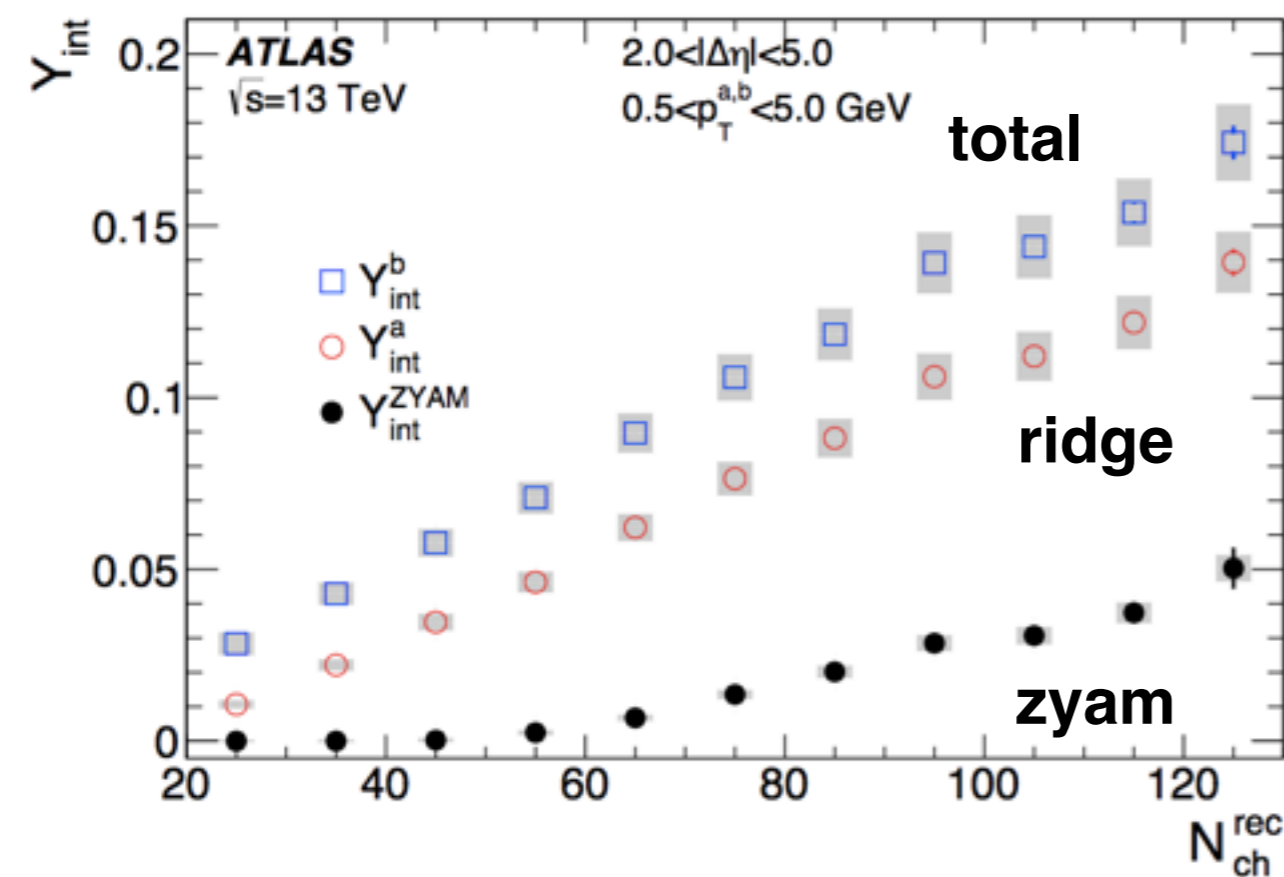
$$Y^{\text{ridge}}(\Delta\phi) = G[1 + 2v_{2,2} \cos(2\Delta\phi)]$$

- G and Y^{ridge} increase with N_{ch}



Low

High

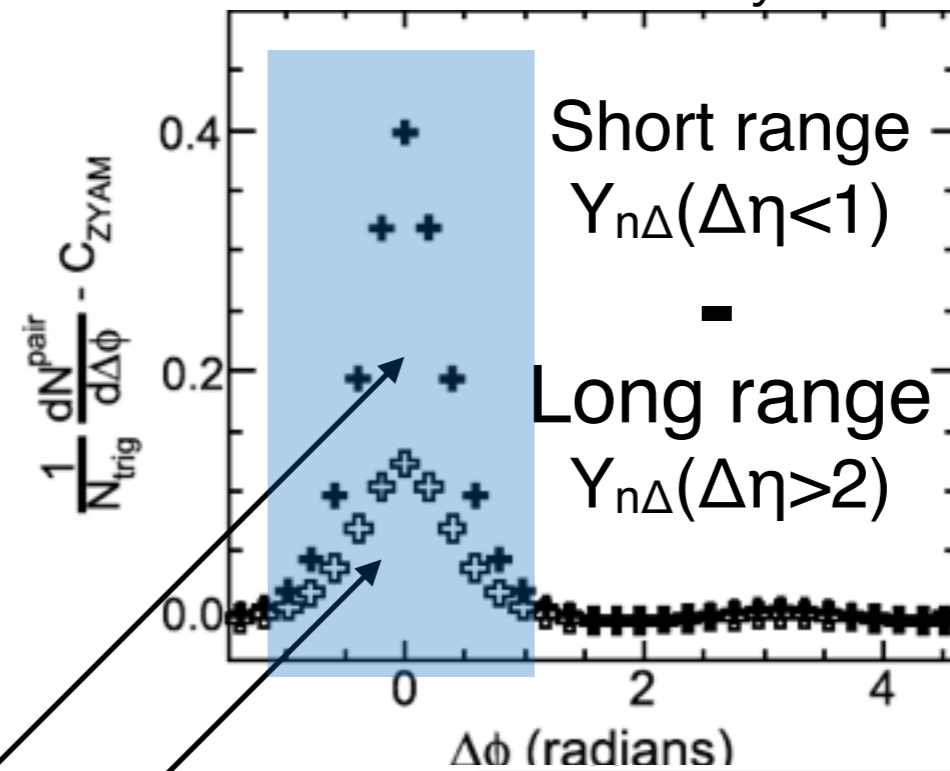
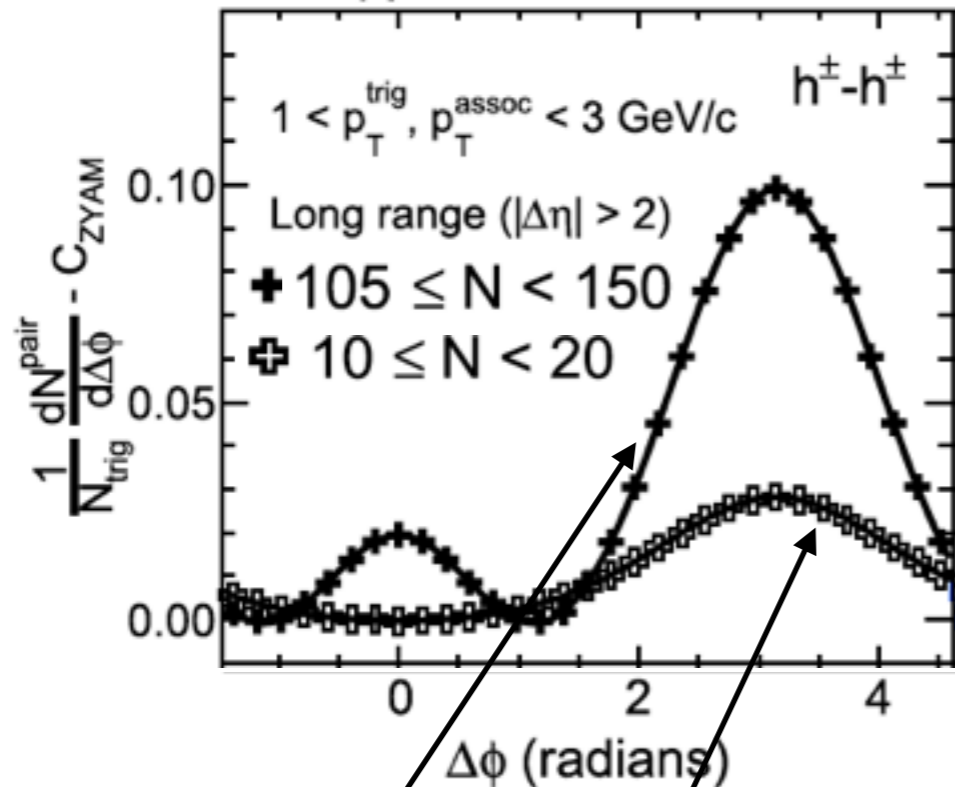


Subtraction method (CMS)

- Extract flow component (v_2) via low mult. subtraction

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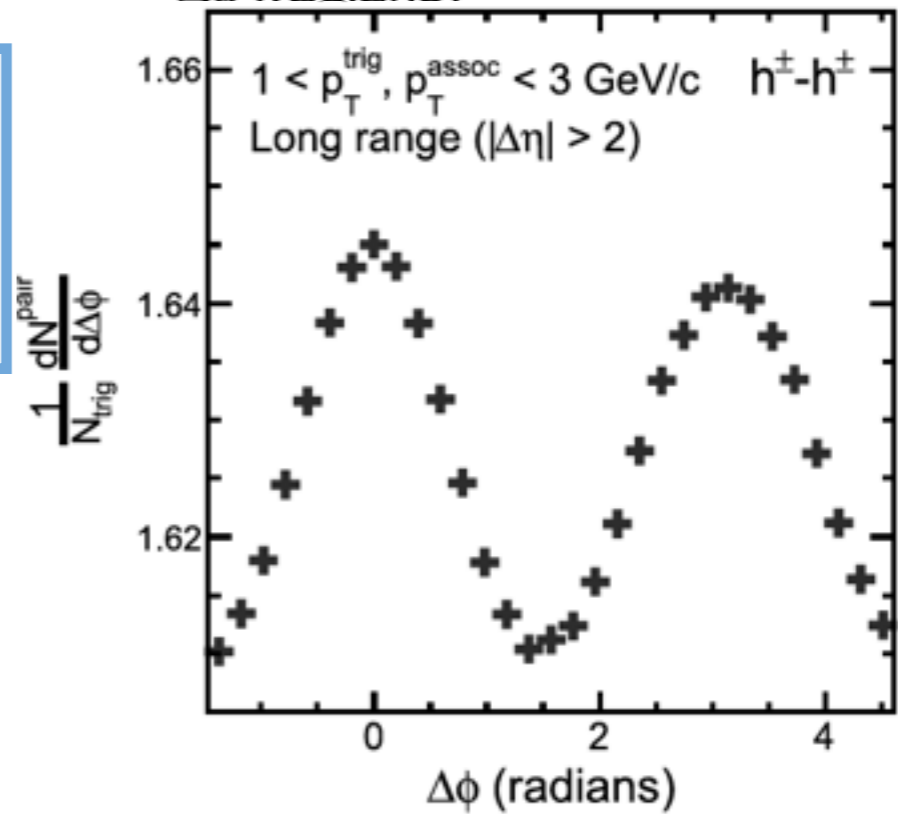
CMS pp $\sqrt{s} = 13$ TeV



$$V_{n\Delta}^{\text{sub}} = V_{n\Delta} - V_{n\Delta}^{\text{per}}$$

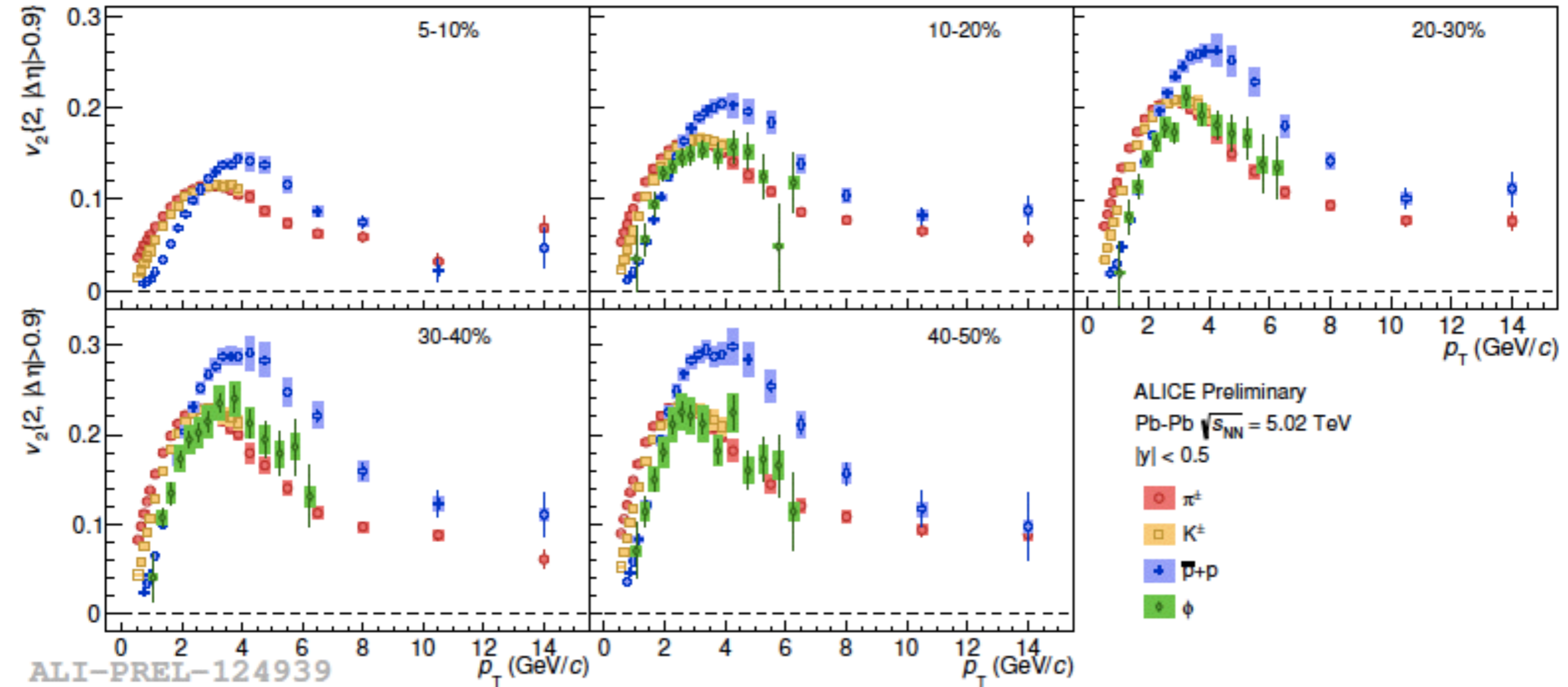
$$\frac{Y_{\text{jet}}}{N_{\text{asso}}} / \frac{Y_{\text{jet}}^{\text{per}}}{N_{\text{asso}}^{\text{per}}}$$

scale factor



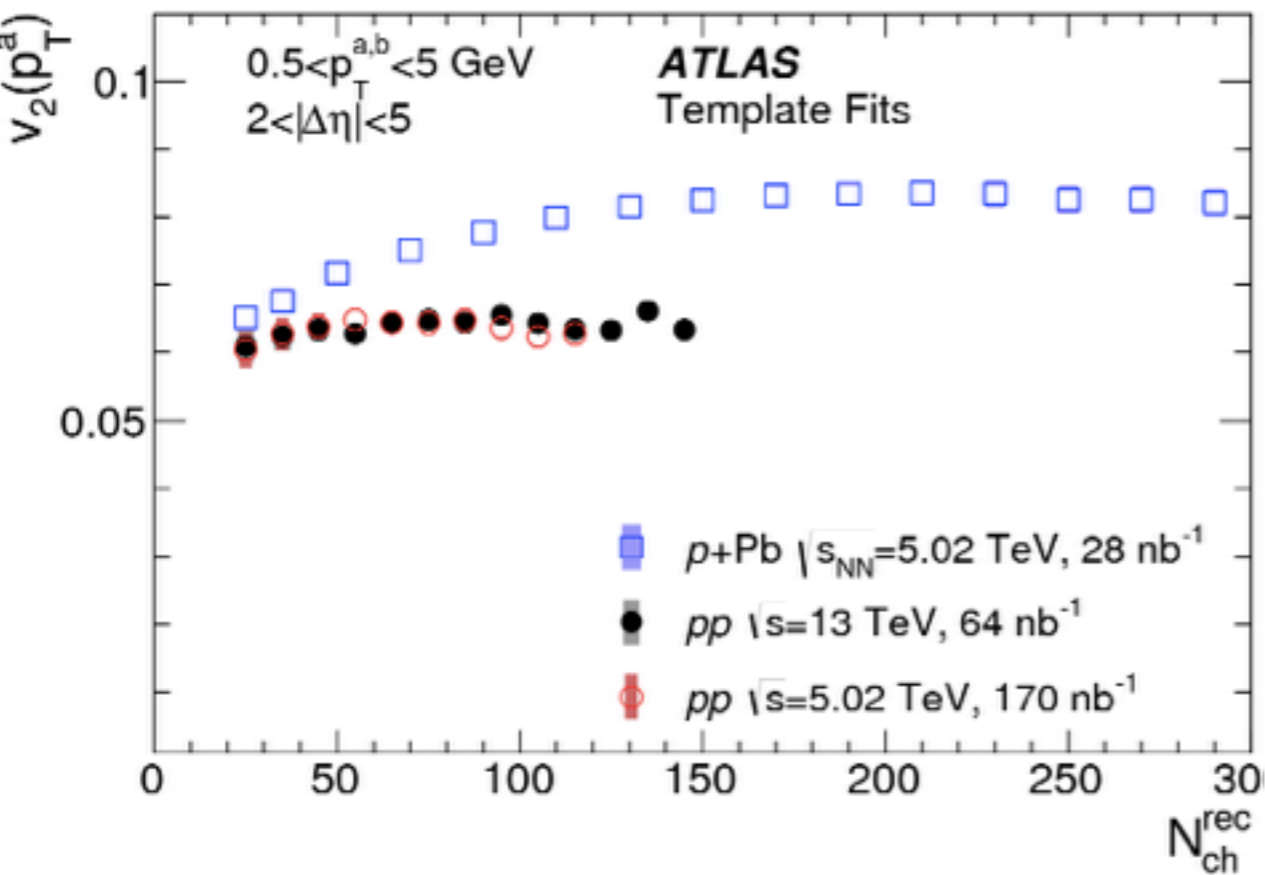
- Scale factor is fraction of jet yield
- Unlike ATLAS, CMS assumes $v_2=0$ at low mult.

PID v_2 in Pb+Pb at 5.02 TeV

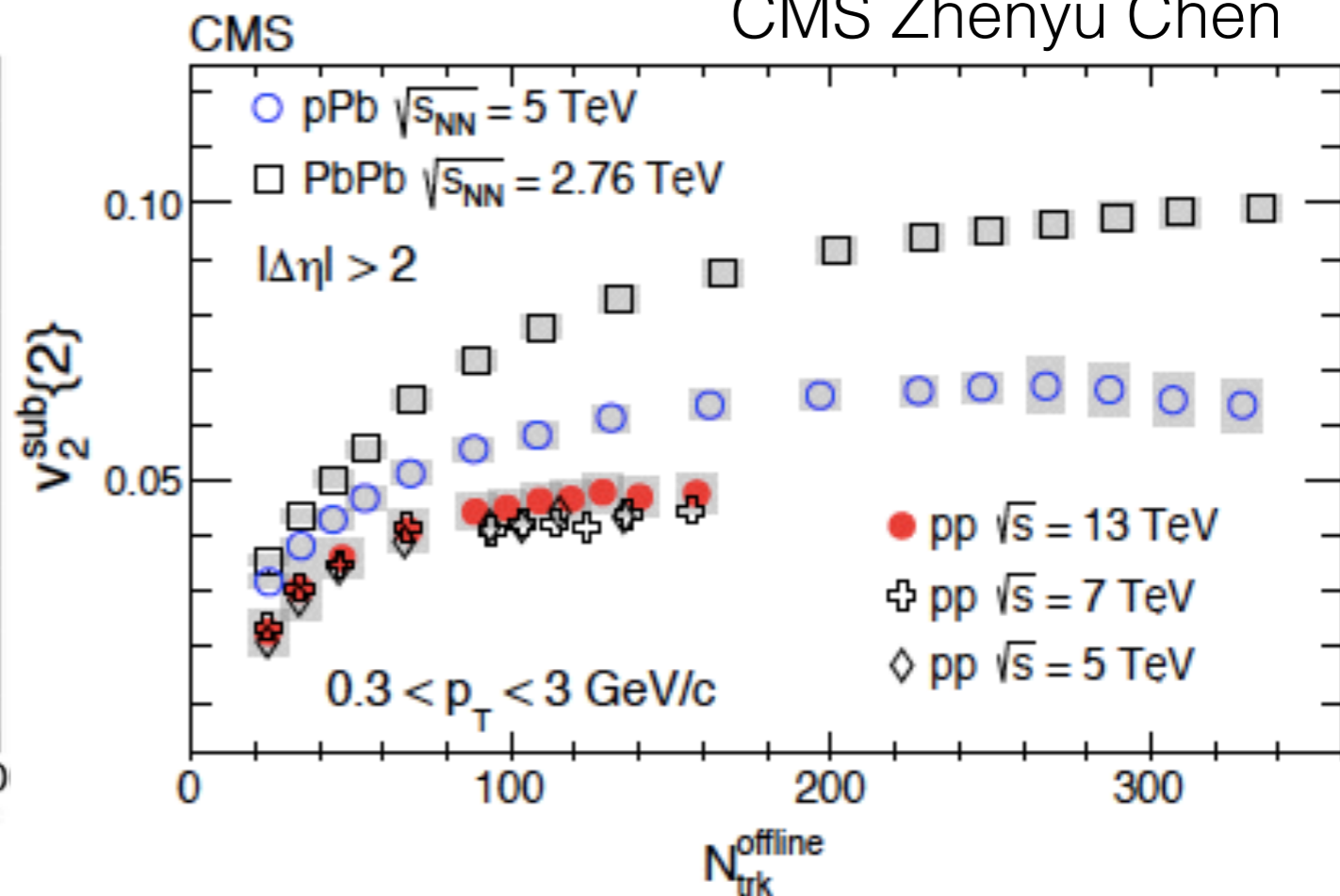


v_2 in p+p 13 TeV

ATLAS Adam Trzupek



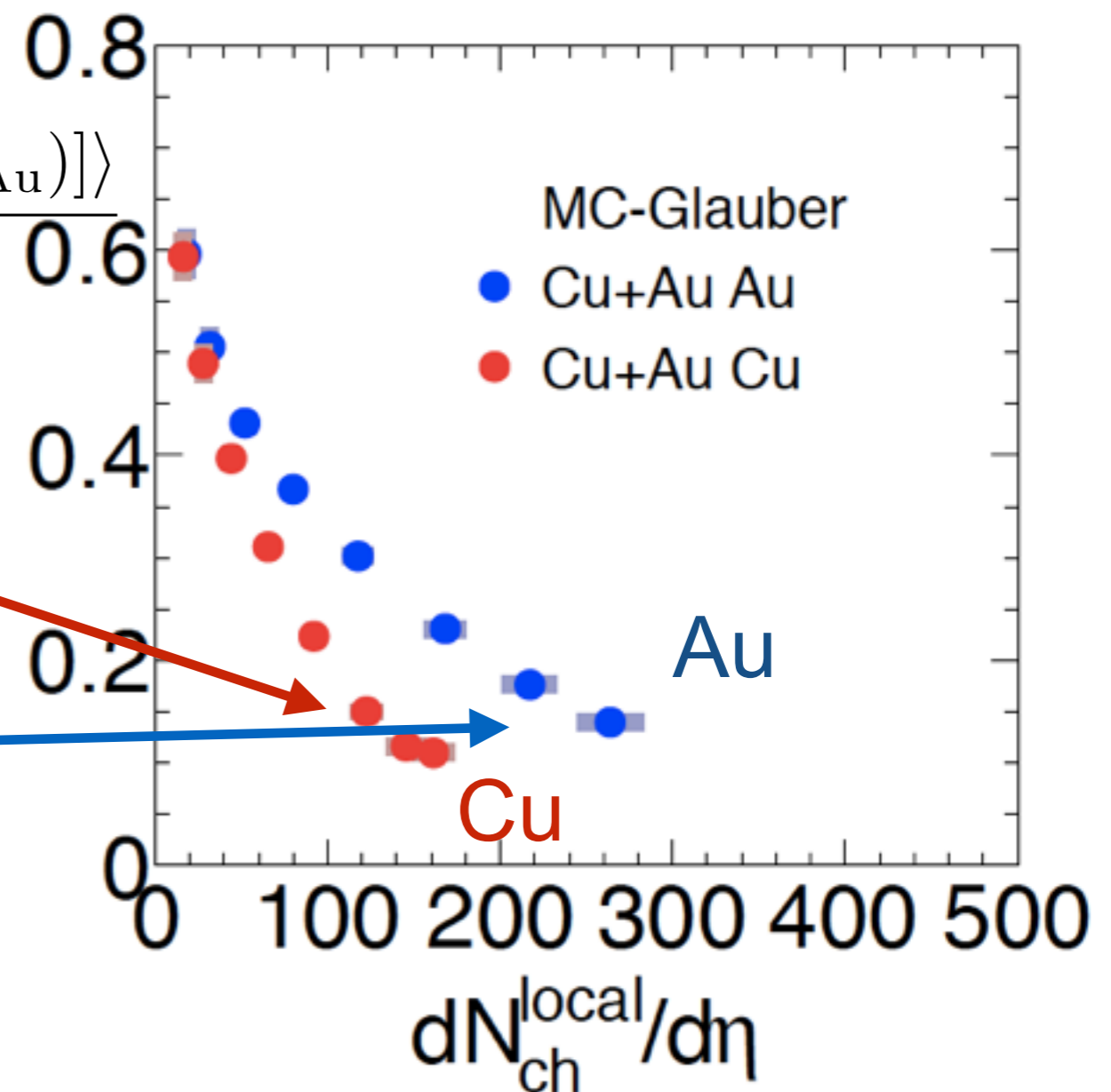
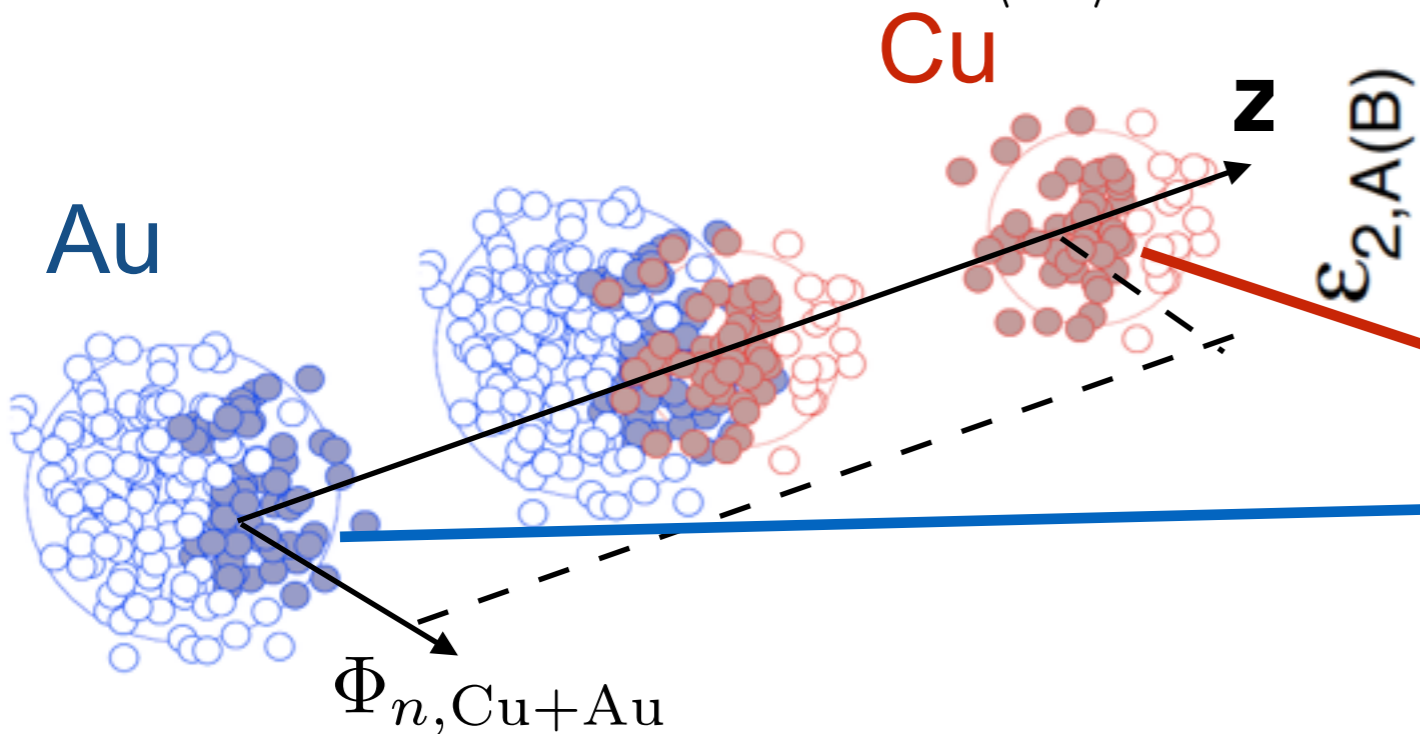
CMS Zhenyu Chen



ϵ_n : Asymmetric initial eccentricity

MC-Glauber model

$$\epsilon_{n, \text{Au}(\text{Cu})} = \frac{\langle r^n \cos[n(\phi_{\text{Au}(\text{Cu})} - \Phi_{n, \text{Cu}+\text{Au}})] \rangle}{\langle r^n \rangle}$$



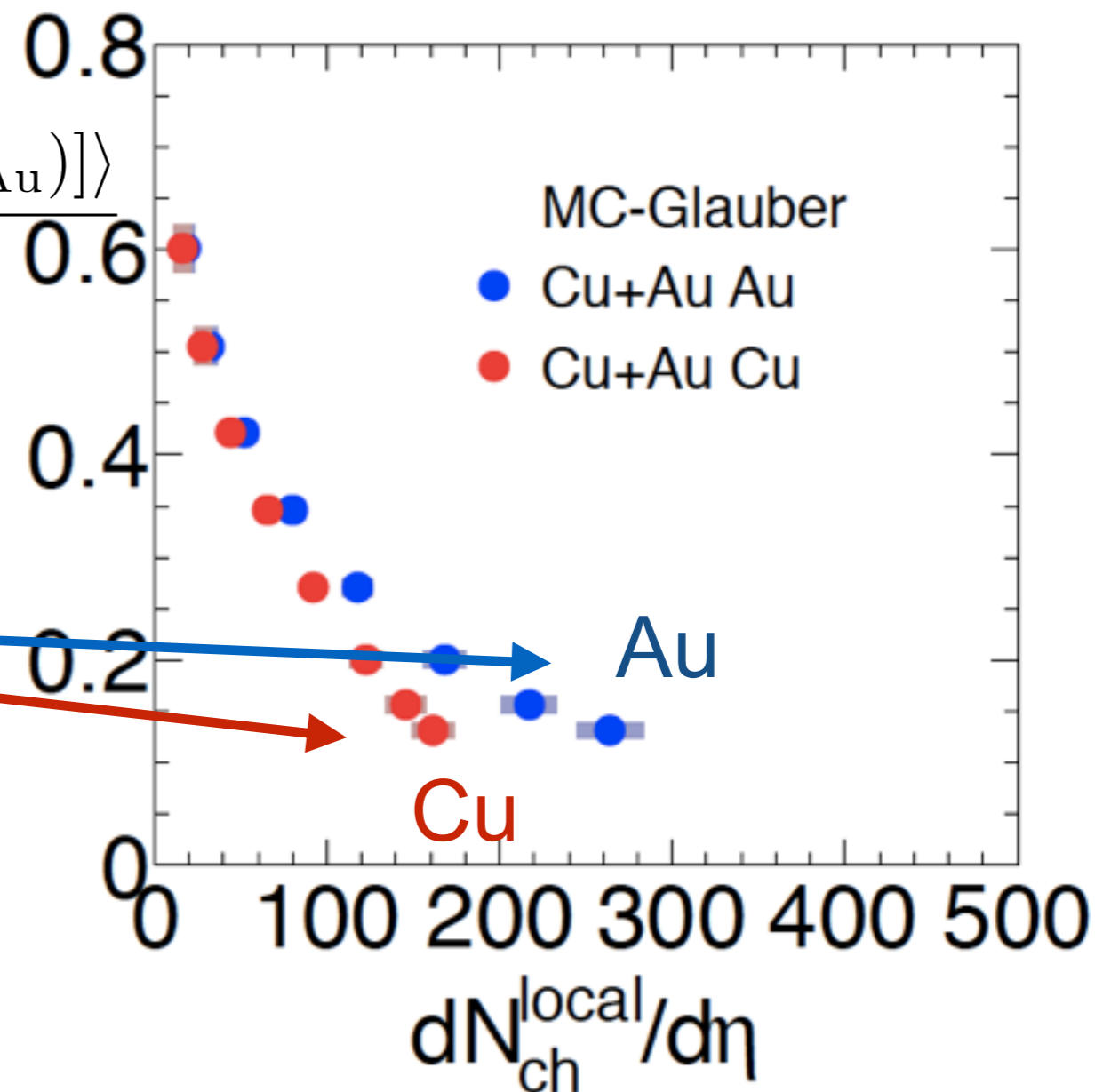
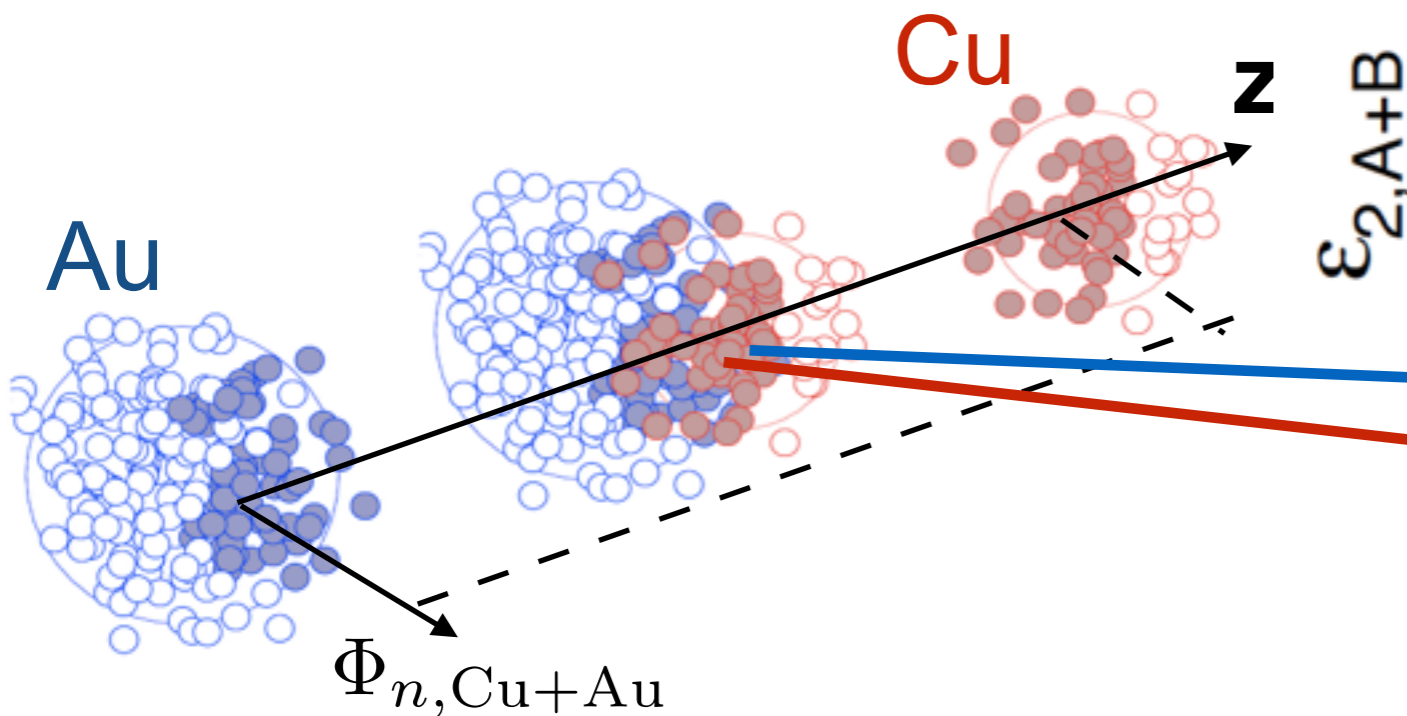
$\epsilon_{n, \text{Au}}$: Au participant eccentricity

$\epsilon_{n, \text{Cu}}$: Cu participant eccentricity

ϵ_n : Symmetric initial eccentricity

MC-Glauber model

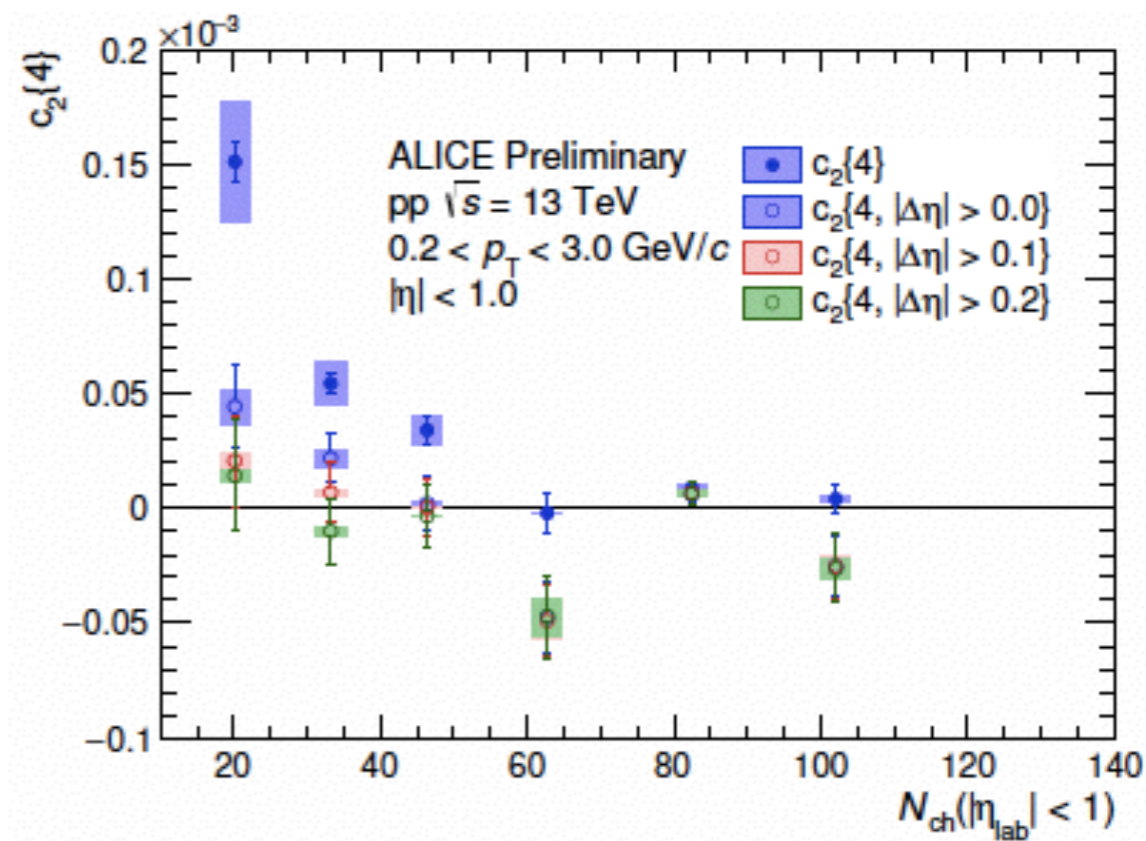
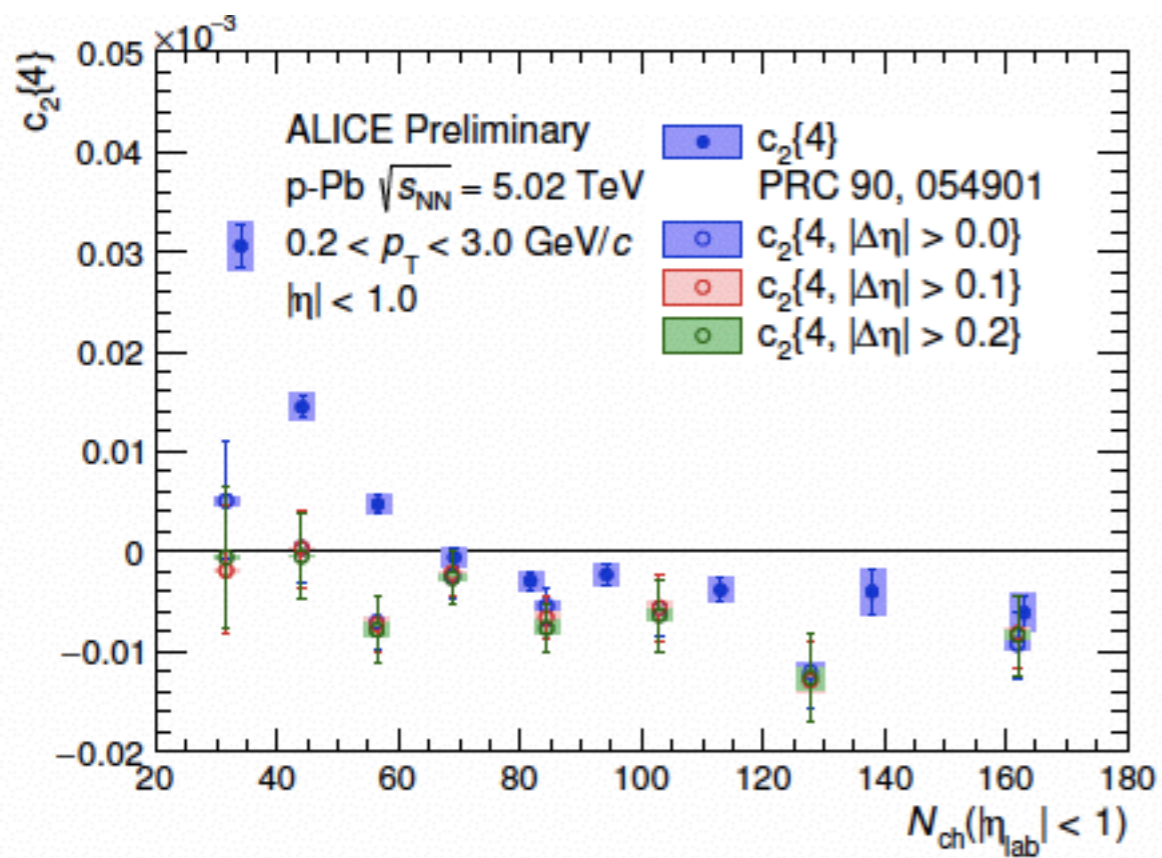
$$\epsilon_{n,Au(Cu)} = \frac{\langle r^n \cos[n(\phi_{Au(Cu)} - \Phi_{n,Cu+Au})] \rangle}{\langle r^n \rangle}$$

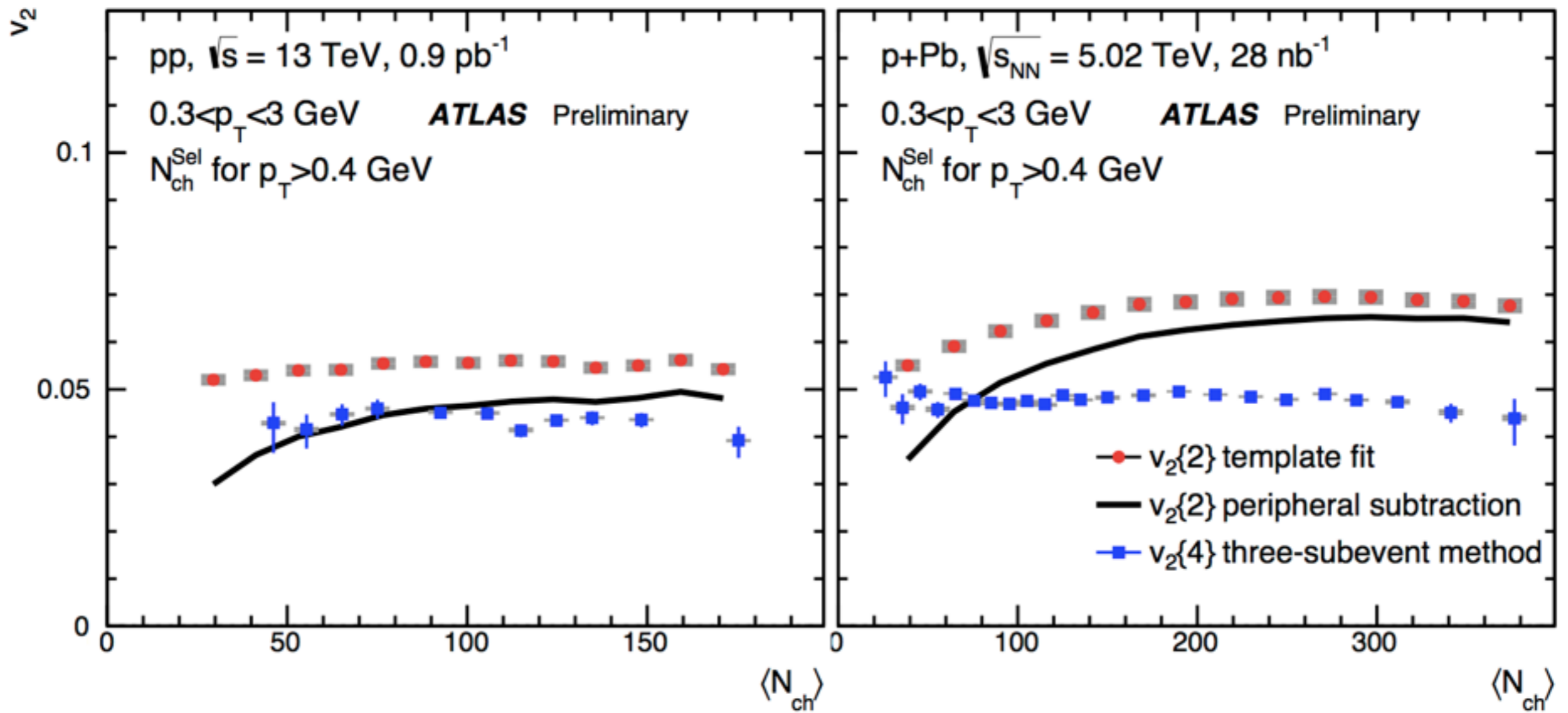


$\epsilon_n, Cu+Au$: Cu+Au participant eccentricity

$\epsilon_n, Cu+Au$: Cu+Au participant eccentricity

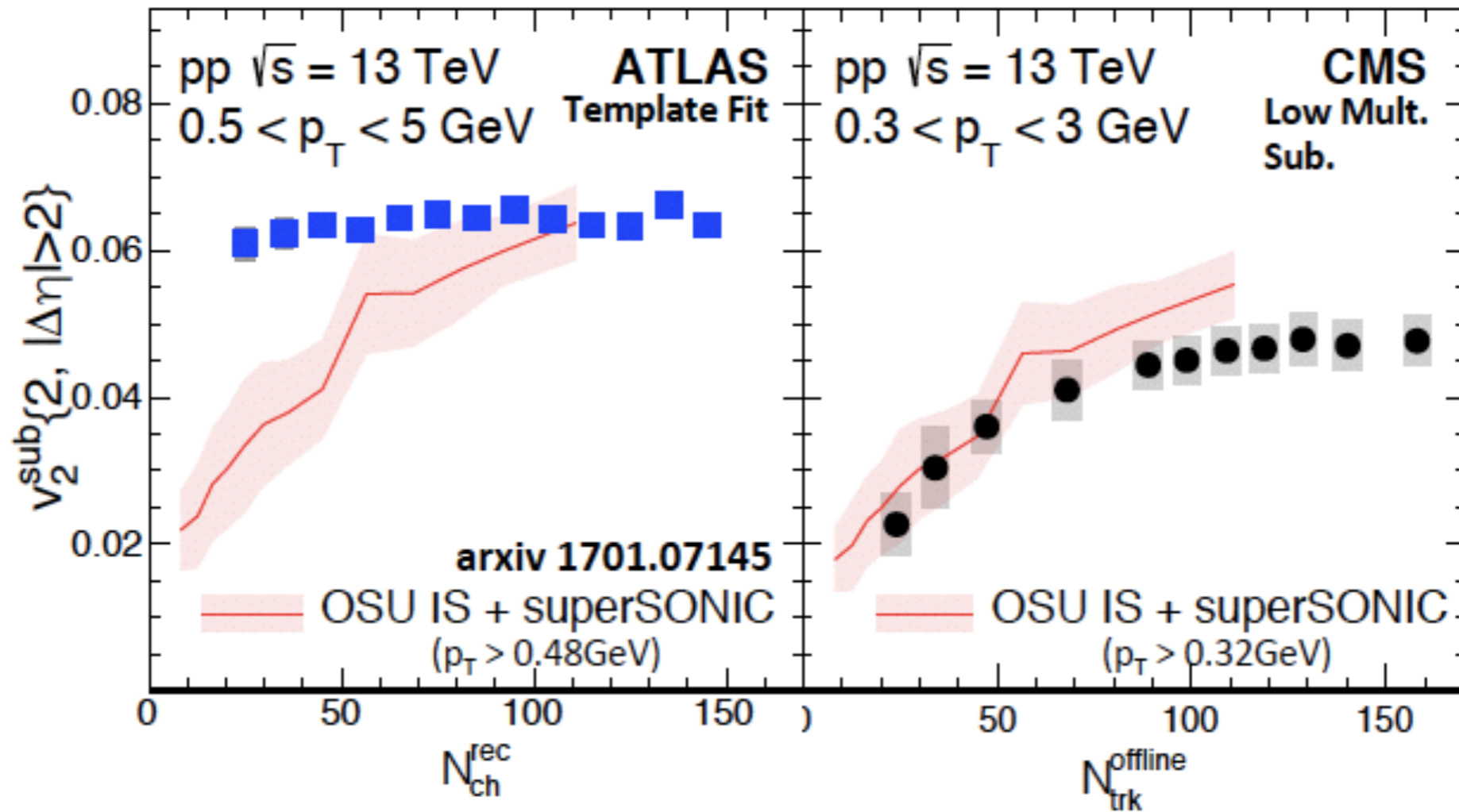
Additional removal of non-flow





v_2 in p+p 13 TeV

CMS Zhenyu Chen

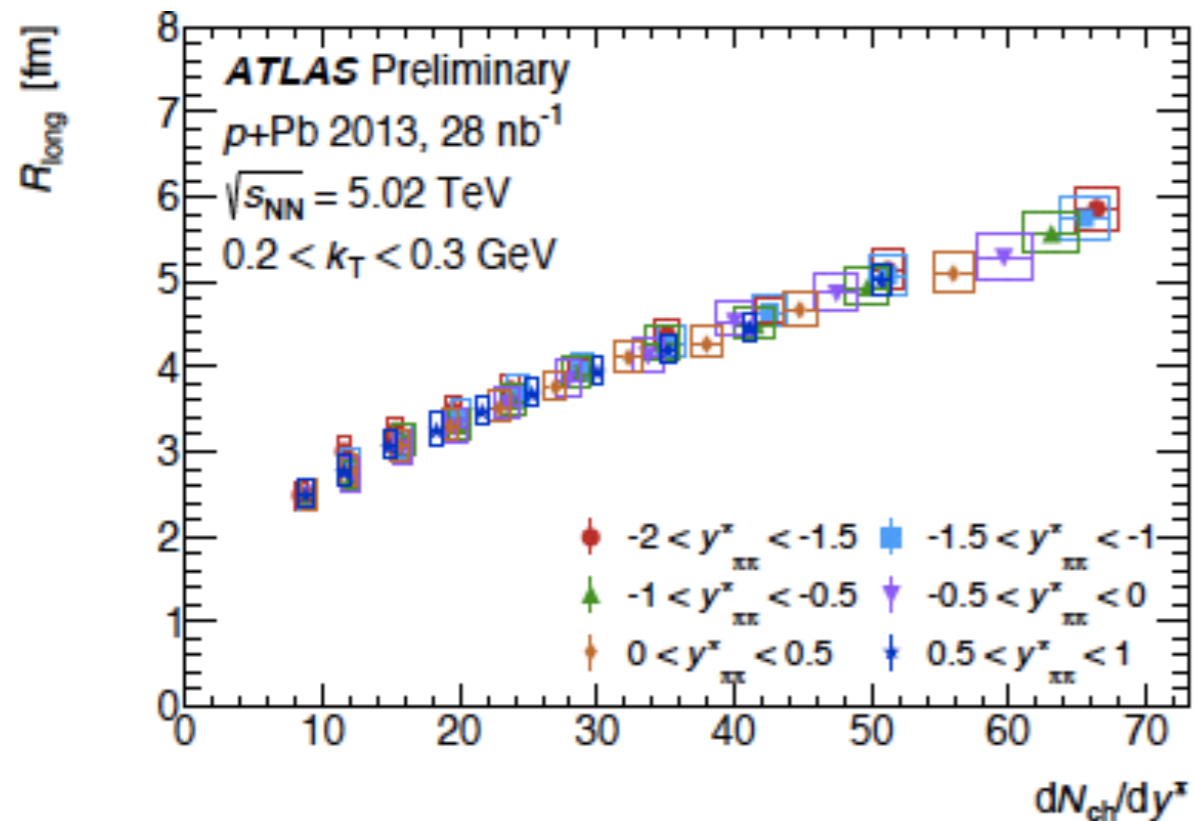
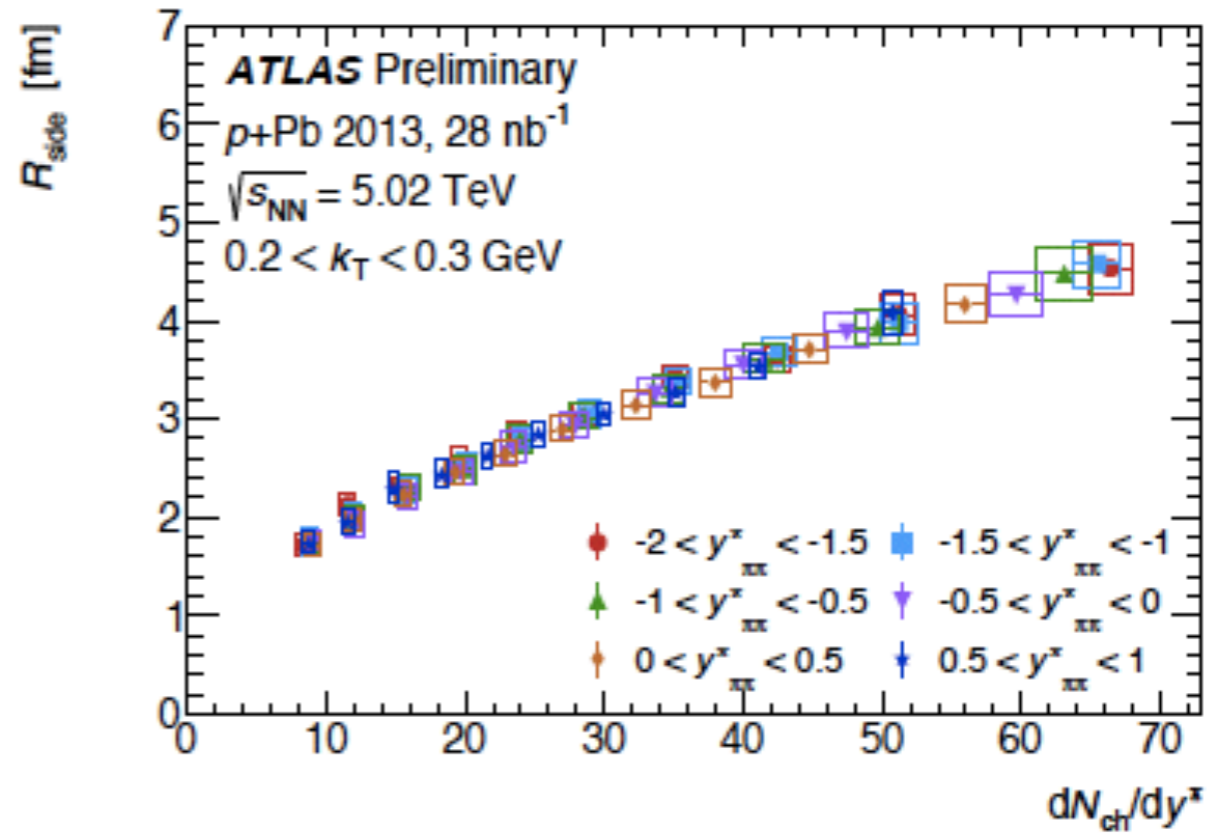
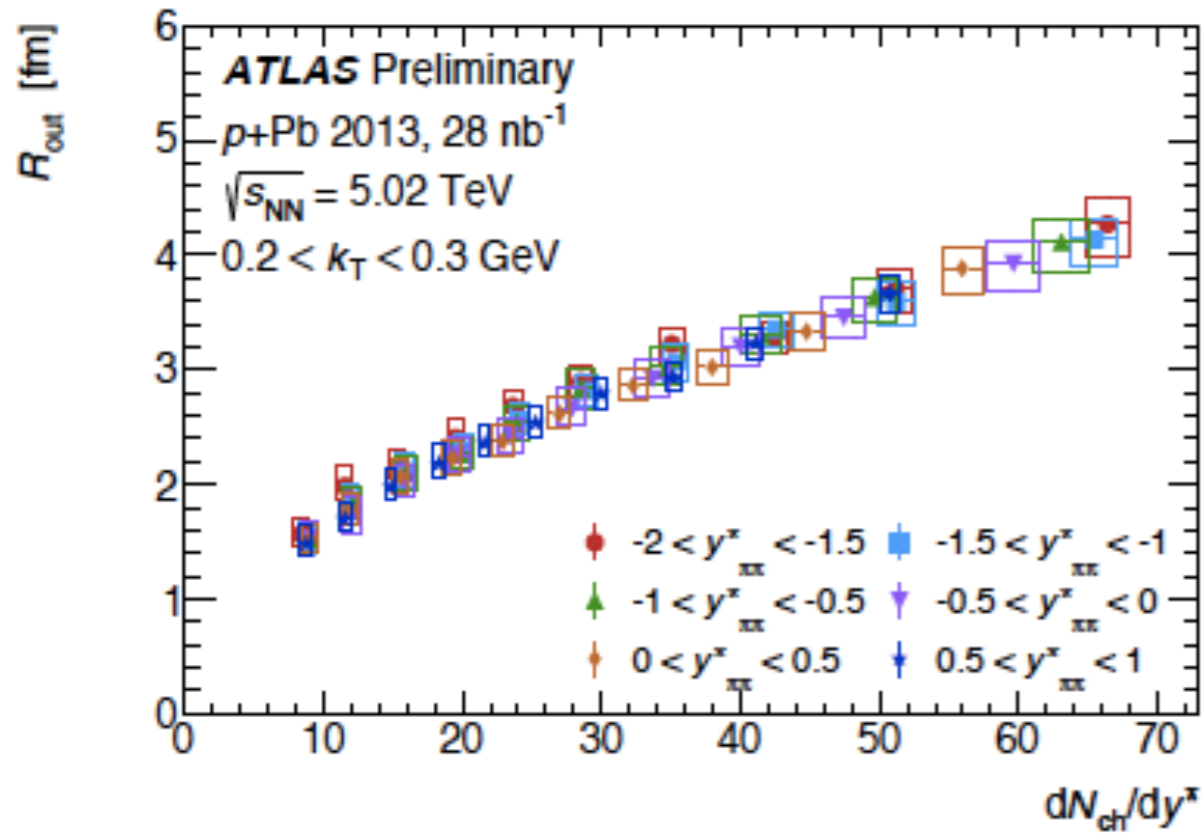


- ATLAS Template fit
- No multiplicity dependence

- CMS Low mult. subtraction method
- Strong multiplicity dependence
- Hydrodynamics well reproduce

→ Results depend on

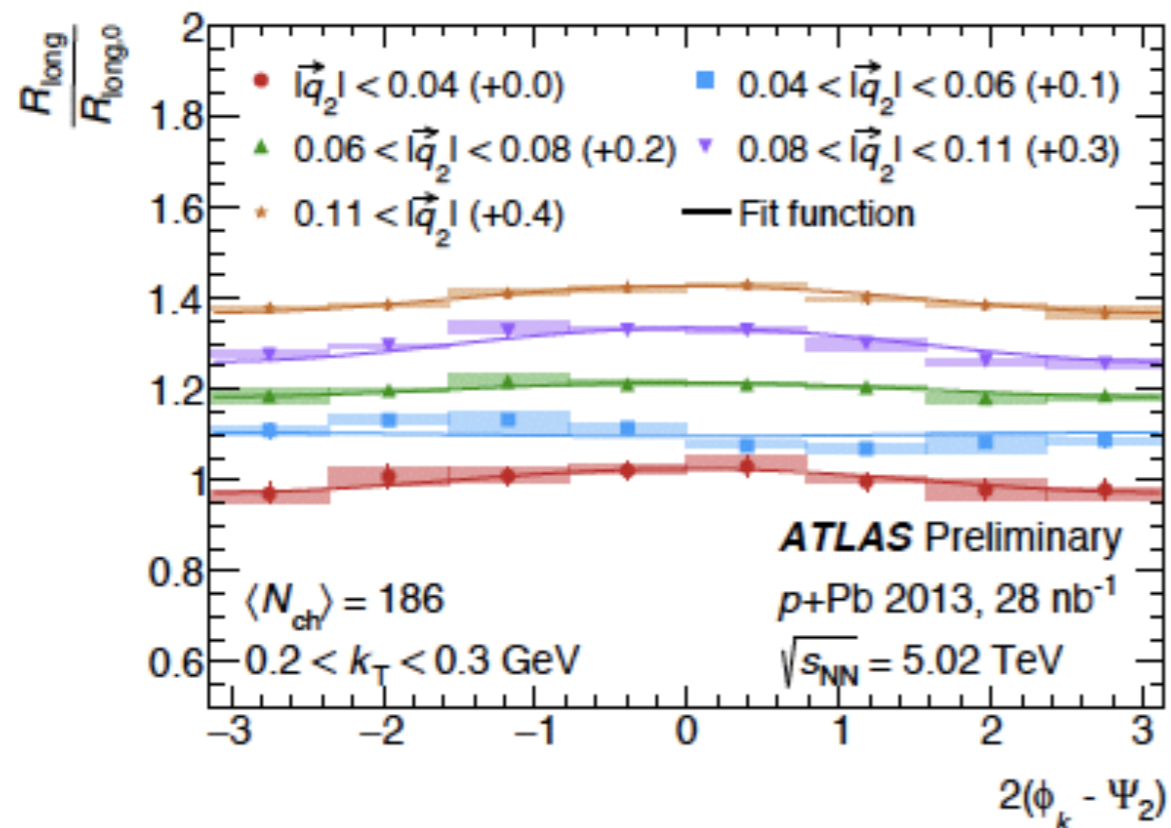
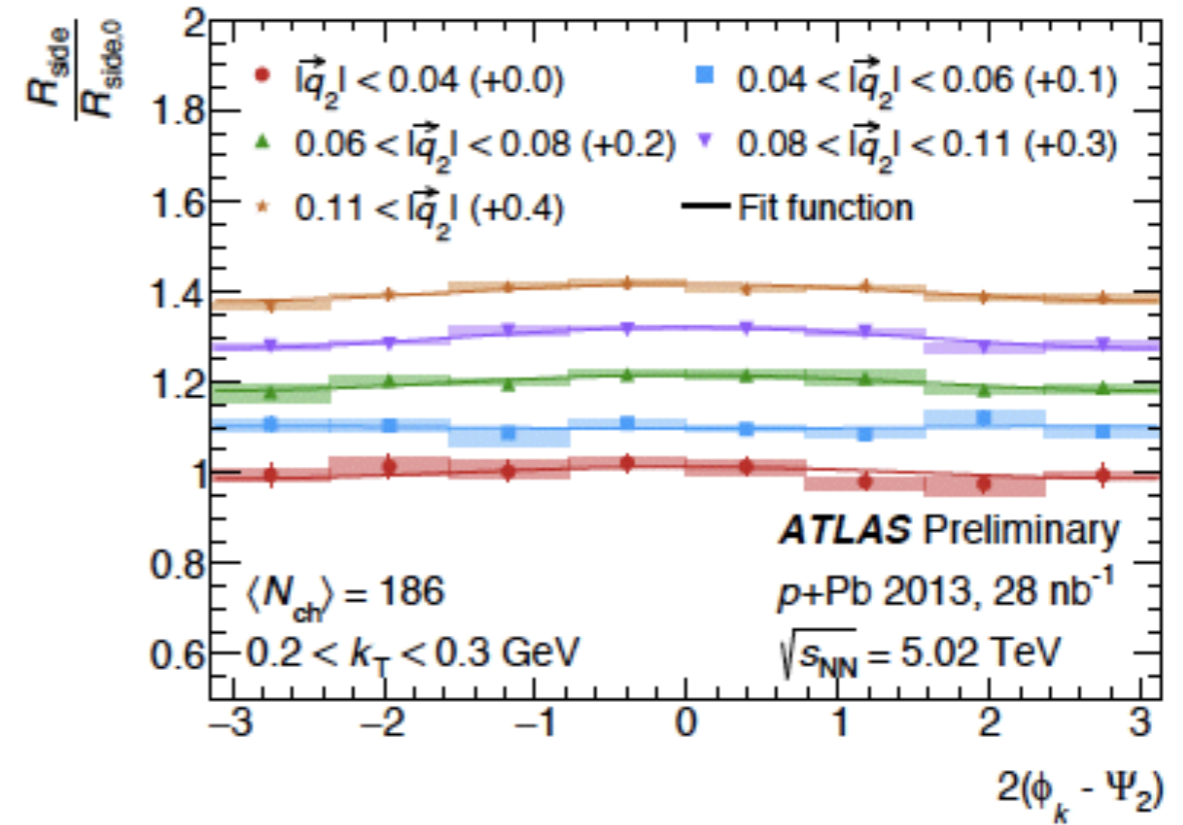
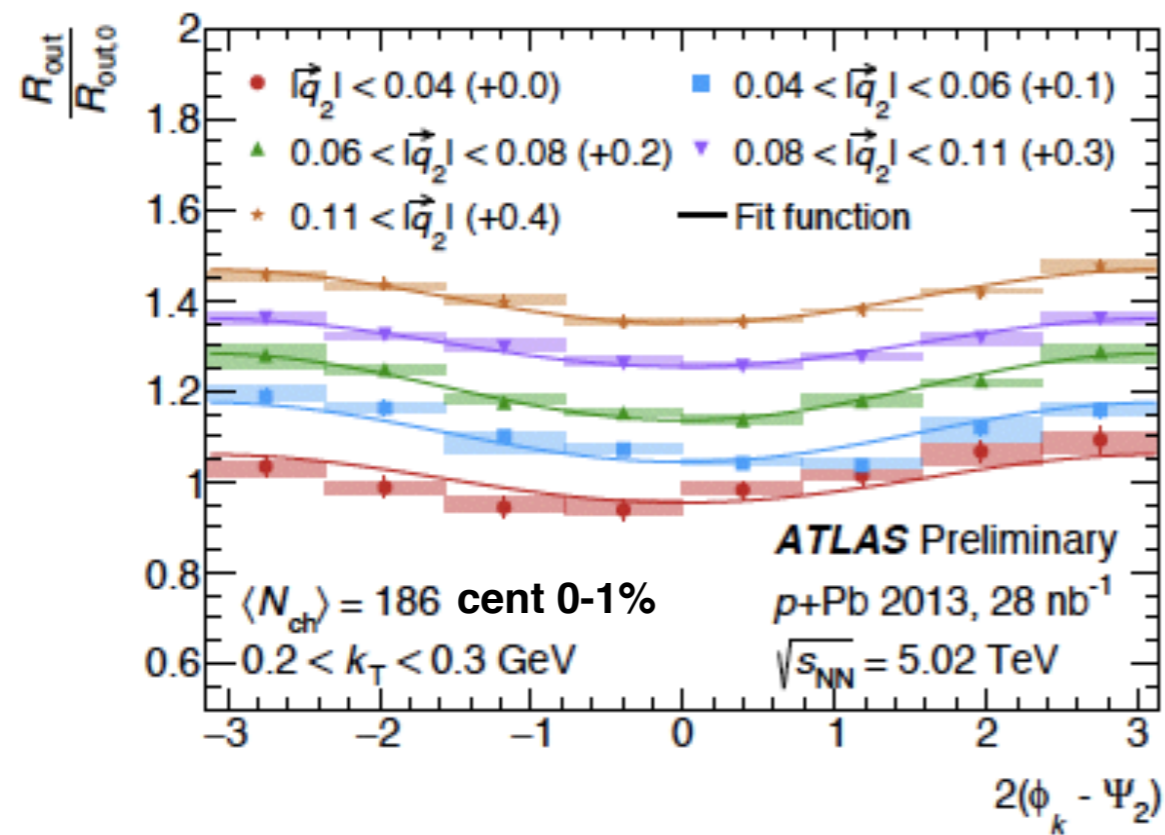
$p+Pb$ HBT vs local dN/dy

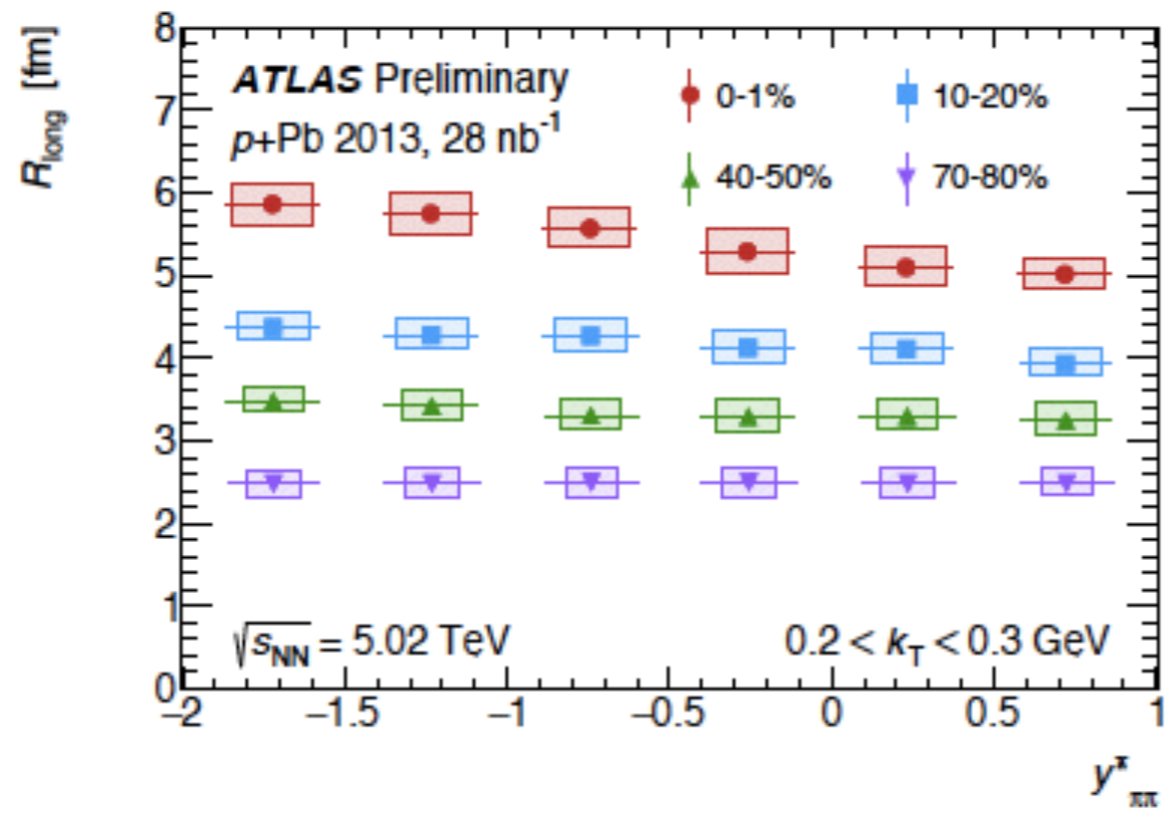


- HBT radii is highly correlated with local multiplicity

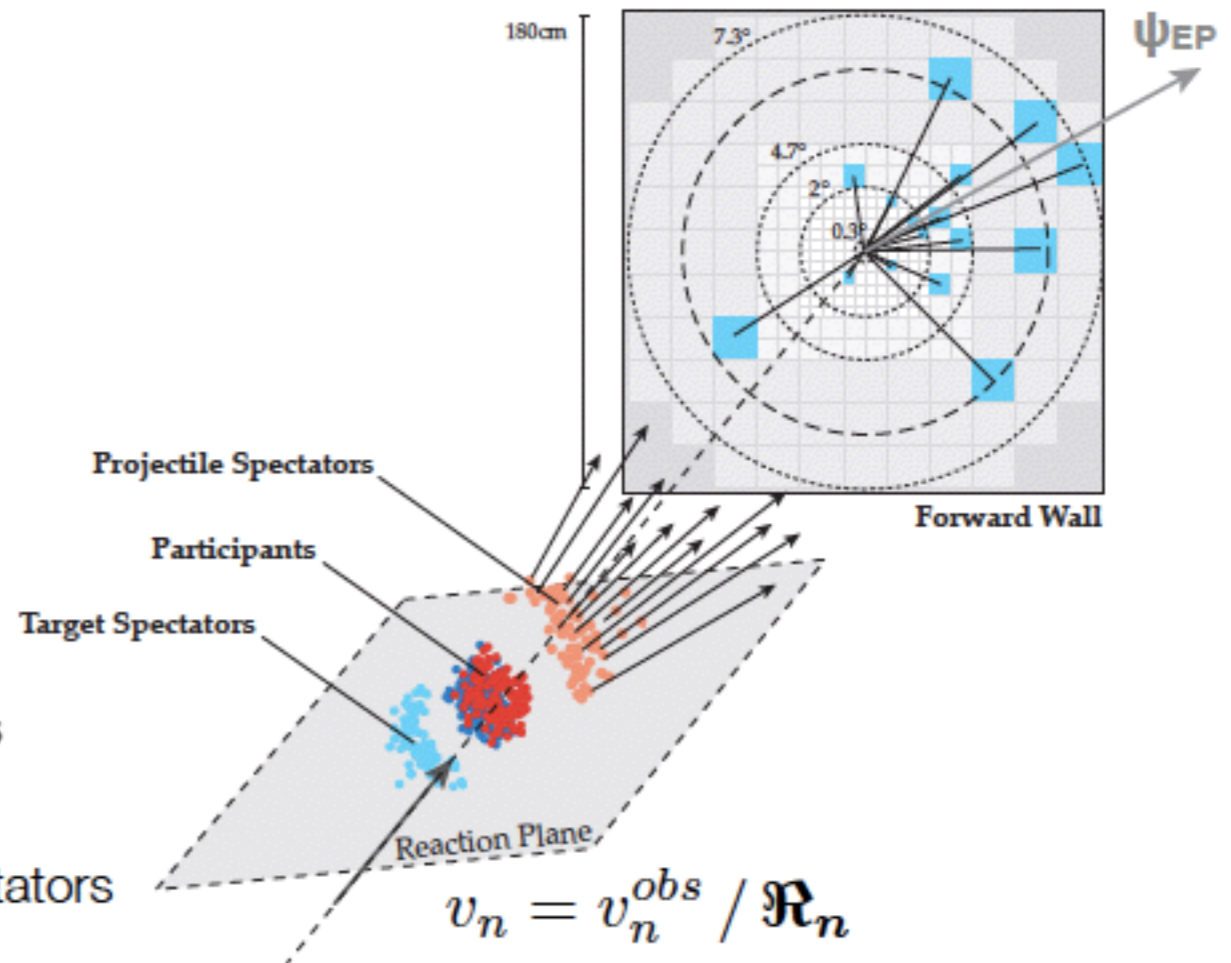
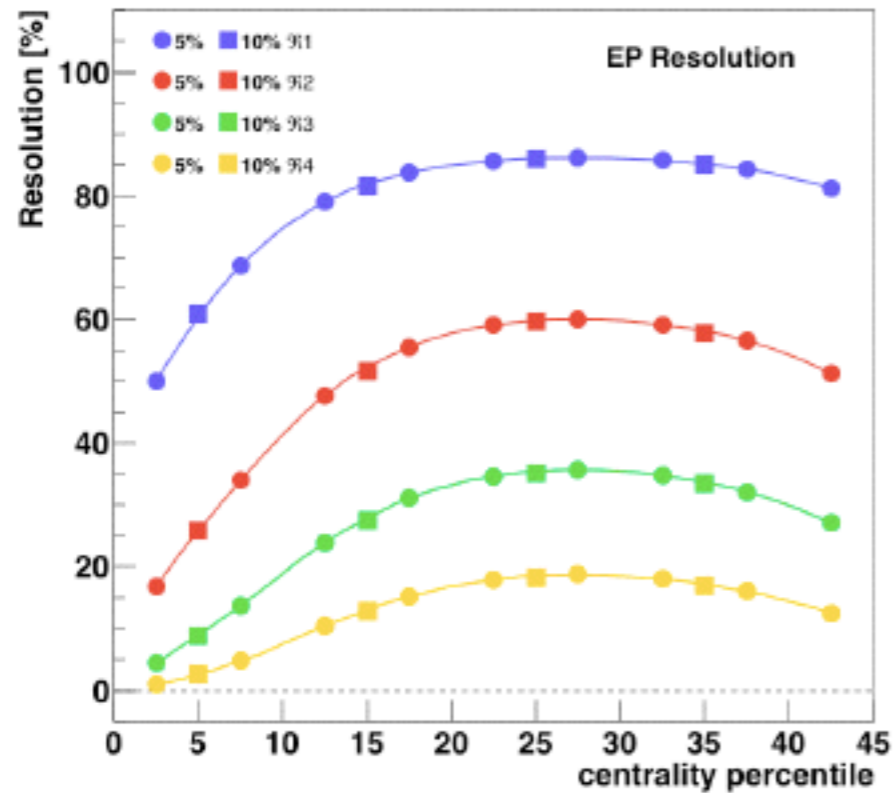
HBT w.r.t Ψ_2 in p+Pb with event shape engineering

ATLAS M. Clark





Event Plane Reconstruction



- Event plane based on projectile spectators
- Resolution determined with two sub-event method and corrected with method described in J.-Y. Ollitrault, [arXiv:nucl-ex/9711003](https://arxiv.org/abs/nucl-ex/9711003)

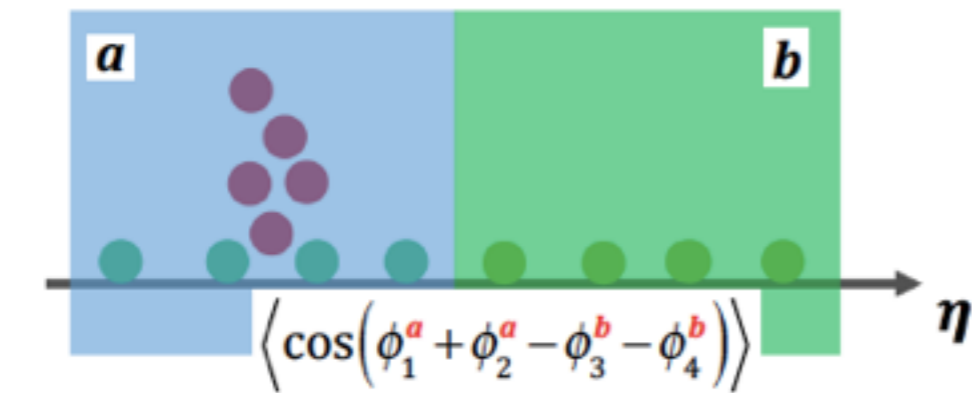
$$v_n = v_n^{obs} / \mathfrak{R}_n$$

$$\mathfrak{R}_n = \langle \cos[n(\Psi_n - \Psi_{RP})] \rangle$$

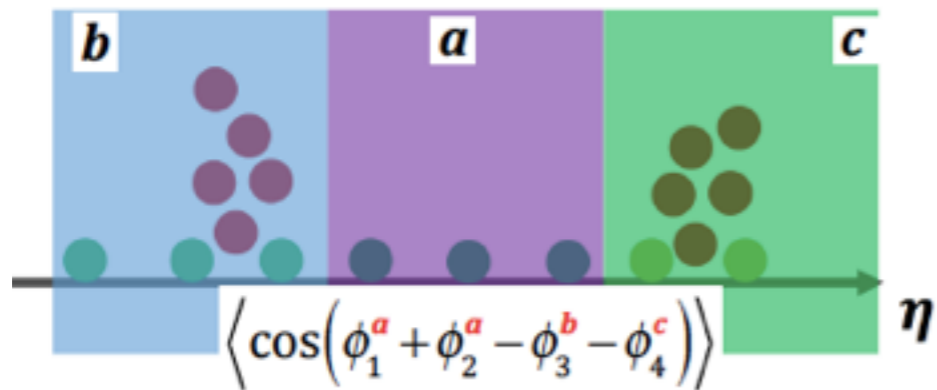
$$= \sqrt{2 \langle \cos[n(\Psi_n^A - \Psi_n^B)] \rangle}$$

Additional removal of non-flow: 3sub method

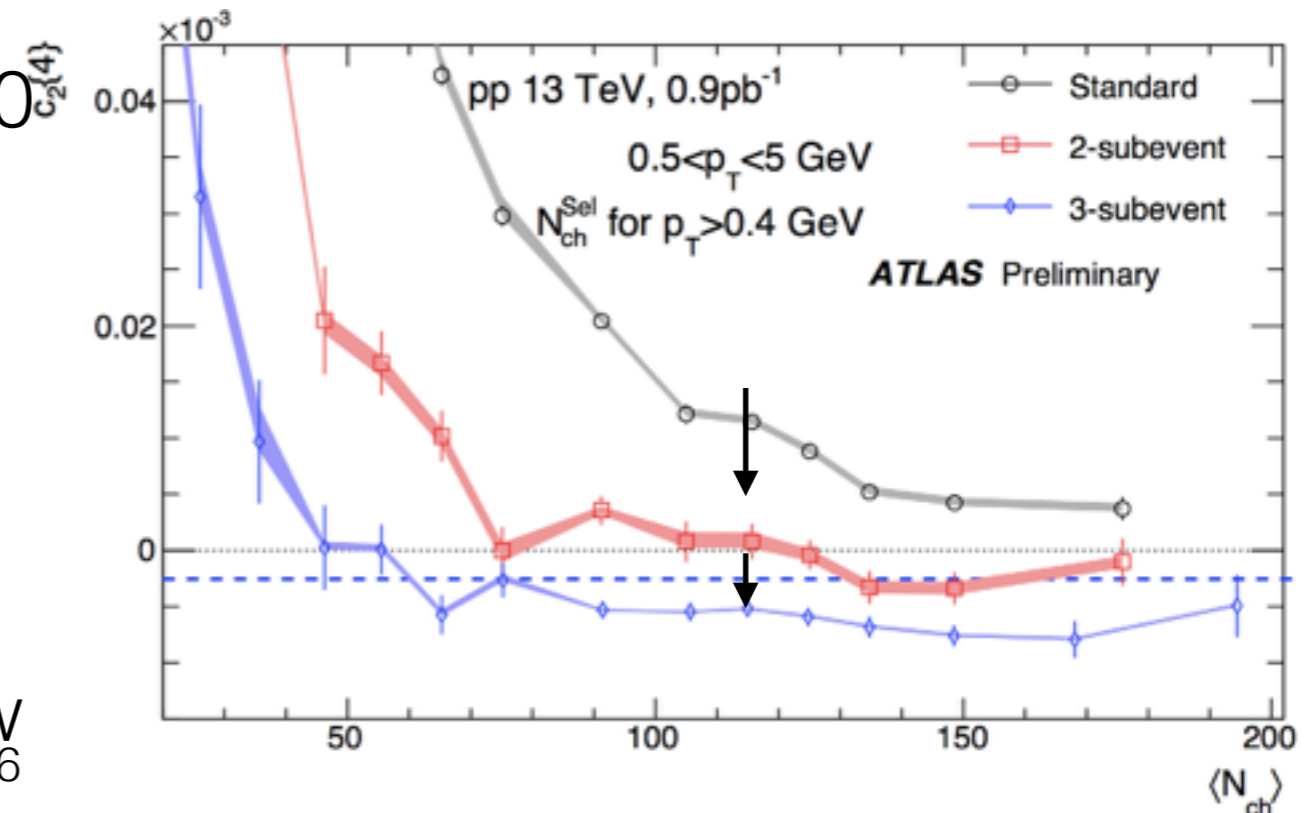
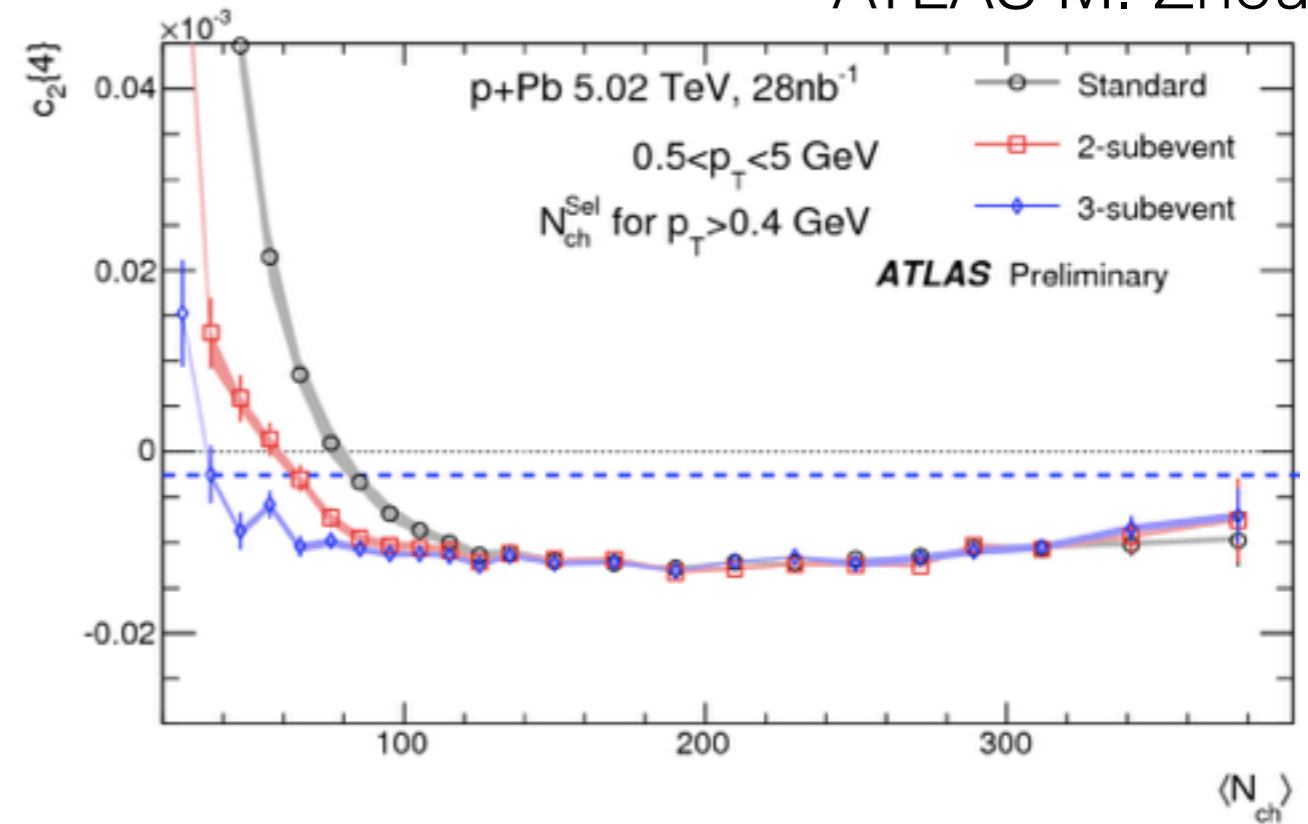
ATLAS M. Zhou



2 sub-event



3 sub-event



- Sub-event method arXiv:1701.03830

- p+Pb

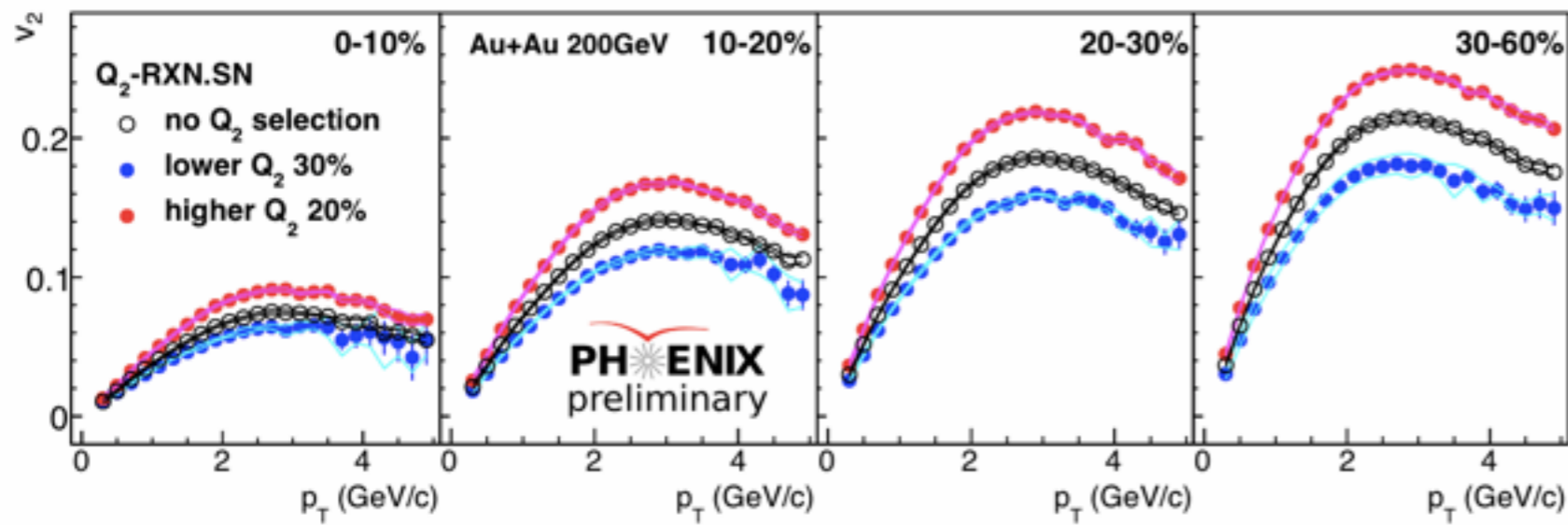
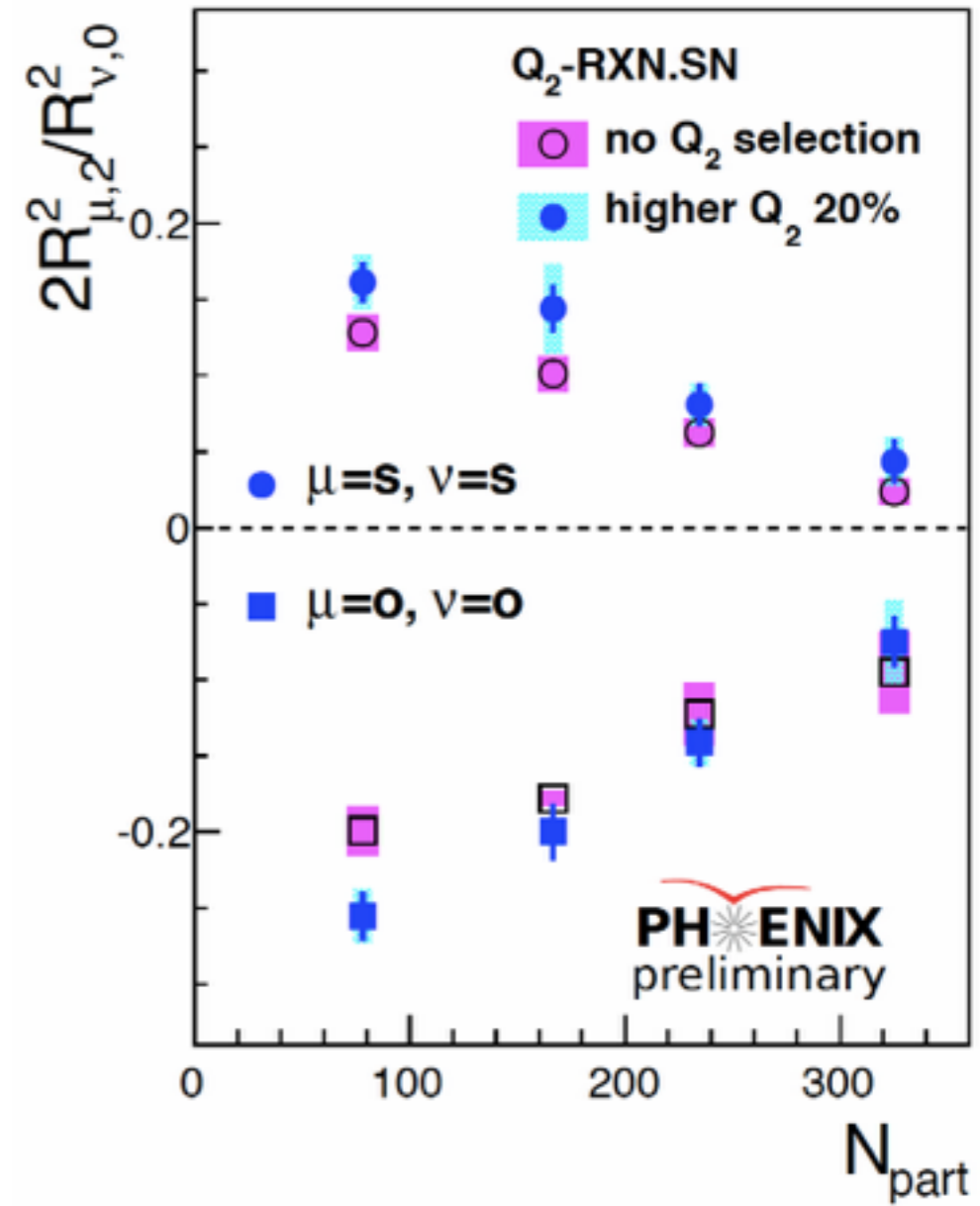
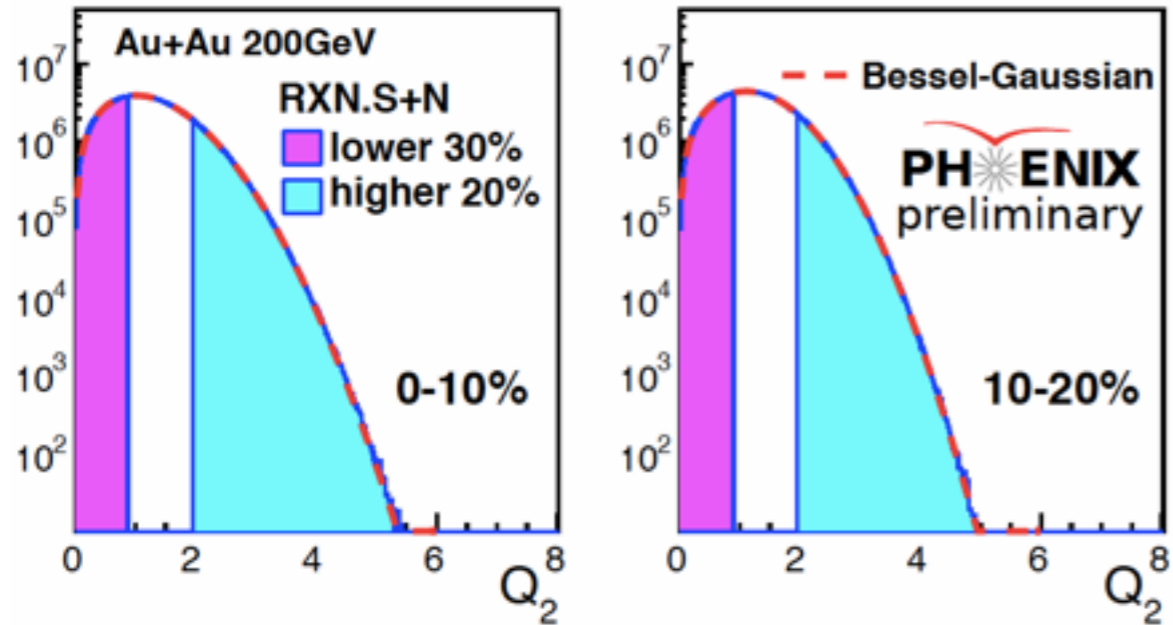
-Larger N_{ch}: non-flow is small

-Smaller N_{ch}: 3sub method reduce non-flow

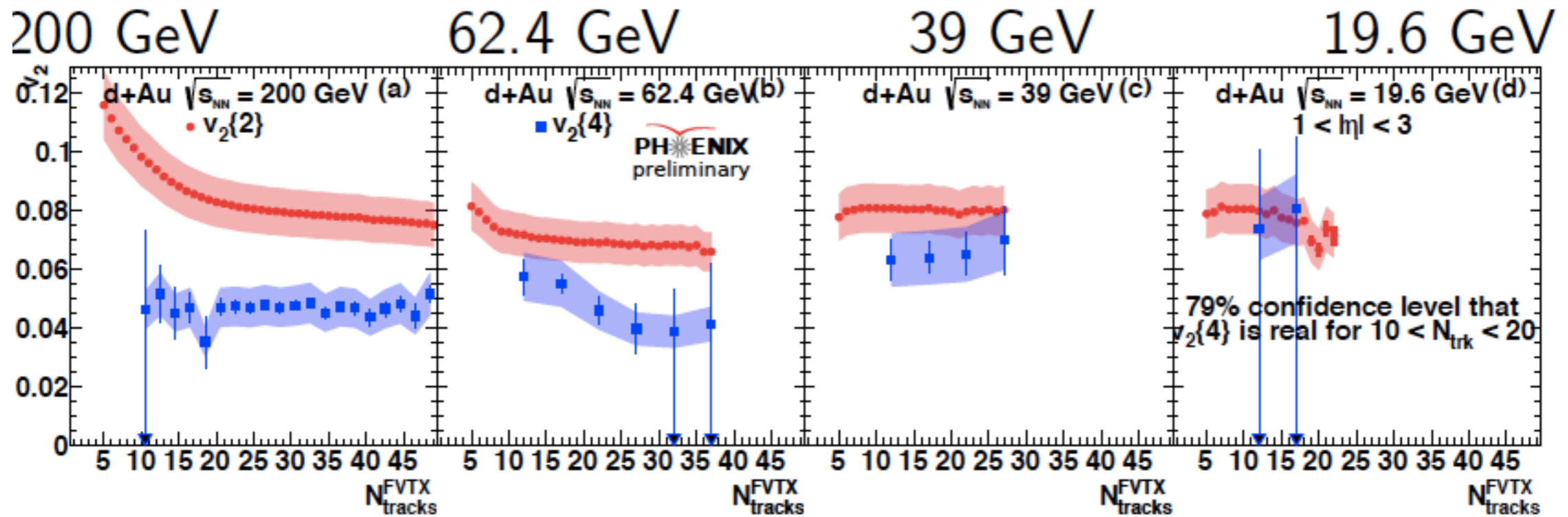
- p+p

-Sub event method reduces non-flow

Final eccentricity with ESE

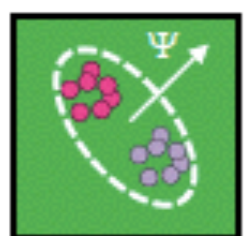
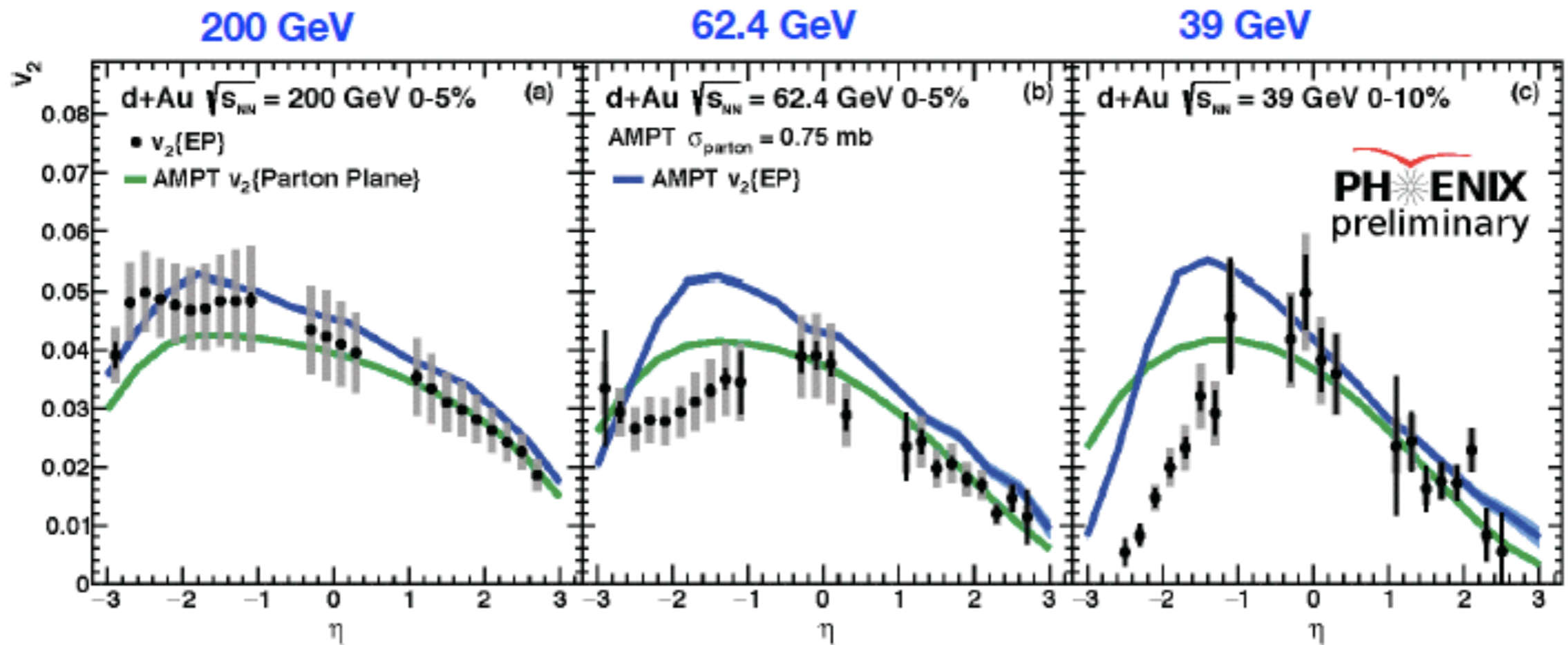


$v_2\{2\}$ and $v_2\{4\}$ in the d+Au beam energy scan

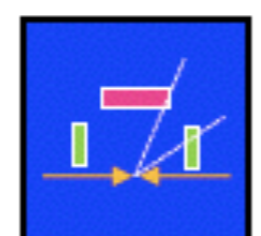


- $v_2\{2\}$ relatively constant with N_{trks}^{FVTX} and collision energy
- **Observation of real $v_2\{4\}$ in d+Au at all energies!!!**
- **Strong evidence for collectivity**

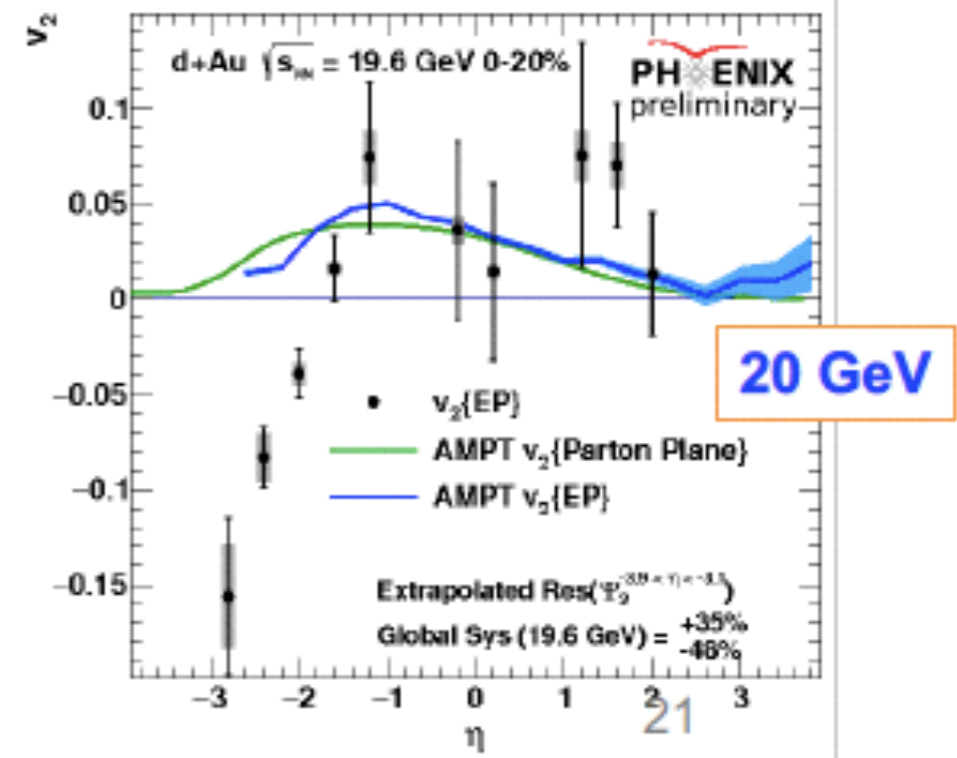
Insights from AMPT



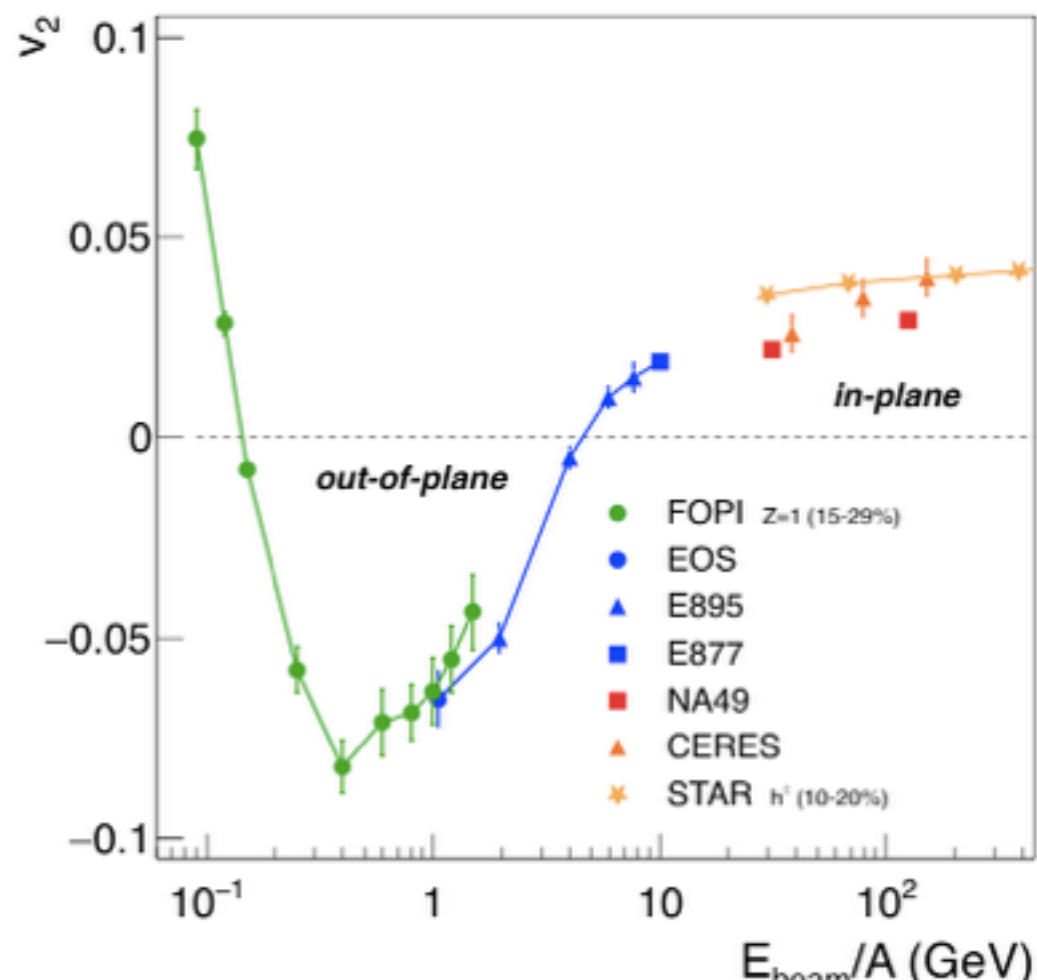
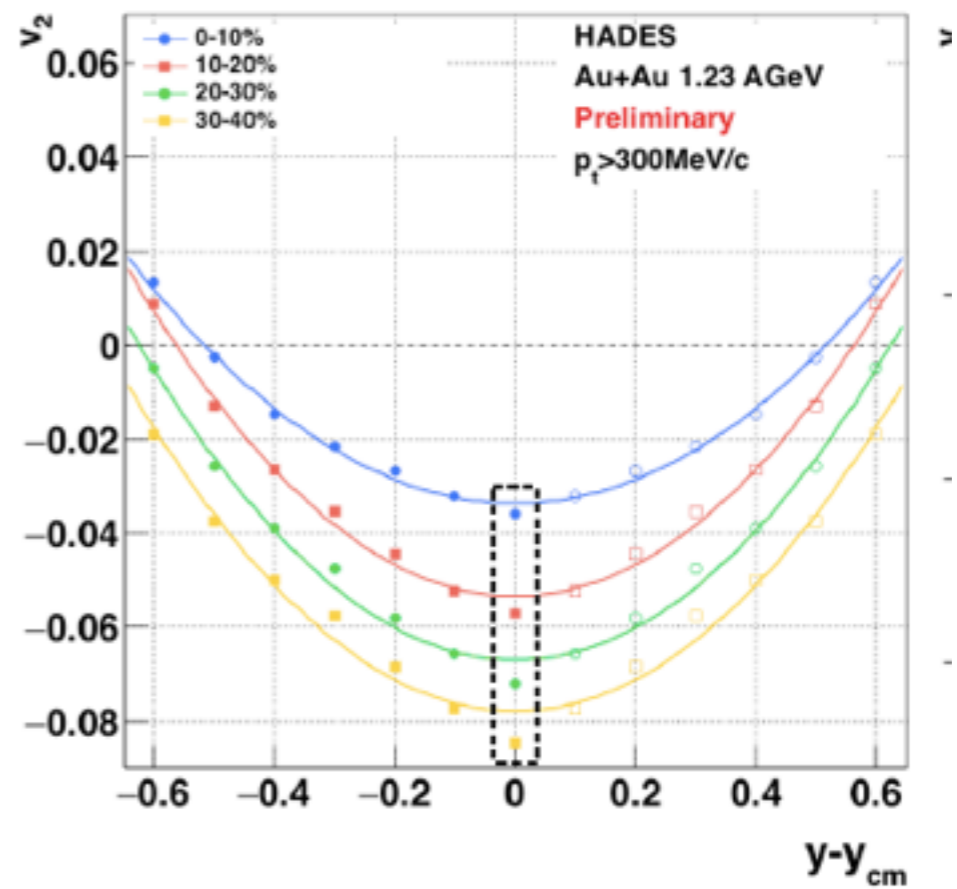
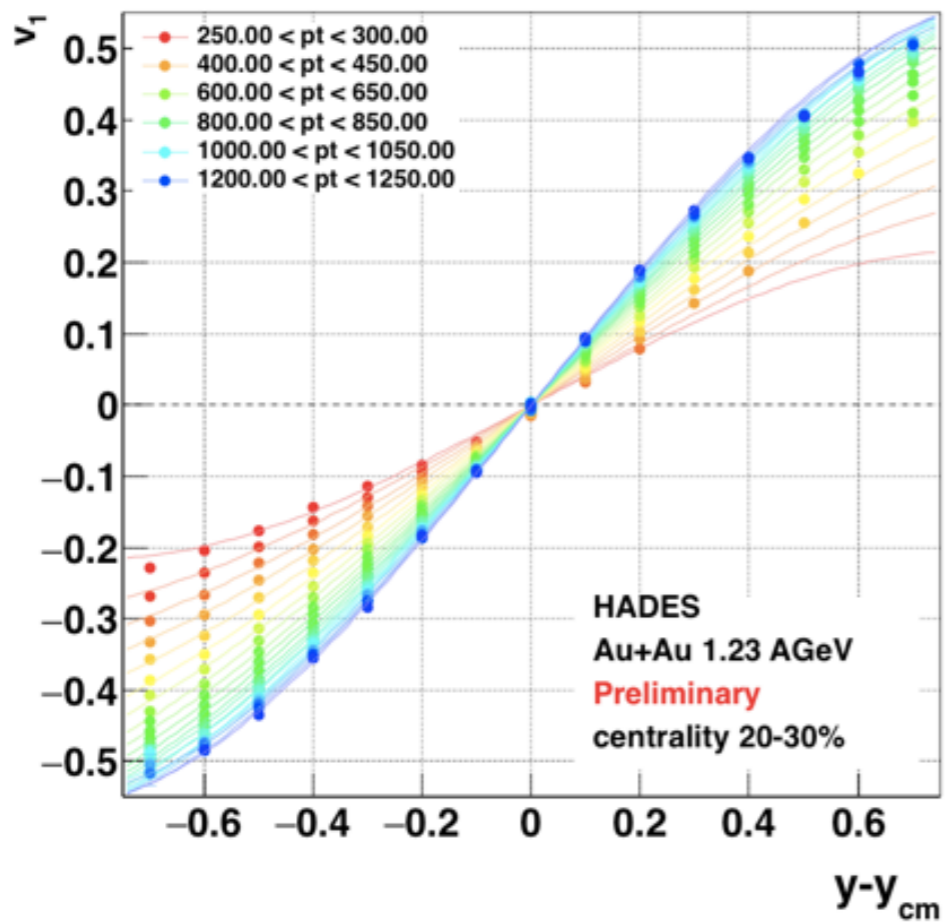
Pure Flow



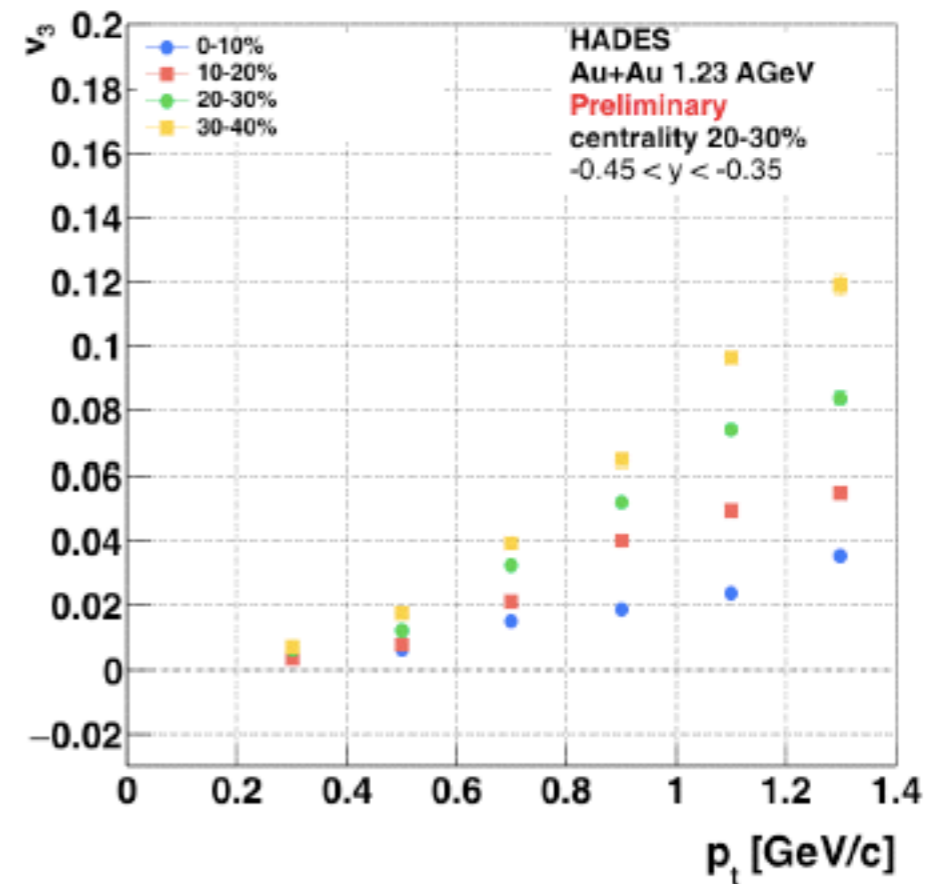
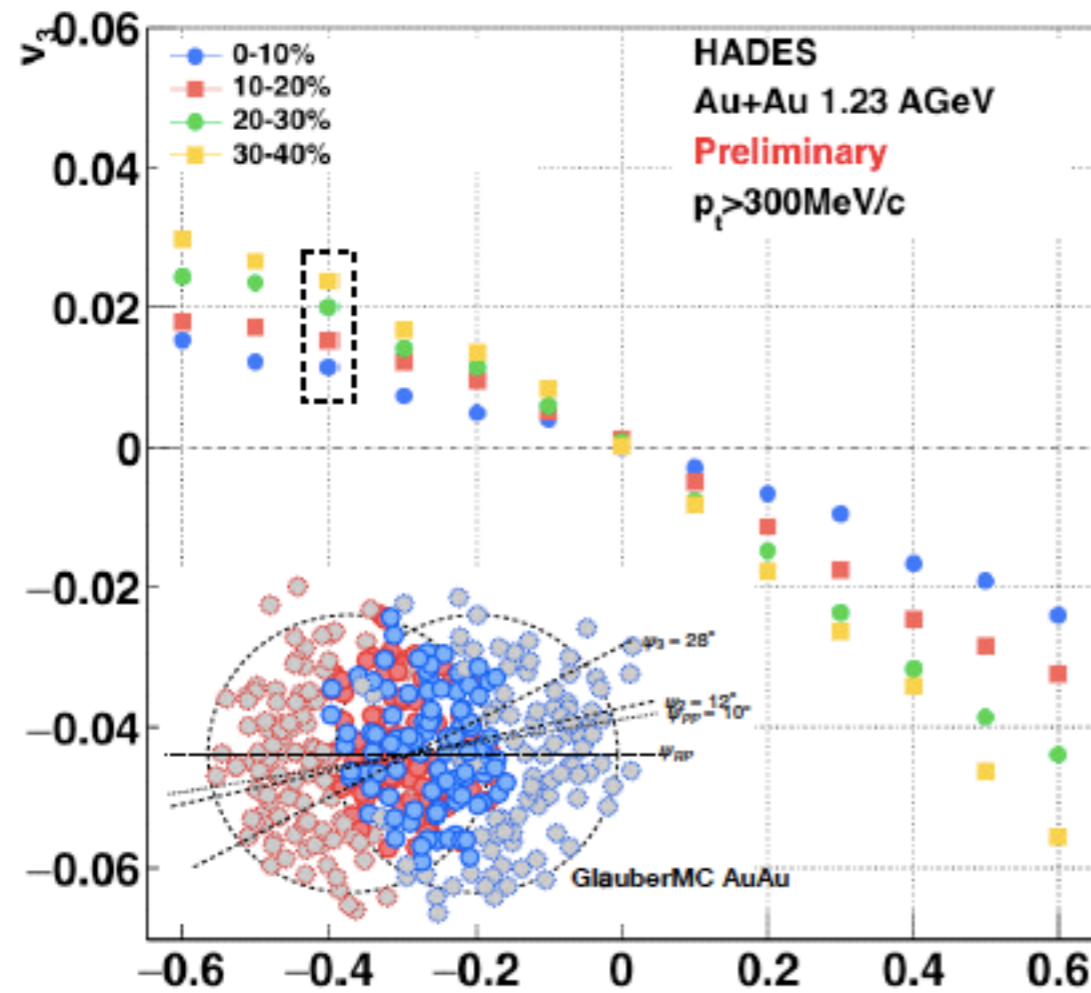
With Non-Flow



- Flow dominates at forward and middle pseudorapidity



Proton $v_3\{\Psi_{RP}\}$



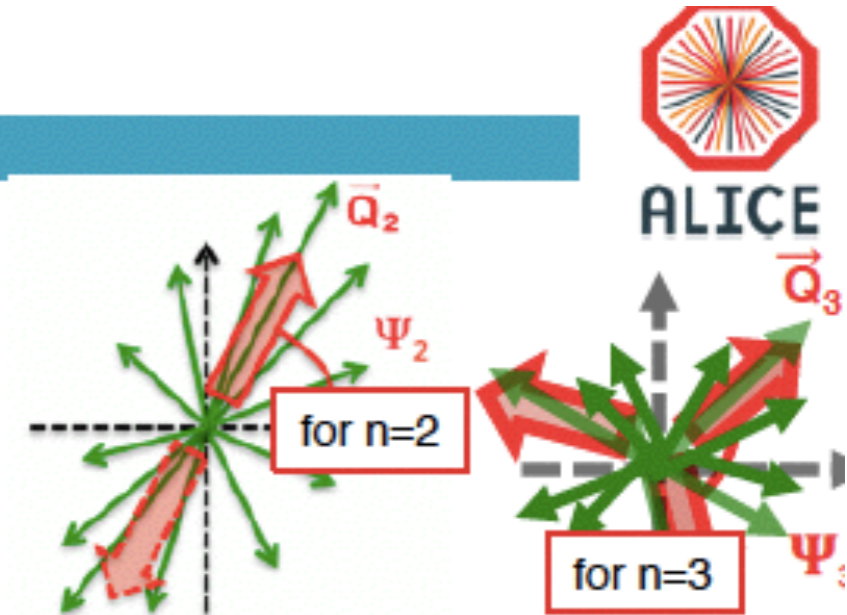
$$\begin{aligned}
 v_3\{\Psi_{RP}\} &= \langle \langle \cos 3(\varphi - \Psi_{RP}) \rangle \rangle \\
 &= \langle \langle \cos 3(\varphi - \Psi_3) \cos 3(\Psi_3 - \Psi_{RP}) \rangle \rangle \\
 &= \langle v_3\{\Psi_3\} \rangle \langle \cos 3(\Psi_3 - \Psi_{RP}) \rangle
 \end{aligned}$$

$y-y_{cm}$

- Note: $v_3\{\Psi_{RP}\}$ w.r.t reaction plane
- Convolution of fluctuation of initial state (Ψ_3) and spectator plane

25 Event shape engineering

- New tool to select the initial source geometry [1]
 - ▣ by the magnitude of the flow vector Q_n



$$|Q_n| = \sqrt{Q_{n,x}^2 + Q_{n,y}^2}$$

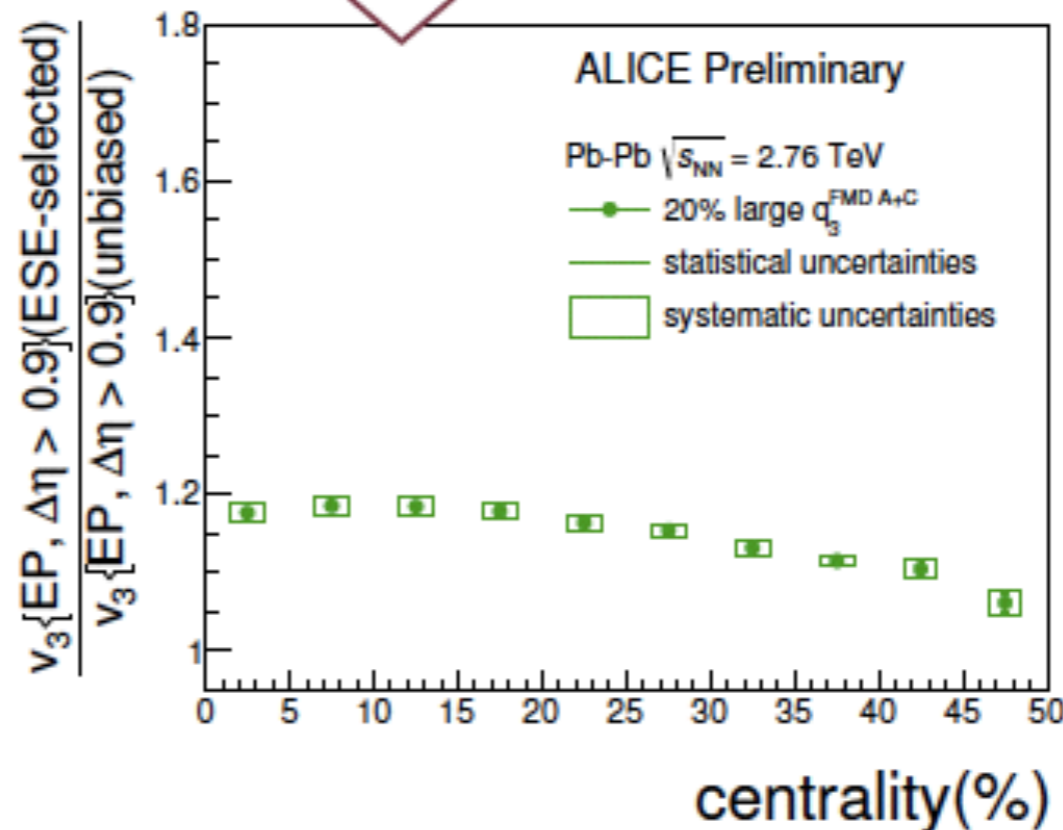
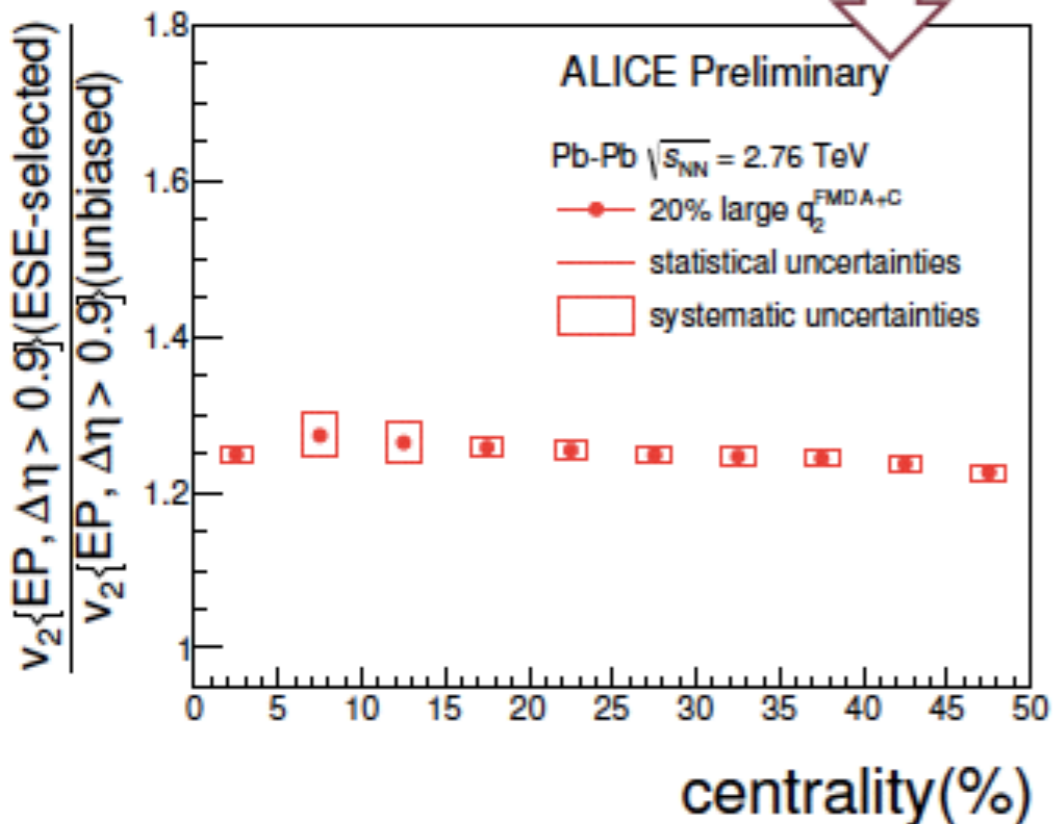
$$Q_{n,x} = \sum w_i \cos n\varphi_i$$

$$Q_{n,y} = \sum w_i \sin n\varphi_i$$

$$q_n = \frac{|Q_n|}{\sqrt{M}}$$

M : the multiplicity of the events

Effect of large q_n selection on v_n

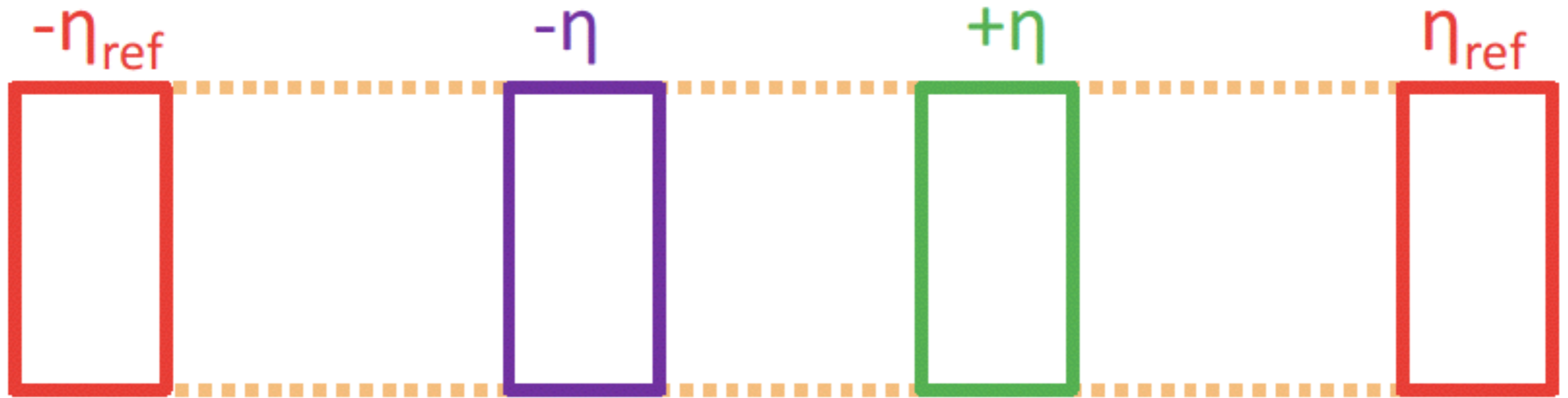


In selected events v_2 is increased about 25% and v_3 about 15%

[1] J. Schukraft, A. Timmins, and S. A. Voloshin, Phys.Lett. B719 (2013)

How to measure twist only

Flow Vector $\mathbf{q}_n \equiv \frac{\sum_i w_i e^{in\phi_i}}{\sum_i w_i} \equiv q_n e^{in\Psi_n}$



$$R_{n,n|n,n} = \frac{\langle q_n(-\eta_{\text{ref}}) q_n(-\eta) q_n^*(+\eta) q_n^*(\eta_{\text{ref}}) \rangle}{\langle q_n(-\eta_{\text{ref}}) q_n(+\eta) q_n^*(-\eta) q_n^*(\eta_{\text{ref}}) \rangle}$$

$$R_{n,n|n,n} \approx 1 - 4F_{n;2}^{twi} \eta$$

This correlator is sensitive only to the event-plane twist